

UNIVERSITY OF OSLO
DEPARTMENT OF ECONOMICS

Exam: ECON4160 - Econometrics - Modeling and systems estimation

Date of exam: Friday, May 21, 2004

Time for exam: 9:00 a.m. – 12:00 noon

The problem set covers 6 pages

Resources allowed:

- All written and printed resources, as well as calculator are allowed

The grades given: A-F, with A as the best and E as the weakest passing grade. F is fail.

Problem 1

We want to estimate the relationship between log hourly wage and labour market experience. The relationship between log hourly wage and experience is given by:

$$(1) \quad \text{LNWAGE}_i = \alpha + \beta \text{ EXPERIENCE}_i + u_i,$$

where α and β are unknown parameters and u_i is a stochastic disturbance.

We have $E(u_i | \text{EXPERIENCE}_i) = 0$ and assume homoskedastic disturbances with no autocorrelation. For this problem we have constructed an experience variable which is considered as the sum of the true experience variable (EXPERIENCE) and a random error (ERROR). We now assume that we cannot observe the true EXPERIENCE variable, only the badly measured one. The badly measured experience variable is thus defined as:

$$(2) \quad \text{EXPERROR} = \text{EXPERIENCE} + \text{ERROR},$$

where ERROR is assumed to be uncorrelated with both EXPERIENCE and u . On the top of page 1 of the printout you will find the mean and variance of the error as well as of the badly measured experience variable for a sample of 681 Norwegian men between ages 18 and 45. The next part of the printout page 1 reports the variances and covariances of log wage (LNWAGE) and the badly measured experience variable. The problem is that we now only observe EXPERROR and not the true value of EXPERIENCE .

- a) From the reported information on the empirical first and second order moments of the distributions of EXPERROR , LNWAGE and ERROR on top of page 1 (the means, variances and covariances) it should be possible to identify β . Explain how and calculate a consistent estimator of β based only on these statistics. Suggest which of these empirical moments that one would be less likely to have information on in real-world data samples.

In terms of the observable variables we have:

$$(3) \quad \text{LNWAGE}_i = \alpha + \beta \text{EXPER}_i + w_i$$

The regression results at (A) in the printout reports an OLS estimate of β in equation (3) of 0.00697.

- b) Explain why this OLS estimator is a biased estimator of β . Do you have enough information on the top of this page to give an estimate of the magnitude of the bias in this case?
- c) The results at (B) in the printout are the results from in instrumental variable regression. In this model, we have used information on the person's AGE as an instrument for the experience variable. Under what crucial assumptions does this method provide us with a consistent estimator of β ? Do you find these assumptions reasonable?

Problem 2

A more comprehensive model of log wages is estimated and the results reported at (C) and (D) in the printout. This model is estimated on data from all workers from 18 to 65 years of age and include years of schooling (YRSCHOOL) as well as a dummy variable for gender (WOMAN) and the true value of experience (EXPERIENCE) and its square (EXPSQUARED):

$$(4) \quad \text{LNWAGE}_i = \alpha_1 + \beta_1 \text{YRSCHOOL}_i + X_i \gamma_{11} + u_i, \quad i=1, \dots, n,$$

where the vector X include (WOMAN, EXPERIENCE, EXPSQUARED), all of which are assumed to be exogenous. The results reported at (C) are from an OLS regression of equation (4). The coefficient for years of schooling is estimated to 0.05461. Some researchers suspect, however, that the schooling variable is endogenous in such an equation. A simple equation describing the determination of years of schooling could be given by:

$$(5) \quad \text{YRSSCHOOL}_i = \alpha_2 + \beta_2 \text{LNWAGE}_i + X_i \gamma_{21} + Z_i \gamma_{22} + v_i, \quad i=1, \dots, n,$$

where the vector X again includes all the exogenous variables in equation (4) (WOMAN, EXPERIENCE, EXPSQUARED) and the vector Z contains a set of variables that are predetermined. These could be fathers' education, mothers' education, the age of the parents etc. We assume that $E(u|X,Z) = E(v|X,Z) = 0$ and that the disturbances u and v are homoskedastic.

- a) Give the order conditions for identification of the structural parameters in these two equations. Which variables should be included in the first step, reduced form regressions of a two-stage least squares estimation of equation (4)?

Part (D) of the printout gives the two-stage least squares estimator where we have used a set of 12 variables describing the parents' education, age and occupation as our Z -vector.

- b) The two-stage least squares estimate of β_1 is 0.07154. This is larger than the OLS estimate of 0.05461. What does this result tell you about the sign of the covariance between YRSCHOOL and u in equation (4)?

- c) At Part (E) of the printout you will find results from an OLS regression of equation (4), augmented with the residual from the reduced form regression of YRSCHOOL. The residual is given the name RESIDUALYRSCHOOL.

Based on the results of this equation, which of the two estimators of β_1 would you rely on, OLS or 2SLS? Explain.

PRINTOUT PAGE 1.

The MEANS Procedure

| Variable | N | Mean | Variance |
|----------|-----|------------|-------------|
| error | 681 | -0.0263547 | 53.8264442 |
| experror | 681 | 13.5771696 | 106.3256153 |

Covariance Matrix, DF = 680

| | lnwage | experror |
|----------|-----------|-------------|
| lnwage | 0.1222462 | 0.7412236 |
| experror | 0.7412236 | 106.3256153 |

PART (A)

OLS estimation

Dependent Variable: lnwage

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 1 | 3.51374 | 3.51374 | 29.97 | <.0001 |
| Error | 679 | 79.61366 | 0.11725 | | |
| Corrected Total | 680 | 83.12740 | | | |
| Root MSE | | 0.34242 | R-Square | 0.0423 | |
| Dependent Mean | | 4.59105 | Adj R-Sq | 0.0409 | |
| Coeff Var | | 7.45843 | | | |

Parameter Estimates

| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
|-----------|----|--------------------|----------------|---------|---------|
| Intercept | 1 | 4.49640 | 0.02171 | 207.16 | <.0001 |
| experror | 1 | 0.00697 | 0.00127 | 5.47 | <.0001 |

PART (B)

Instrumental Variables Estimation

Dependent Variable: lnwage

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 1 | 12.82006 | 12.82006 | 95.63 | <.0001 |
| Error | 679 | 91.02443 | 0.134057 | | |
| Corrected Total | 680 | 83.12740 | | | |
| Root MSE | | 0.36614 | R-Square | 0.12345 | |
| Dependent Mean | | 4.59105 | Adj R-Sq | 0.12216 | |
| Coeff Var | | 7.97503 | | | |

Parameter Estimates

| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
|-----------|----|--------------------|----------------|---------|---------|
| Intercept | 1 | 4.325830 | 0.030535 | 141.67 | <.0001 |
| experror | 1 | 0.019534 | 0.001998 | 9.78 | <.0001 |

PRINTOUT PAGE 2.

PART (C)**OLS estimation**

Dependent Variable: lnwage

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|------|----------------|-------------|---------|--------|
| Model | 4 | 72.37514 | 18.09379 | 253.06 | <.0001 |
| Error | 1942 | 138.85315 | 0.07150 | | |
| Corrected Total | 1946 | 211.22829 | | | |
| Root MSE | | 0.26739 | R-Square | 0.3426 | |
| Dependent Mean | | 4.54814 | Adj R-Sq | 0.3413 | |
| Coeff Var | | 5.87922 | | | |

Parameter Estimates

| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
|------------|----|--------------------|----------------|---------|---------|
| Intercept | 1 | 3.67966 | 0.03639 | 101.13 | <.0001 |
| woman | 1 | -0.16676 | 0.01220 | -13.67 | <.0001 |
| yrsschool | 1 | 0.05461 | 0.00258 | 21.13 | <.0001 |
| experience | 1 | 0.02528 | 0.00190 | 13.32 | <.0001 |
| expsquared | 1 | -0.00038842 | 0.00004122 | -9.42 | <.0001 |

PART (D)**Two-Stage Least Squares Estimation**

Dependent Variable: lnwage

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|------|----------------|-------------|---------|--------|
| Model | 4 | 42.72578 | 10.68144 | 146.16 | <.0001 |
| Error | 1942 | 141.9237 | 0.073081 | | |
| Corrected Total | 1946 | 211.2283 | | | |
| Root MSE | | 0.27034 | R-Square | 0.23139 | |
| Dependent Mean | | 4.54814 | Adj R-Sq | 0.22981 | |
| Coeff Var | | 5.94387 | | | |

Parameter Estimates

| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
|------------|----|--------------------|----------------|---------|---------|
| Intercept | 1 | 3.479323 | 0.152962 | 22.75 | <.0001 |
| yrsschool | 1 | 0.071544 | 0.012820 | 5.58 | <.0001 |
| woman | 1 | -0.16103 | 0.013040 | -12.35 | <.0001 |
| experience | 1 | 0.023863 | 0.002187 | 10.91 | <.0001 |
| expsquared | 1 | -0.00034 | 0.000053 | -6.48 | <.0001 |

PRINTOUT PAGE 3.

PART (E)**Two-Stage Least Squares Estimation**

Dependent Variable: lnwage

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|------|----------------|-------------|---------|--------|
| Model | 5 | 72.50819 | 14.50164 | 202.91 | <.0001 |
| Error | 1941 | 138.72010 | 0.07147 | | |
| Corrected Total | 1946 | 211.22829 | | | |
| Root MSE | | 0.26734 | R-Square | 0.3433 | |
| Dependent Mean | | 4.54814 | Adj R-Sq | 0.3416 | |
| Coeff Var | | 5.87792 | | | |

Parameter Estimates

| Variable | Label | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
|-------------------|-----------|----|--------------------|----------------|---------|---------|
| Intercept | Intercept | 1 | 3.47932 | 0.15127 | 23.00 | <.0001 |
| yrsschool | | 1 | 0.07154 | 0.01268 | 5.64 | <.0001 |
| woman | | 1 | -0.16103 | 0.01290 | -12.49 | <.0001 |
| experience | | 1 | 0.02386 | 0.00216 | 11.03 | <.0001 |
| expsquared | | 1 | -0.00034400 | 0.00005252 | -6.55 | <.0001 |
| residualyrsschool | Residual | 1 | -0.01767 | 0.01295 | -1.36 | 0.1726 |