

Interaction theory – Neutrons

Lesson FYSKJM4710

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Sources:

F. H. Attix: Introduction to radiological physics and radiation dosimetry (ISBN 0-471-01146-0)

P. Rinard: Neutron interactions with matter

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The neutron

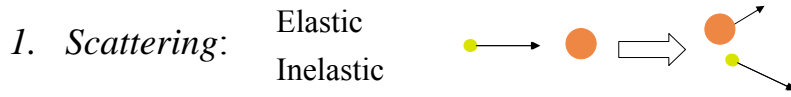
- Uncharged particle, mass close to that of proton
- Unstable as free particle; disintegrates into a proton, an electron and an antineutrino ($t_{1/2}=12$ min)
- Do not interact with electrons
- Only nuclear interactions; complex cross sections
- Neutron attenuation similar to that for photons

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Neutron interactions

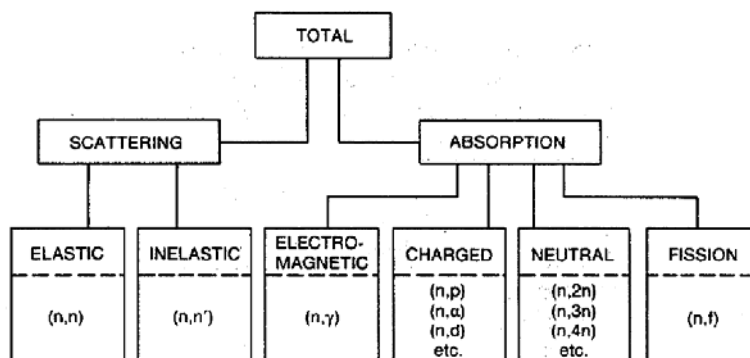
- Principally two types of interaction with matter:



2. *Absorption*: creation of compound nucleus, deexcitation yields p, α , fission products

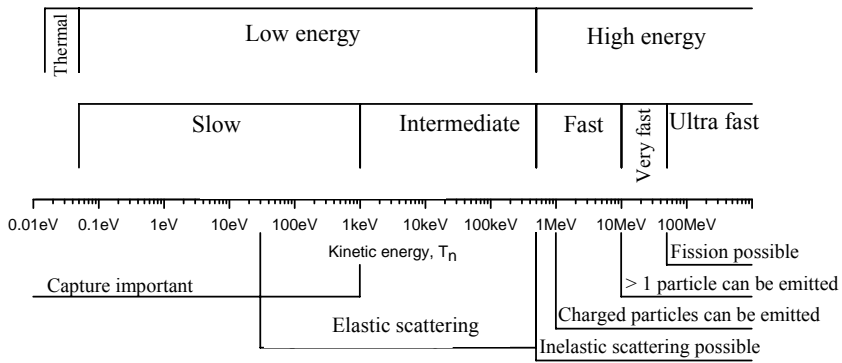


Interactions



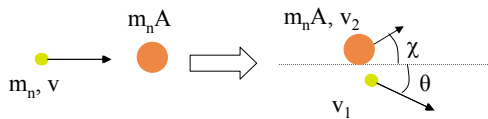
Interactions

- Cross section depends on:
 - Kinetic energy T_n
 - Nuclear structure



Neutron moderation 1

- Elastic scattering against nucleus – energy of neutron after scattering:



$$E_{max} = \frac{1}{2} (m_n A) v_{2,max}^2 = 4 \frac{A m_n^2}{(m_n + A m_n)^2} T_0$$

$$= 4 \frac{A}{(A + 1)^2} T$$

- Hydrogen rich absorbers most effective



Neutron moderation 2

- It may be shown that, after n interactions, the *average* neutron energy is:

$$T_n = T_0 \left[\frac{A^2 + 1}{(A + 1)^2} \right]^n \quad \Rightarrow \quad n = \frac{\ln\left(\frac{T_n}{T_0}\right)}{\ln\left[\frac{A^2 + 1}{(A + 1)^2}\right]}$$

Table 12-1. Average number of collisions required to reduce a neutron's energy from 2 MeV to 0.025 eV by elastic scattering

Element	Atomic Weight	Number of Collisions
Hydrogen	1	27
Deuterium	2	31
Helium	4	48
Beryllium	9	92
Carbon	12	119
Uranium	238	2175

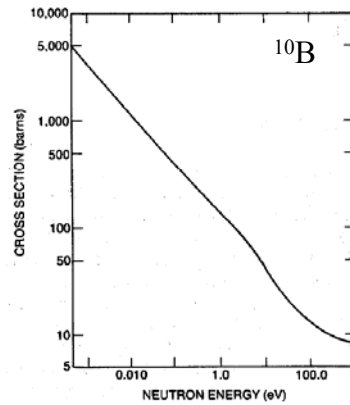


Low energies, $T_n < 500$ keV

- “Potential” (1) and “resonance” (2) elastic scattering:
 - Scattering on the nuclear ‘surface’
 - Neutron absorbed, but reemitted
 For (1): virtually constant cross section
- At thermal energies, the neutron is captured and the compound nucleus deexcites via e.g. γ emission
cross section $\sim 1/v_n$



“1/v” cross section



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Thermal neutrons

- For neutrons in thermal equilibrium with surroundings:

$$T_n = kT = 0.025 \text{ eV at } T = 293 \text{ K}$$

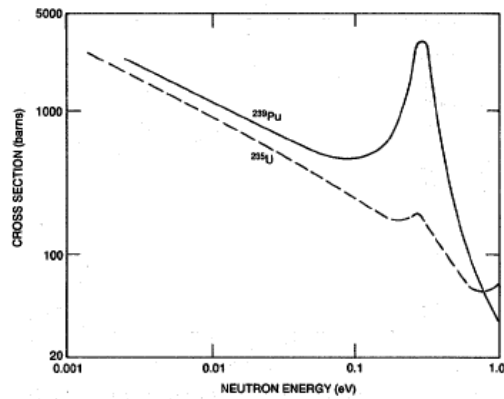
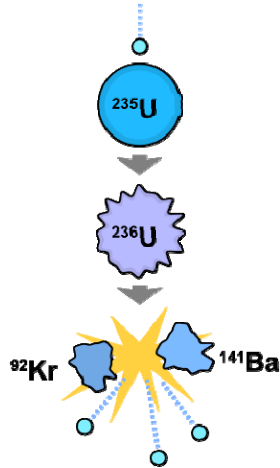
(k: Boltzman constant)

- ^{235}U has a high cross section for capture of thermal neutrons – gives fission

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Fission



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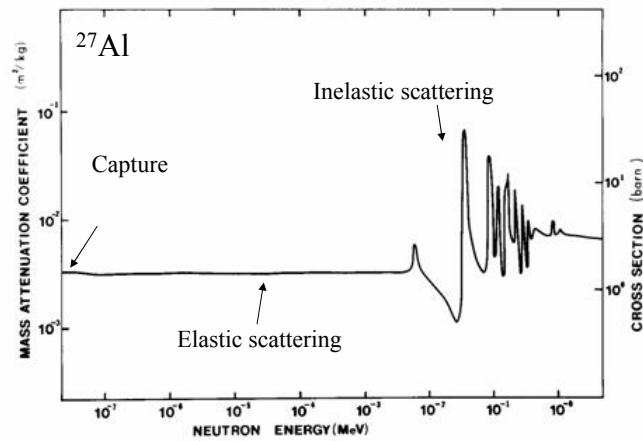
High energy neutrons, $T_n > 0.5 \text{ MeV}$

- Inelastic: $(n, n\gamma)$, threshold kinetic energy $\sim 0.5 \text{ MeV}$
- Occurs at given energies: *resonances*
- Capture reactions: (n, p) , (n, α)
- Emission of more than one particle:
 (n, np) , $(n, n\alpha)$ (threshold $\sim 10 \text{ MeV}$)
- Complicated cross sections

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Cross section



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Neutron attenuation

- For a thin neutron beam:

$$N = N_0 e^{-\mu x}$$

- μ is the attenuation coefficient:

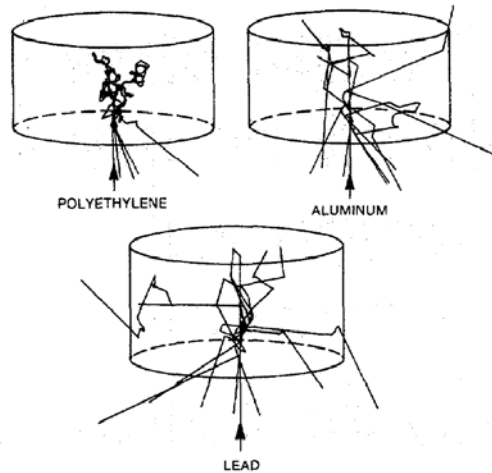
$$\mu = \rho \frac{N_A}{A} \sigma$$

- Note: the cross section σ may show extreme variations over small energy range

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Monte Carlo simulations

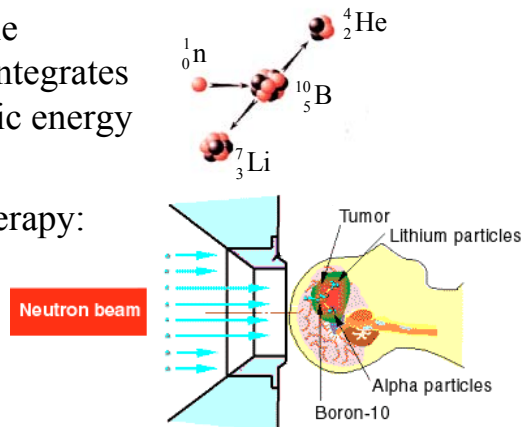


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Boron neutron capture therapy

- Thermal neutrons are efficiently captured by ^{10}B
- Result is an unstable nucleus which disintegrates ^7Li og ^4He (+ kinetic energy and a photon)
- May be used for therapy:



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