

Seminar IV

*Problem 1.*

This problem is a continuation of Problem 1 in Seminar III.

Paul finds out that the liquidity problem raised by the prospects of a cost over-run could be mitigated if there would be a way to secure short-term returns from the project, which could be used to cover in part the cost over-run. In particular, he could sell part of the property before completion of the project, providing verifiable short-term returns  $rI$ , where again  $I$  is the initial investment, and the distribution of  $r$  is subject to a second moral-hazard problem, in addition to the one affecting the success probability of the completed project: If Paul works hard on getting high short-term returns, he would suffer a loss  $B_0I$  and  $r$  would be distributed according to the probability distribution  $G(r)$ , with density  $g(r)$ . If not, then  $r$  is distributed according to the probability distribution  $\tilde{G}(r)$ , with density  $\tilde{g}(r)$ . Assume that the likelihood ratio,  $l(r) = [g(r) - \tilde{g}(r)] / g(r)$ , is (weakly) increasing in  $r$ . Define a contract as a pair of functions  $\{\rho^*(r), \Delta(r)\}$ , where  $\rho^*(r)$  is the cutoff reinvestment need when short-term returns are  $r$ , such that the project is abandoned if  $\rho > \rho^*(r)$ , and  $\Delta(r)$  is Paul's per-unit-of-investment extra rent, for each realization of  $r$ , over and above what is required by the other moral-hazard problem if the project is completed, and a per-unit-of-investment cash compensation if it is abandoned.

- i. Explain the meaning of  $l'(r) \geq 0$ . Also, explain why we need the restriction  $\Delta(r) \geq 0$ .
- ii. Explain why the equilibrium contract has the property that  $\rho^*(r)$  is (weakly) increasing in  $r$ , and discuss features of the project that determine whether the variation in the cutoff  $\rho^*$ , as the level of short-term return  $r$  varies, is large or small.

- iii. In cases where  $r$  is low, the cutoff  $\rho^*$  may be so low that a credibility problem arises, leading to a scope for renegotiation of the initial contract. This is called the problem of the *soft budget constraint*. Explain the nature of the problem and discuss how the contract needs to be amended in order to cope with it.

*Problem 2.*

Review Problem 4 in Tirole, pp. 627-628.