

### **Refinement – basic concepts and ideas**

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Øystein Haugen



### **Objectives for the lectures on refinement**

#### The two lectures on refinement aim to

- to motivate and explain a basic apparatus to define and relate the notions of refinement
  - this includes
    - representing executions by traces
    - explaining the significance of a notion of observation
    - outlining the assumption-guarantee paradigm
- introduce and related the following notions of refinement
  - supplementing
  - narrowing
  - detailing
  - property refinement
  - interface refinement
- Illustrate the use of these notions of refinement
  - the interplay between specification and refinement



#### The role of refinement

 System development makes use of refinement as a means to check and document incremental steps aiming to

- reduce the set of legal implementations
- introduce error handling
- introduce time constraints
- introduce finer granularity of interaction and execution
- introduce implementation dependent data types
- introduce implementation oriented communication protocols
- introduce constraints on unlimited resources
- extend the input domain



### Why refinement is important

 Systems of today are large and complex – abstraction is a necessary means to

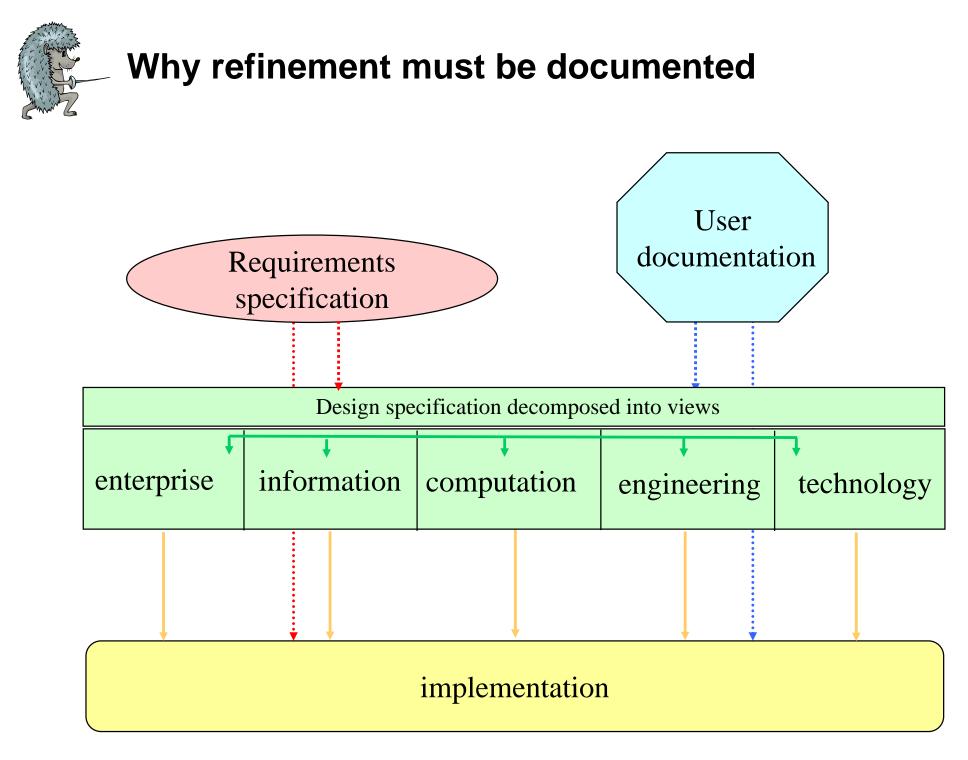
- explain what the systems do
- explain how the systems are built
- distinguish the essentials from the inessential
- decompose large and complicated aspects into small more easily understandable entities
- extract specialized system views
- Formal documentation gives new possibilities

#### Refinement

- relates system descriptions at different levels of abstraction
- connects and relates different system views
- provides a foundation for verifications and validations

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system



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### **Documenting refinement**

- Precision is just as important when we document refinements as when we write specifications
- Refinements can be documented using standard specification languages
  - in INF 5150 we will use UML for this purpose
- Formal documentation of refinements facilitates integrated analysis, validation, testing and verification



### Three main concepts of language theory

#### Syntax

 The relationship between symbols or groups of symbols independent of content, usage and interpretation

#### Semantics

- The rules and conventions that are necessary to interpret and understand the content of language constructs
- Pragmatics
  - The study of the relationship between symbols or groups of symbols and their interpretation and usage



#### Semantic relation

Set of syntactically correct expressions in the language to be explained

What does it mean that a language is wellunderstood?

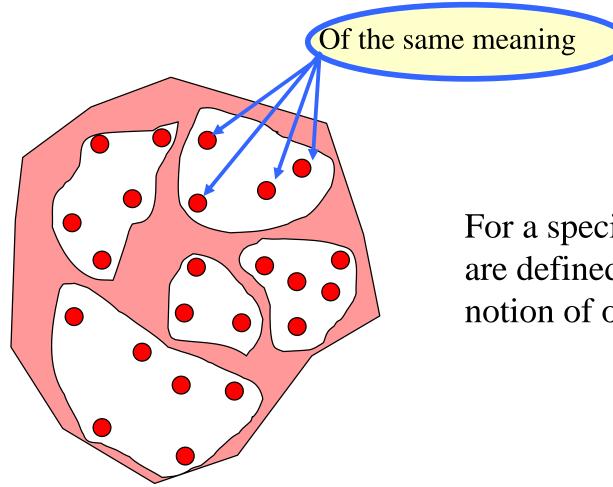
Semantic relation

Relates expressions that need interpretation to expressions that are wellunderstood Øystein Haugen Set of syntactically correct expressions in a language that is wellunderstood



### The need for a notion of observation

A semantic relation will define an equivalence relation on the language that should be understood



For a specification language these are defined with respect to a notion of observation

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### Definition of a notion of observation

- May observe only external behavior
- May observe any potential behavior
- May observe time with respect to a global clock
- May observe safety properties
  - Always falsified by a partial execution
- May observe liveness
  - Falsified only by complete executions



# May our notion of observation be implemented by a human being?



### **Assumption-guarantee paradigm**

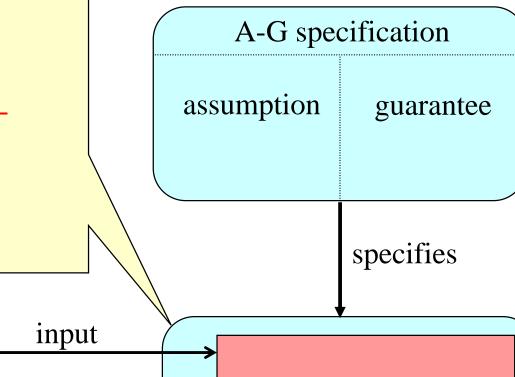
Well-known specification technique to facilitate modularity

- appeared first with pre-post specifications in the 60ies
- since then taken further and adapted in many directions
- referred to as: pre-post, rely-guarantee, assumption-commitment, assumption-guarantee, contracts, goal-means-task
- Motivation:
  - The behavior of a system component depends on the context it is executed in
  - Not all contexts are equally interesting
- The assumption describes expected input
  - The input that can be produced by the relevant contexts
- The guarantee describes the output the specified component is obligated to produce as long as the context behaves in accordance with the assumption



### **Graphical illustration of the A-G paradigm**

NOTE: The A-G paradigm does not specify the context – only the context's interaction with the system in question



Context

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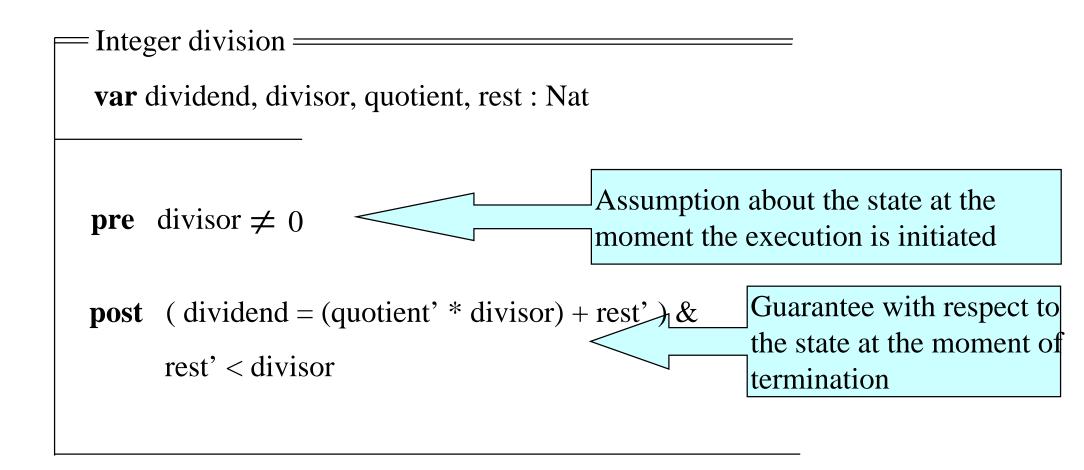
output

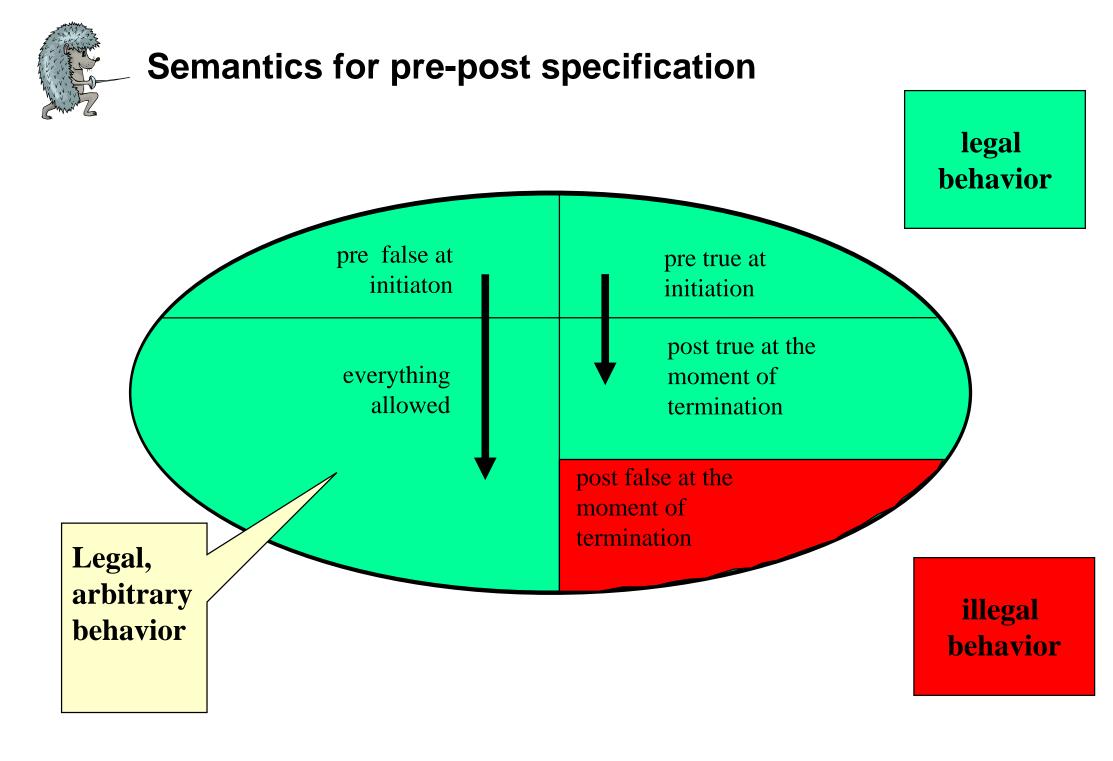
System



### **Pre-post specifications**

Pre-post specifications are based on the assumption-guarantee paradigm





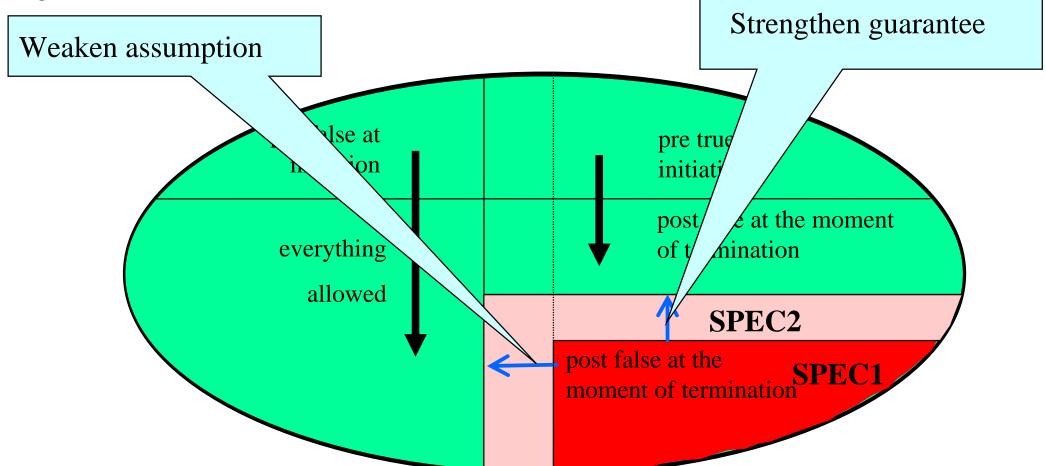


### Semantics for pre-post specifications

- A state is a function from the set of variable names to type correct values
  - e.g.,
    - state(dividend)=600
    - state(divisor)=6
    - state(quotient)=100
- A state S satisfies a pre-condition if the condition evaluates to true when for any variable v
  - S(v) is substituted for each occurrence of v in the condition
- A pair of states (S,S') satisfies a post-condition if the condition evaluates to true when for any variable v
  - S(v) is substituted for each occurrence of v in the condition
  - S'(v) is substituted for each occurrence of v' in the condition
- The semantics of a pre-post specification is the set of all pairs of states (S,S') such that
  - S satisfies pre and (S,S') satisfies post, or
  - S does not satisfy pre
  - In other words: pre(S) => post(S,S')
- We use [SPEC] to denote the semantics of the pre-post specification SPEC



### Property refinement for pre-post specifications



#### SPEC2 is a property refinement of SPEK1 if [SPEC2] is contained in [SPEC1]

This corresponds to logical implication

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### Weakening the pre-condition (assumption)

= Integer division ===

var dividend, divisor, quotient, rest : Nat

pre true

post

```
if divisor ≠ 0 then
  ( dividend = (quotient' * divisor) + rest' ) & rest' < divisor
else quotient' = 0</pre>
```



### Strengthening the post-condition (guarantee)

=Integer division ===

var dividend, divisor, quotient, rest : Nat

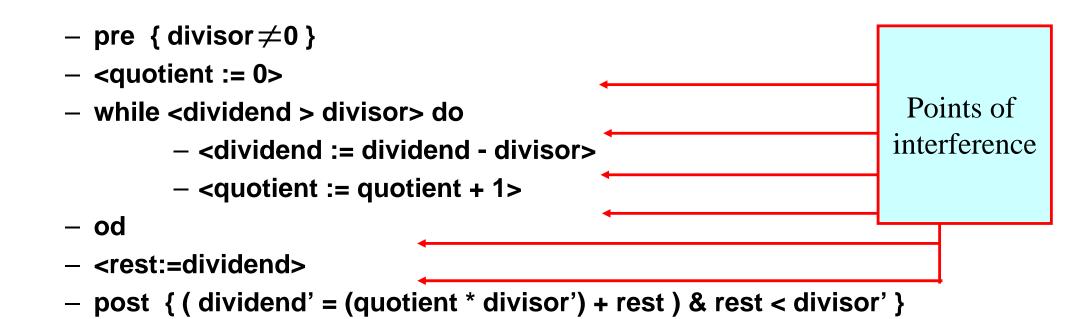
**pre** divisor  $\neq 0$ 

post ( dividend = (quotient' \* divisor) + rest' ) &
 rest' < divisor & dividend' = dividend &
 divisor' = divisor</pre>



### The shortcomings of pre-post specifications

Pre-condition describes only what the context may do before the operation is started up – not what the context may do during the execution of the operation



• "<Statement>" denotes that "statement" is atomic (in the meaning that the context cannot interfere with its execution)

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- Traces are used to represent system runs matematically
- In the literature there are many different kinds of traces
- INF 5150 traces are sequences of events

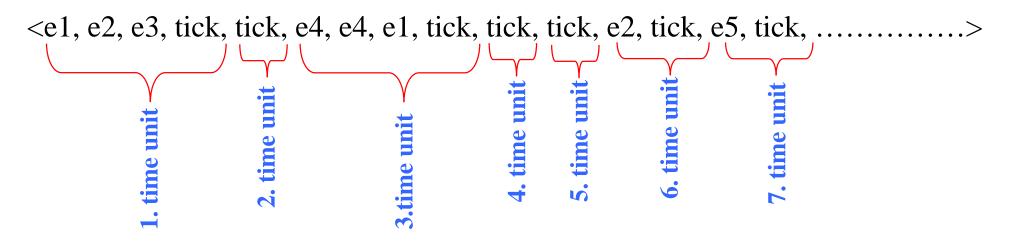
<e1, e2, e3, e4, e4, e1, e2, e5, .....>

- Events are instantaneous
- The number of events in a trace may be finite
  - may be caused by: termination, deadlock, infinite waiting, system crash
- The number of events in a trace may be infinite
  - May be cause by: nontermination, livelock, nontermination by purpose



#### **Traces with time ticks**

#### Traces are infinite sequences of events and time ticks



- Events and time ticks are instantaneous
- Each trace contains infinitely time ticks
  - this reflects that time never halts
- The number of events in a trace may be finite



### **Traces with time stamps**

Each element of the trace is a pair of an event and a time stamp

<e1:t1, e2:t2, e3:t3, e4:t4, e4:t5, e1:t6, e2:t7, e5:t8, .....>

The elements are ordered according to their time stamps

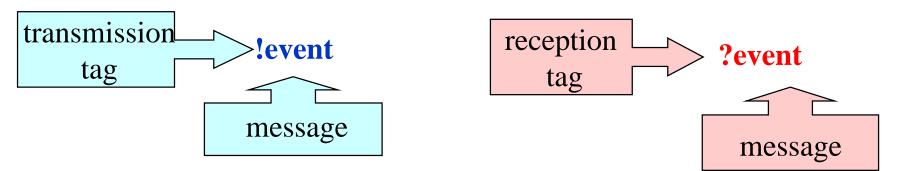
- (t1<=t2<=t3 ....)
- Events are instantaneous
- A trace is either finite or there is for every point in time k an element n:t with time stamp t such that k< t</p>
  - this is necessary to avoid Zenon's paradox

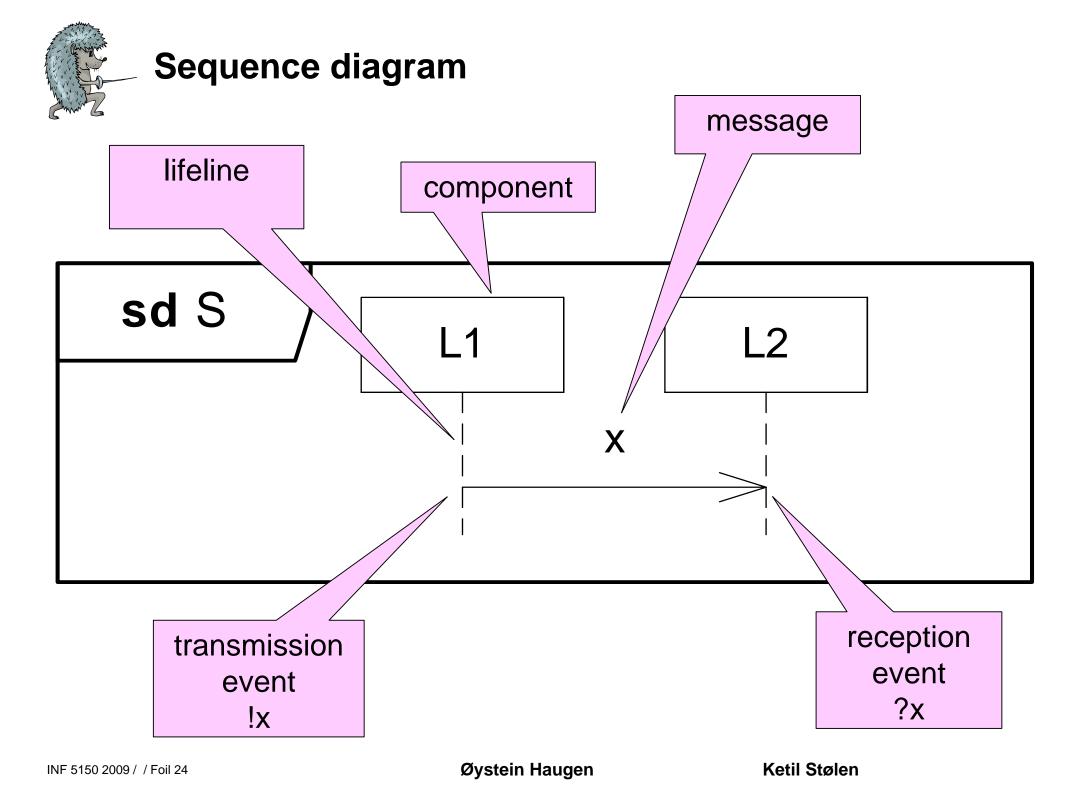


### **Traces for sequence diagrams**

#### • Two kinds of events:

- transmission events
- reception events







### Causality and weak sequencing

### Causality:

- a message can never be received before it has been transmitted
- the transmission event for a message is therefore always ordered before the reception event for the same message

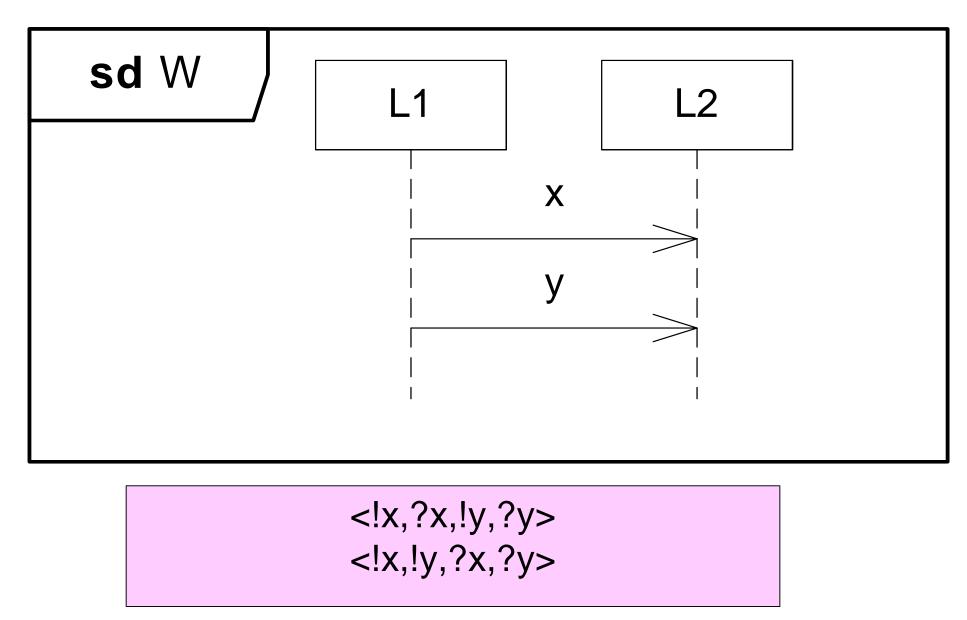
#### • Weak sequencing:

 events from the same lifeline are ordered in the trace in the same order as on the lifeline

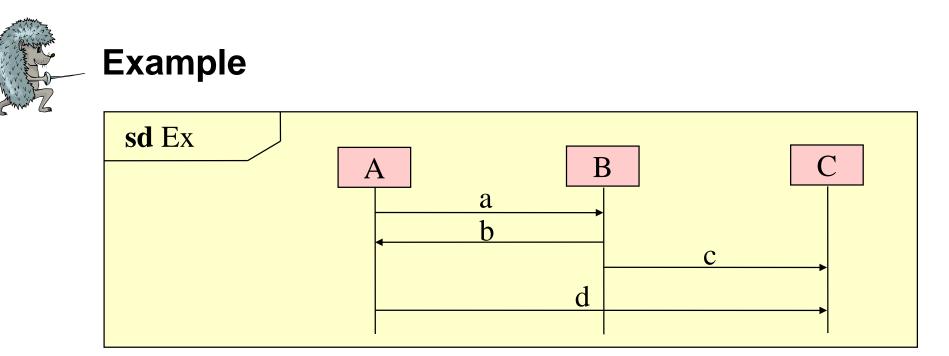
#### NOTE: A sequence diagram will normally be represented by more than one trace, and in some cases by infinitely many traces



### Weak sequencing



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There are six possible traces if time information is ignored:

<!a, ?a, !b, ?b, !c, ?c, !d, ?d> <!a, ?a, !b, ?b, !c, !d, ?c, ?d> <!a, ?a, !b, ?b, !d, !c, ?c, ?d> <!a, ?a, !b, !c, ?b, ?c, !d, ?d> <!a, ?a, !b, !c, ?b, !d, ?c, ?d> <!a, ?a, !b, !c, ?c, ?b, !d, ?d>

Each of these corresponds to infinitely many traces with time information

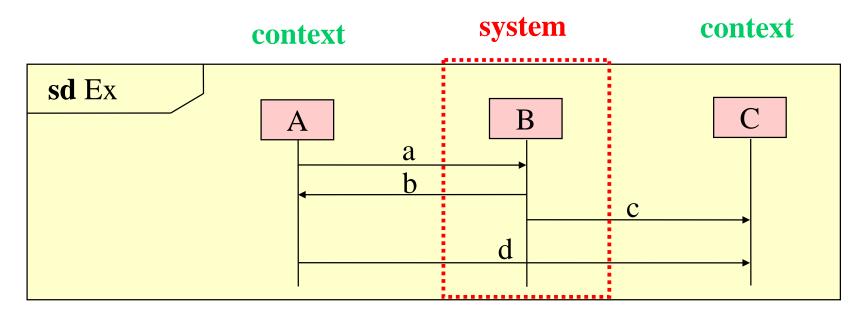
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#### **External behavior**

- Property refinement in the classical sense takes only external behavior into consideration
- We therefore need a well-defined interface between
  - the component to be refined, and
  - its context





System has one possible external trace:

<?a, !b, !c>

This trace is an abstraction of infinitely many traces with time information

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## - STAIRS -Steps to Analyze Sequence Diagrams with Refinement Semantics

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#### **Motivation**

Make use of classical refinement theory in a practical UML setting

- From theory to practice, and not the other way around
- We aim to explain how classical theory of refinement can be used to refine specifications expressed with the help
- Sequence diagrams can be used to explain other kinds of UML diagrams
- By defining refinement for sequence diagrams we implicitly define refinement for the UML as a whole



### **Requirements to STAIRS**

- Should support specification of potential behavior
  - Means to abstraction
- Should support specification of mandatory behavior
  - Important within the security domain
- Should support specification of negative behavior in addition to positive behavior
- Should support classical refinement theory
- Should formalize incremental system development
- Should facilitate modular analysis, verification and testing



### Next lecture on refinement – September 18

- Example based introduction to STAIRS
- Semantics of sequence diagrams
- Refinement in STAIRS
  - Supplementing
  - Narrowing
  - Detailing
- Relation to pre-post