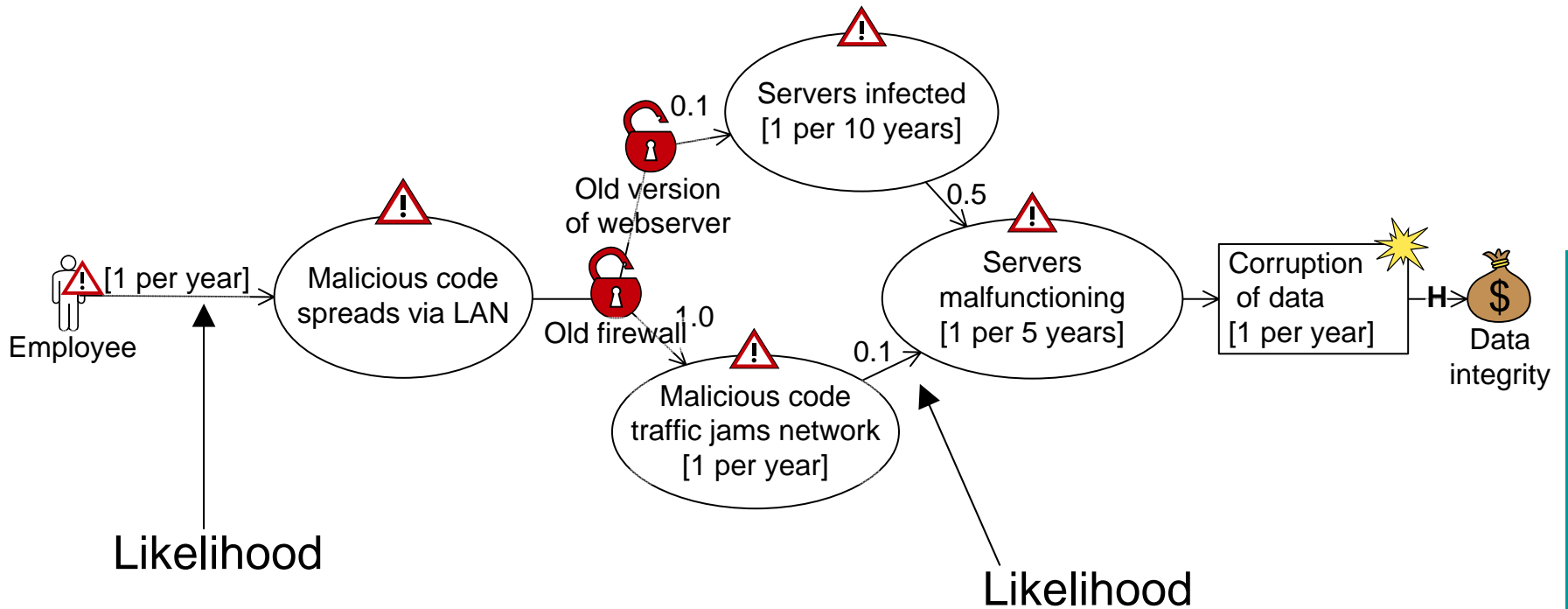




Solution to exercises

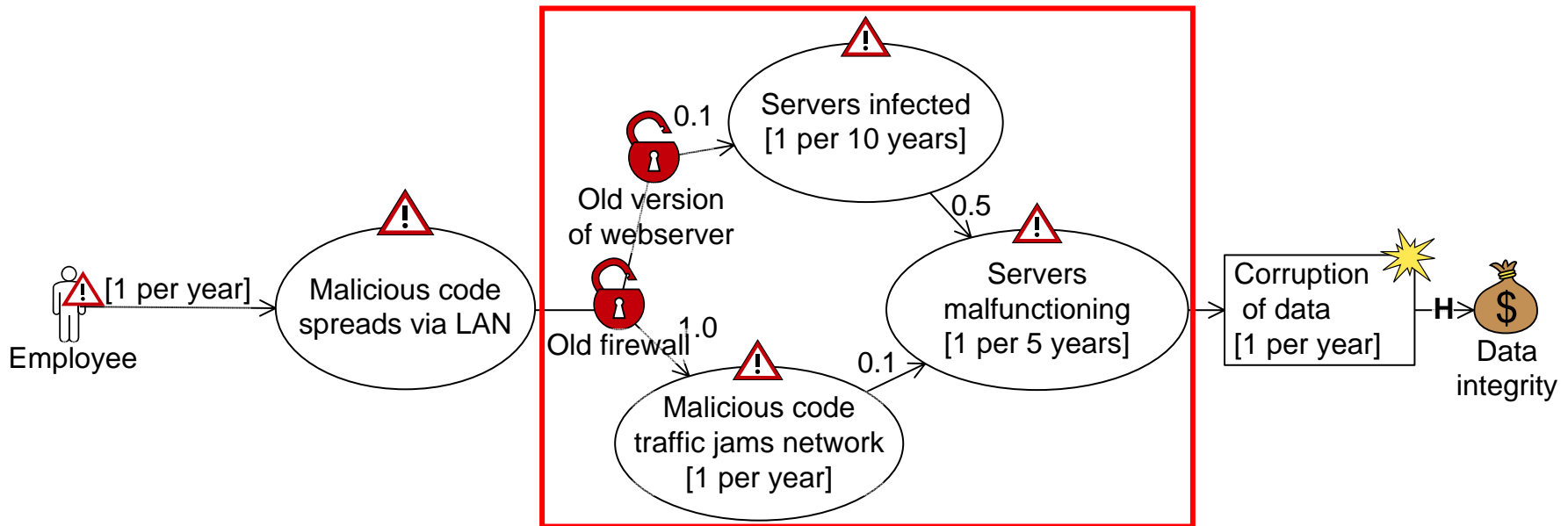


Building a threat diagram (4)



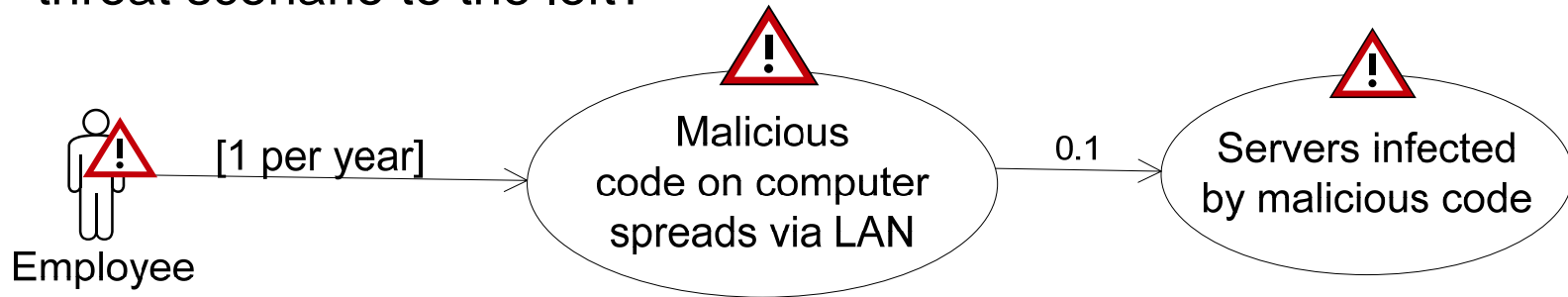
Consistency checking of likelihoods

- Use the CORAS calculus to check the consistency of assigned likelihood values



Exercise I, 1a) – initiate rule

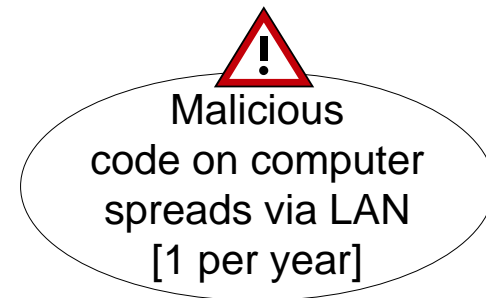
- What is the likelihood of the threat scenario to the left?



- If the vertices t and v are related by initiate, we have:

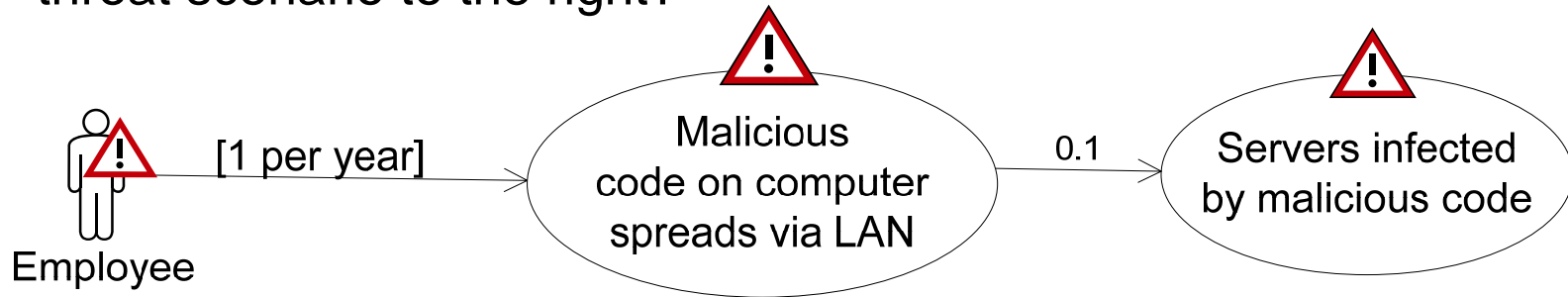
$$\frac{t \xrightarrow{l} v}{(t \sqcap v)(l)}$$

- i.e.:



Exercise I, 1b) – leads-to rule

- What is the likelihood of the threat scenario to the right?



- If the vertices v_1 and v_2 are related by leads-to, we have:
 - $1 \text{ per } 1 \text{ year} \times 0.1 = 1 \text{ per } 10 \text{ years}$

$$\frac{v_1(f) \quad v_1 \xrightarrow{l} v_2}{(v_1 \sqcap v_2)(f \cdot l)}$$

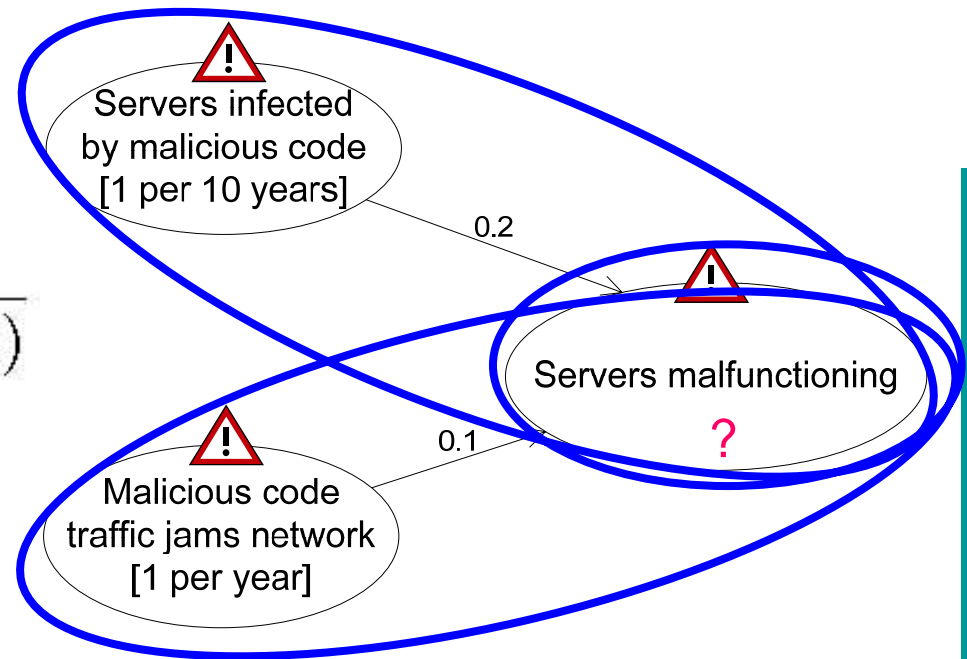


2a) Leads-to + statistically independent vertices

- 1 per 10 years \times 0.2 = 1 per 50 years
- 1 per 1 year \times 0.1 = 1 per 10 years
- If the vertices v_1 and v_2 are statistically independent, we have:

$$\frac{v_1(f_1) \quad v_2(f_2)}{(v_1 \sqcup v_2)(f_1 + f_2 - f_1 \cdot f_2)}$$

- $(1/50 + 1/10) - (1/50 \times 1/10) =$
1.18 per 10 years

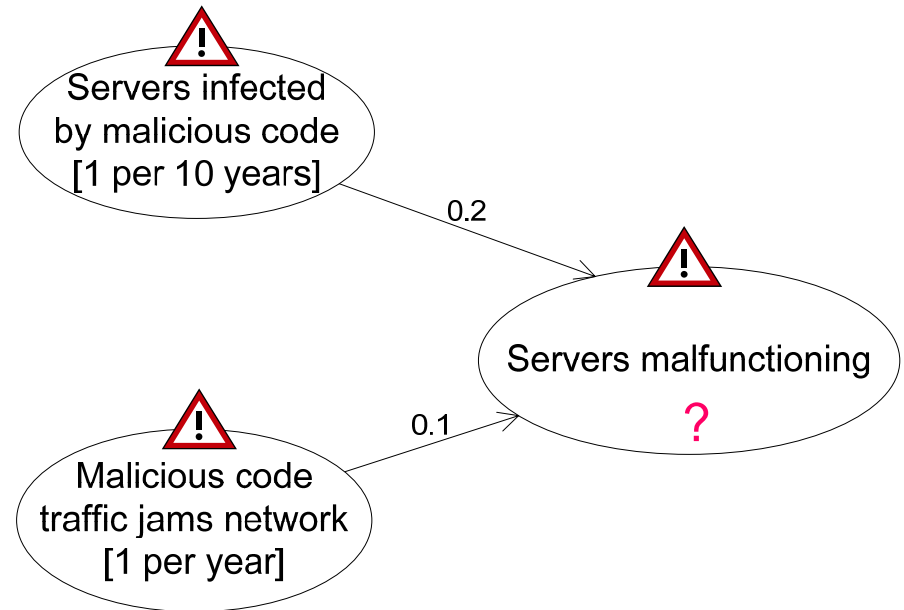


2b) Leads-to + mutually exclusive vertices

- If the vertices v_1 and v_2 are mutually exclusive, we have:

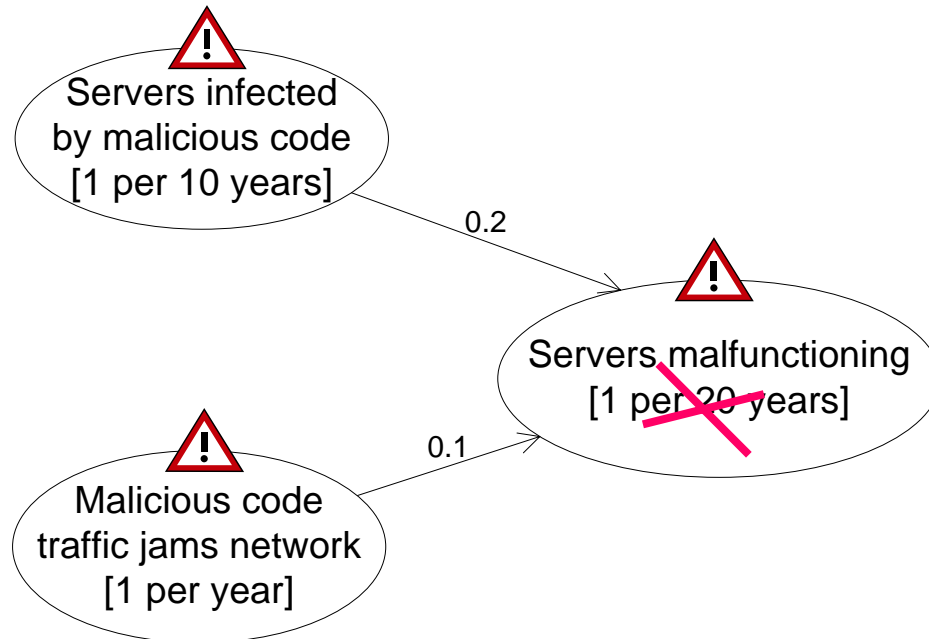
$$\frac{v_1(f_1) \quad v_2(f_2)}{(v_1 \sqcup v_2)(f_1 + f_2)}$$

- $(1/50 + 1/10) = 1.2$ per 10 years



2c) Consistency check

- Both 1.18 per 10 years and 1.2 per 10 years are higher values than 1 per 20 years
- The diagram is inconsistent



Exercise II – computing likelihood intervals

	Scale	Value
1	Rarely	≤ 1 per 10 years
2	Seldom	> 1 per 10 years & ≤ 1 per 5 years
3	Sometimes	> 1 per 5 years & ≤ 1 per 1 year
4	Often	> 1 per 1 year



Exercise I, 1a) – initiate rule

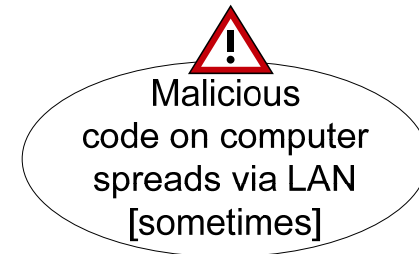
- What is the likelihood of the threat scenario to the left?



- If the vertices t and v are related by initiate, we have:

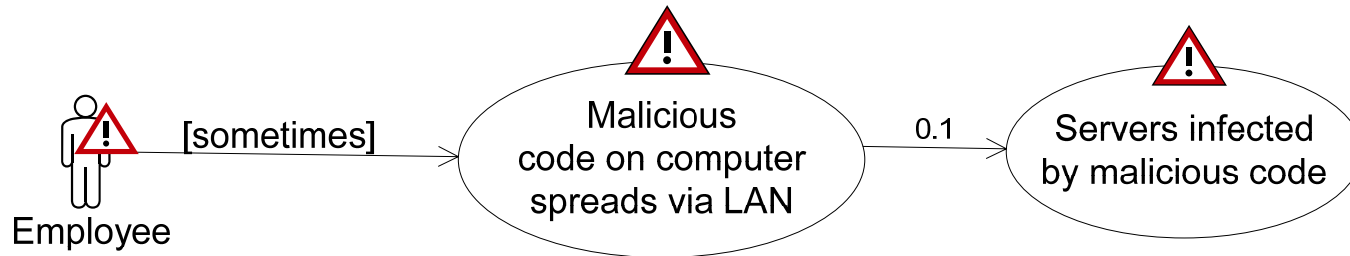
$$\frac{t \xrightarrow{l} v}{(t \sqcap v)(l)}$$

- i.e.:



Exercise I, 1b) – leads-to rule

- What is the likelihood of the threat scenario to the right?



- If the vertices v_1 and v_2 are related by leads-to, we have:

$$\frac{v_1(f)}{(v_1 \sqcap v_2)(f \cdot l)}$$

- sometimes = $\langle 1/5, 1/1 \rangle$
- 1 per 5 years $\times 0.1 = 1$ per 50 years
- 1 per 1 year $\times 0.1 = 1$ per 10 years
- $\langle 1/50, 1/10 \rangle =$ rarely

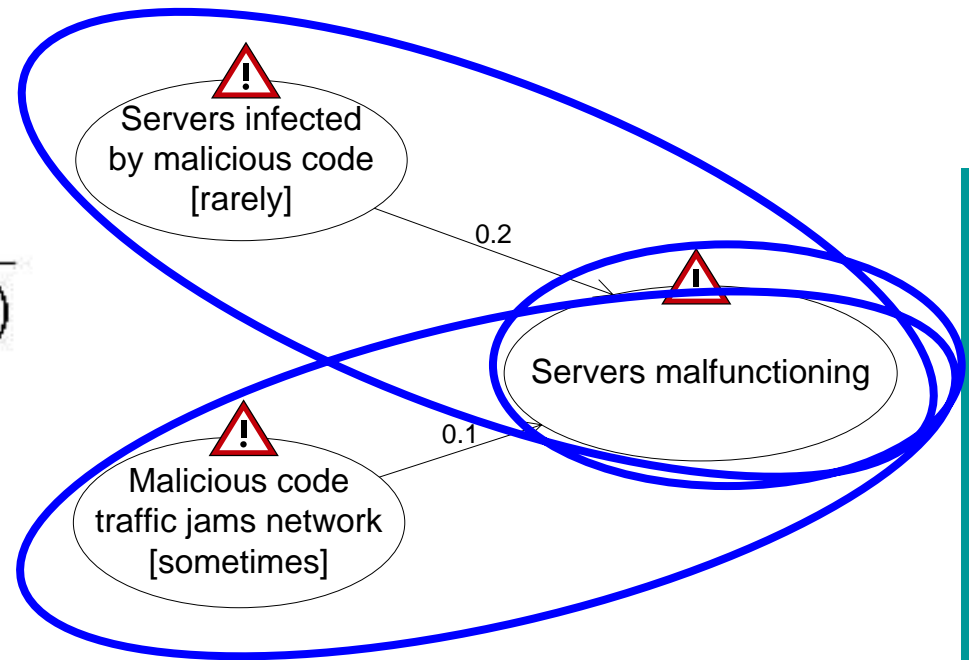


2a) Leads-to + statistical independence

- $[0, 1/10] \times 0.2 = [0, 1/50]$
- $\langle 1/5, 1/1 \rangle \times 0.1 = \langle 1/50, 1/10 \rangle$
- If the vertices v_1 and v_2 are statistically independent, we have:

$$\frac{v_1(f_1) \quad v_2(f_2)}{(v_1 \sqcup v_2)(f_1 + f_2 - f_1 \cdot f_2)}$$

- $([0, 1/50] + \langle 1/50, 1/10 \rangle) - ([0, 1/50] \times \langle 1/50, 1/10 \rangle) = \langle 1/50, 1.18/10 \rangle$
- 1.18 per 10 years \in seldom
- we interpret this as seldom

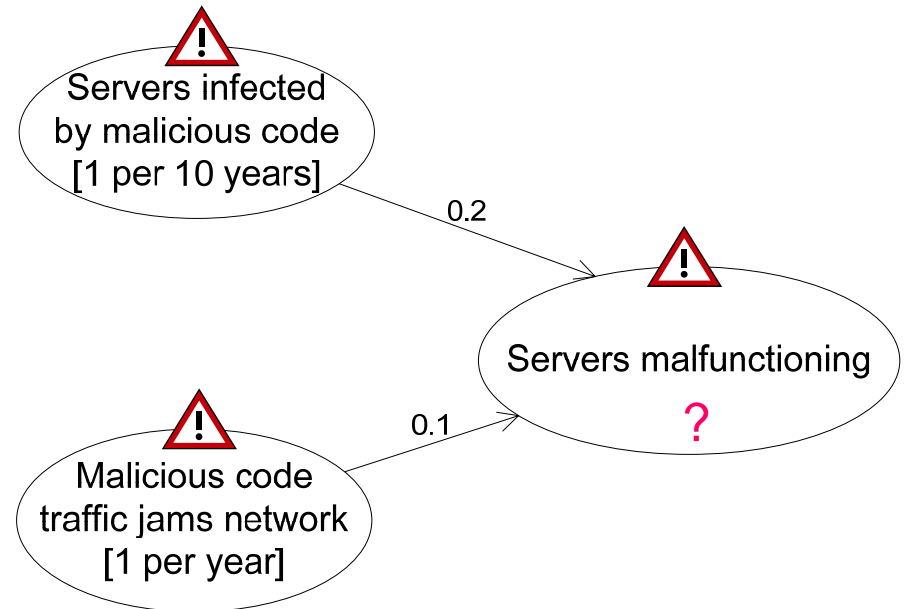


2b) Leads-to + mutually exclusive vertices

- If the vertices v_1 and v_2 are mutually exclusive, we have:

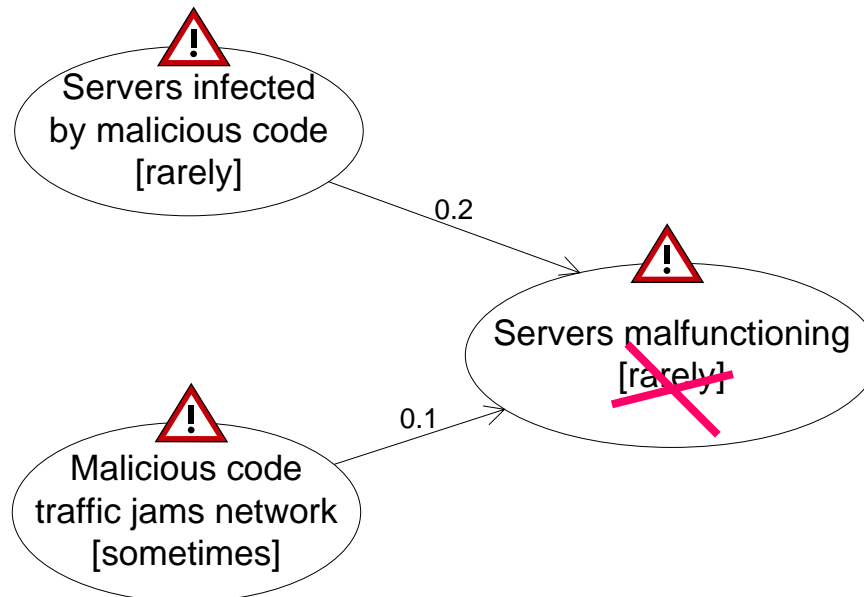
$$\frac{v_1(f_1) \quad v_2(f_2)}{(v_1 \sqcup v_2)(f_1 + f_2)}$$

- $([0, 1/50] + <1/50, 1/10]) = <1/50, 1.2/10]$
- 1.2 per 10 years \in seldom
- we interpret this as seldom

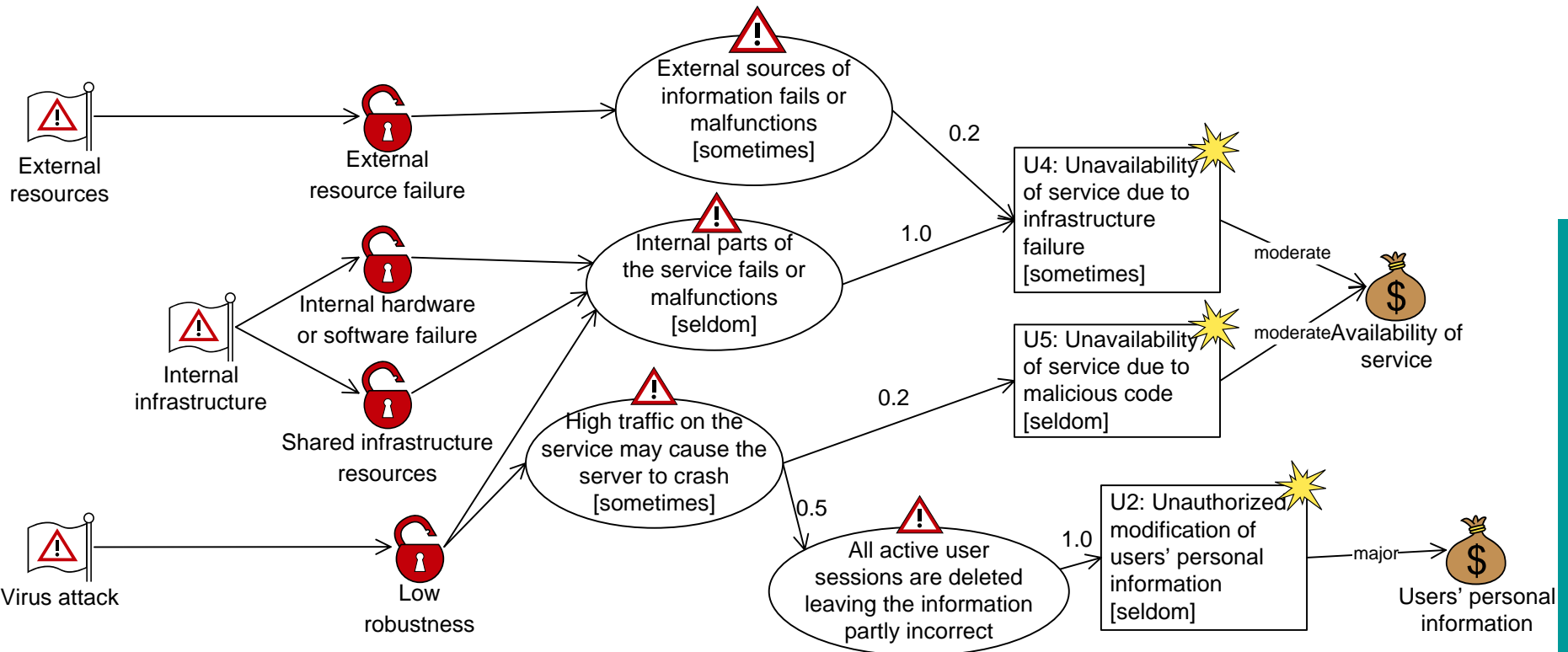


2c) Consistency check

- seldom > rarely
- The diagram is inconsistent

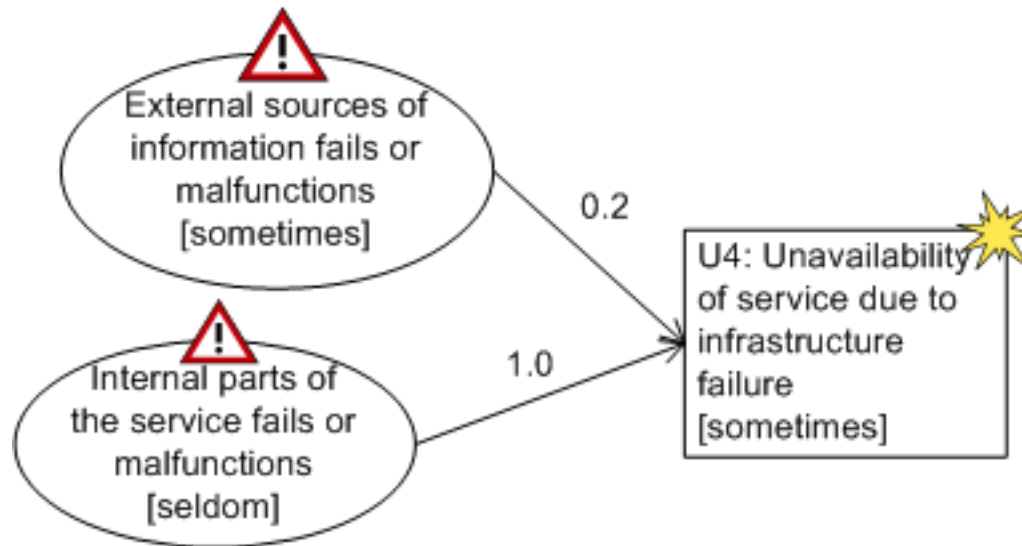


3a) Consistency check



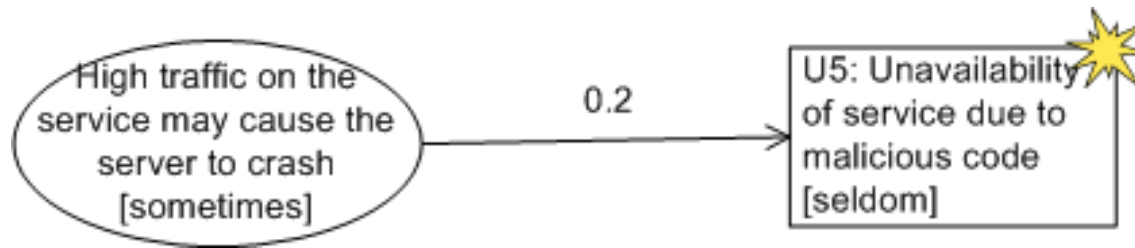
Consistency check

- We look at max values:
- 1 per 1 year \times 0.2 = 1 per 5 years
- 1 per 5 years \times 1.0 = 1 per 5 years
- (1 per 5 years + 1 per 5 years) - (1 per 5 years + 1 per 5 years)
= 1.8 per 5 years \in sometimes OK



Consistency check

- 1 per 1 year \times 0.2 = 1 per 5 years \in seldom OK



- 1 per 1 year \times 0.5 = 1 per 2 years \times 1.0 = 1 per 2 years \notin seldom Not OK

