



UiO : **Fysisk institutt**

Det matematisk-naturvitenskapelige fakultet

Lecture 13



This week

- **Wednesday:** Relativistic four-vectors and the Lorentz transformations, general four-vectors. (Sections 6.1-6.4)
- **Thursday:** Problem set 6, mostly with relativistic physics. Also mid-term exam question from 2014.
- **Friday:** Cancelled (NFK).

Recap

- A body of length L_0 at rest in RF S' moving with velocity v w.r.t. RF S has length L in S given by

$$L = \frac{1}{\gamma} L_0 \leq L_0$$

A time interval τ in S' is the interval t in S

$$t = \gamma \tau \geq \tau$$

This is **length contraction** and **time dilation**.

- The **proper time** is given as

$$\tau_{AB} \equiv \int_{t_A}^{t_B} \sqrt{1 - \frac{v^2(t)}{c^2}} dt$$

Today

- Return of the four-vectors
 - We repeat Einstein's summation convention.
 - The metric tensor.
 - Lower indices (finally).
 - The general four-vector. (Not necessarily space-time x^μ .)
- Lorentz transformations strike again
 - Now properly using four-vectors and the metric.

Summary

- We define the metric tensor g and inverse g^{-1} as

$$g = g^{-1} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$$

- This is used to raise and lower indices

$$A^\mu = g^{\mu\nu} A_\nu, \quad A_\mu = g_{\mu\nu} A^\nu$$

- Lorentz transformations are given by

$$A'^\mu = L^\mu_\nu A^\nu, \quad A'_\mu = L_\mu^\nu A_\nu$$

where L fulfils $g_{\mu\nu} L^\mu_\rho L^\nu_\sigma = g_{\rho\sigma}$