

Tsunamier

Mekanismer og vitenskapelige utfordringer.

Pedersen G.

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Outline

- 1 Introduction
- 2 Models, computations
- 3 Tsunami properties
- 4 Earthquake tsunamis
- 5 Slide generated tsunamis



List of Topics

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Definisjon av tsunami

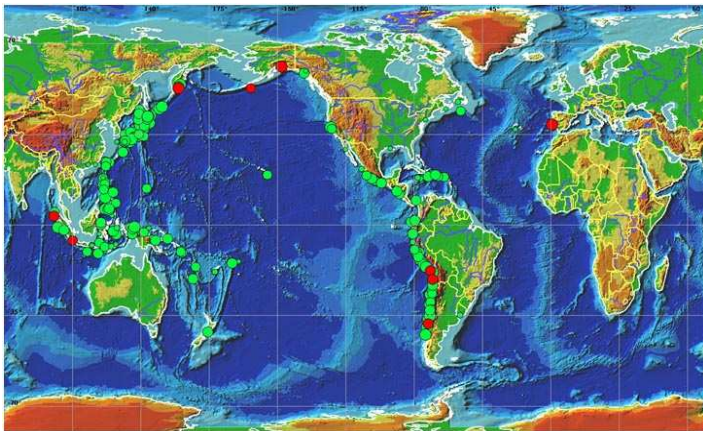
Ordet **Tsunami** er fra japansk: **bølge havn**

Definisjon

Tyngdedrevet overflatebølge på havet, skapt av en brå geologisk hendelse

- 1 Jordskjelv
- 2 Skred. Undersjøiske eller ned i innsjøer/hav ("Mass gravity flows")
- 3 Vulkaner
- 4 Asteroider/kometer
- 5 Kjernefysiske eksplosjoner – jada, det er undersøkt det også

Tsunami laboratory, Novosibirsk: Historiske tsunamier



Grønt 223 kjente tilfeller med dødsfall av totalt 2250

Rødt transoceaniske tsunamier

Mer statistikk, Novosibirsk (H_{max} = oppskylling)

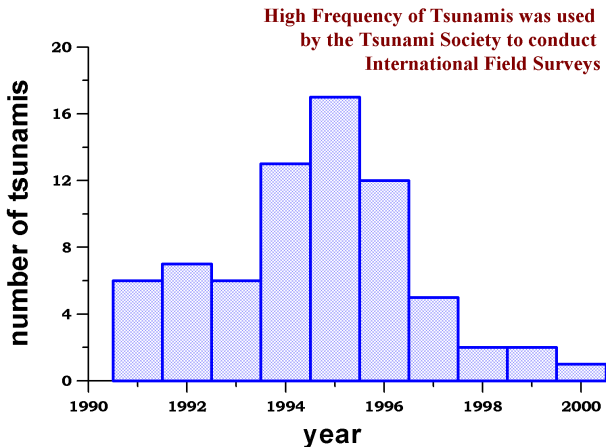
Tsunami occurrence in XX century

	World	Pacific
All tsunamis	911	704
(events per year)	9.1	7.0
Tsunamis with $H_{max} > 1$ M	252	213
(events per year)	2.5	2.1
Tsunamis with $H_{max} > 5$ M	96	82
(events per year)	1.0	0.8

Tsunamis with heights more than **5 M** at distance more than **5000 km** (so called **trans-oceanic** tsunamis) were observed **only in 5 cases** (all in the Pacific)

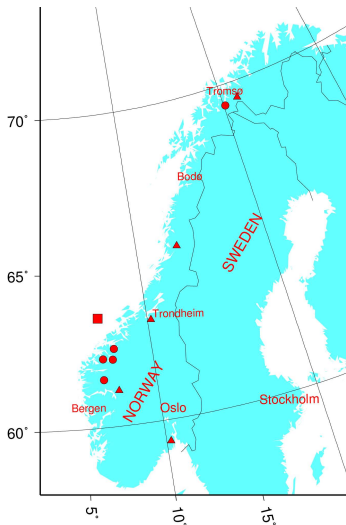
- 1946 Aleutians
- 1952 Kamchatka
- 1957 Aleutians
- 1960 Chile
- 1964 Alaska

Økt tsunamiaktivitet på 90-tallet



Mange tsunamier 1990-2000 \Rightarrow stor forskningsaktivitet
Enkelte utropte det til “tsunamidekaden”.

Norske tsunamier



● Mer enn 10 døde

■ Storeggaskred
(6.200 fKr.)

▲ Mindre hendelser
(utvalg)

Norsk tsunamiforskning

- UiO
 - Periodevis aktivitet 1980 →; forsøk, teori og modellering
 - 1992 →; økt aktivitet gjennom internasjonale og nasjonale prosjekter
- Beslektede tema: skred; Vedvarende stor aktivitet hos NGI, NGU, UiO etc.
- Rundt år 2000: Utbygging av Ormen lange
 - bred undersøkelse av Storeggaskred og tsunami
- 2002: ICG (International Centre for Geohazards)
 - Samarbeid NGI, UiO, NORSAR, NGU, NTNU
 - Tsunamier er ett av flere satsningsområder

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- 2 Models, computations**
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Tsunamis

Geological source

Earthquakes, slides,
asteroids, volcanoes.
Models are challenging

Tsunami generation

Slide/wave dynamics is complex.
Earthquakes are simpler.

Tsunami propagation

Large propagation distances.
Dispersion often important.
Huge grids.

Coastal impact

Difficult physics.
High resolution models.

The Navier-Stokes (*NS*) equation

The primitive equations:

$$\frac{D\vec{v}}{Dt} \equiv \frac{\partial\vec{v}}{\partial t} + \vec{v} \cdot \nabla\vec{v} = -\frac{1}{\rho}\nabla p + \mathcal{D} - g\vec{k}$$

$$\nabla \cdot \vec{v} = 0$$

where \vec{v} = velocity, D/Dt = material derivative, p = pressure and \mathcal{D} is viscous/turbulent term. In words:

acceleration = - pressure gradient + friction + gravity

net outflux from any fluid volume = 0

Boundary conditions: impermeable, no-slip, free (surface), artificial

Key problems: turbulence model, free surface tracking, underresolved boundary layers, etc.

Applicability of primitive models

- Robust free surface techniques (VOF, SPH)
- Industrial solvers (CFX, Fluent...)
- Analytic solutions are sparse, circumstantial and cumbersome
- Computations readily become very heavy \Rightarrow numerical solutions are under-resolved or unattainable \Rightarrow feasible only in local and idealized studies
- The burden of the computations often lead to wavering of the physics

Surprisingly (?) little insight in hydrodynamic wave theory yet stem from “full computational models”.

Simplified theories are crucial, but general models become increasingly important

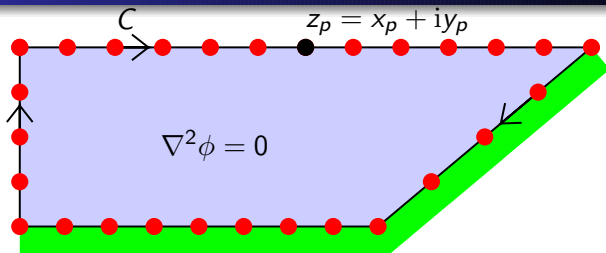
Full potential theory

No viscosity, no rotation \Rightarrow all velocity components can be derived from a scalar potential ϕ ($\nabla\phi \equiv \vec{v}$) that fulfills Laplace equation

$$\nabla^2\phi = 0$$

- Simpler than the Navier-Stokes system
- At a given time the velocity distribution in the fluid is given by one component at the boundary \Rightarrow boundary integral equations
- Not incorporable: viscous effects, bottom and surface drag, turbulence, overturning waves, Corioli's force ...
- Water waves are often well described by potential theory

Integral equation; example: Cauchy's formula



$$\alpha i q(z_p) = \text{PV} \oint_C \frac{q(z)}{z_p - z} dz$$

where $q = u - iw$ ("complex velocity") or $q = \phi + i\psi$ (complex potential), $\alpha =$ interior angle.

Interpolation between nodes, and one velocity comp. known \Rightarrow implicit equation in boundary value only.

Potential flow models

- 1 Integral equation discretized by panels. Boundary location updated in time as part of the method.
- 2 FFT techniques; approximations at free surface

Computation still heavy. Useful for local simulations and for assessing validity of simpler models. Cannot incorporate wave breaking and rotational effects. **More efficient and robust models must be employed for large scale tsunami modeling**

Scales for surface gravity waves

Acceleration scale

g acceleration of gravity

Remark: scale for particle acceleration in gravity waves is always the same, regardless of size of problem

Length scales

λ wavelength

h depth

A amplitude (height)

L_h depth variations

L_λ variation of λ

Often $L_h \sim L_\lambda$

Velocity and time scales

May be built from length and acceleration scales

Approximations

- $\frac{A}{h}, \frac{A}{\lambda} \ll 1 \Rightarrow$ linear and weakly non-linear theories
- $\frac{\lambda}{h} \ll 1 \Rightarrow$ deep water
- $\frac{h}{\lambda} \ll 1 \Rightarrow$ **shallow water; long wave theory**
- $\frac{h}{L_h}, \frac{\lambda}{L_\lambda} \ll 1 \Rightarrow$ multiple scale methods: ray theory; narrow band (nearly uniform waves)

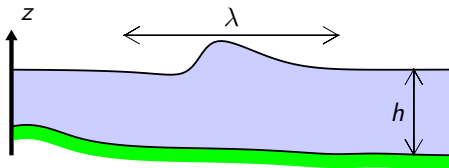
Different requirements may be combined; long wave theory is often combined with weak non-linearity.

Definition of characteristic scales may be vague or ambiguous

Tsunami and ocean modeling

Tools of the trade

- Depth integrated models for long waves
- Efficient and robust numerical techniques
- Ray tracing, wave kinematics



Long waves $\lambda/h \gg 1$

U , W – characteristic horizontal and vertical velocities

$$\frac{\partial u}{\partial x} + \frac{\partial w}{\partial z} = 0 \Rightarrow \frac{W}{h} \sim \frac{U}{\lambda} \Rightarrow \frac{W}{U} \sim \frac{h}{\lambda} \ll 1$$

\Rightarrow vertical motion is small

Depth integrated theory; shallow water

Vertical acceleration neglected \Rightarrow hydrostatic pressure \Rightarrow no vertical variation in horizontal velocity

Shallow water eq. ($\lambda/h > 20$)

$$\frac{\partial \bar{\mathbf{v}}_h}{\partial t} + \bar{\mathbf{v}}_h \cdot \nabla_h \bar{\mathbf{v}}_h = -g \nabla_h \eta$$

$$\frac{\partial \eta}{\partial t} = -\nabla_h \cdot ((h + \eta) \bar{\mathbf{v}}_h)$$

η : surface elevation, $\bar{\mathbf{v}}_h$: velocity (horizontal), ∇_h : horizontal gradient operator

Efficient and simple numerical solution; hyperbolic equations
May include bores, Coriolis effects and bottom drag, *but wave dispersion is lost.*

Use: propagation of tsunamis, inundation. The dominant tsunami model (MOST at PTWS/NOAA, TUNAMI, COMCOT, CLAWPACK)

Depth integrated theory; Boussinesq

Vertical acceleration small, but not neglected

$(\lambda/h > 2)$

$$\frac{\partial \bar{\mathbf{v}}_h}{\partial t} + \bar{\mathbf{v}}_h \cdot \nabla_h \bar{\mathbf{v}}_h = -g \nabla_h \eta + \frac{1}{2} h \nabla_h \nabla_h \cdot (h \frac{\partial \bar{\mathbf{v}}_h}{\partial t}) - \frac{1}{6} h^2 \nabla_h \nabla_h \cdot \frac{\partial \bar{\mathbf{v}}_h}{\partial t} - \kappa h^2 (\nabla_h^3 \eta + \nabla_h \nabla_h \cdot \frac{\partial \bar{\mathbf{v}}_h}{\partial t})$$

$$\frac{\partial \eta}{\partial t} = -\nabla_h \cdot ((h + \eta) \bar{\mathbf{v}}_h)$$

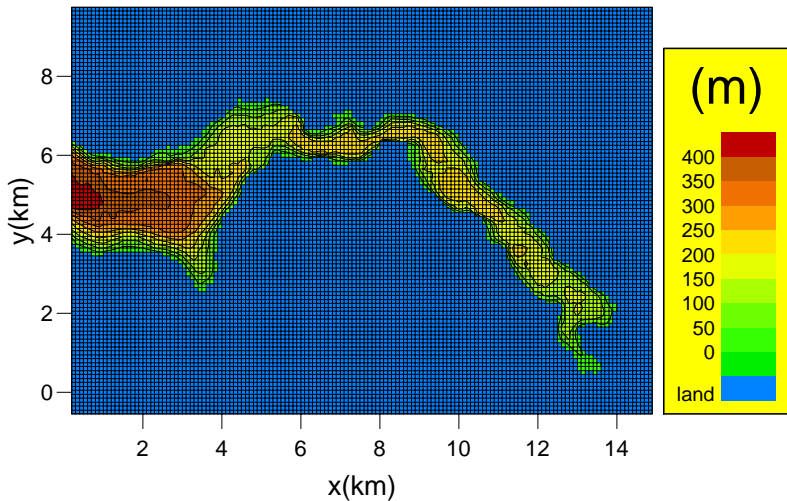
Numerical solution much heavier than for shallow water eq. – implicit solution strategy needed. Still, much faster to solve than primitive equations. Wave dispersion included.

Use: propagation of moderately short tsunamis, particularly from non-earthquake sources. Boussinesq propagation models should always be considered for global propagation.

What is gained by long wave theory

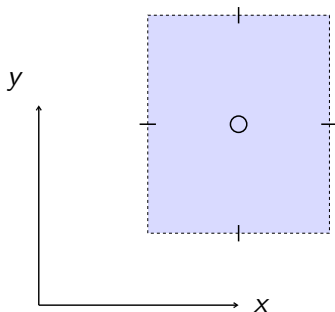
- 1 The number of dimensions reduced by 1 (depth integration)
- 2 Upper and lower bound of fluid replaced by coefficients PDEs in the horizontal coordinates
- 3 Shallow water equations are hyperbolic with characteristics and shocks \Rightarrow simple models of wave breaking and surf may be included
- 4 Physical contents more transparent; analytic solutions

First two points important for numerics

Finite Differences *FDM*

Finite size grid cells. Generally: staircase boundaries.

Kontrollvolum i FDM



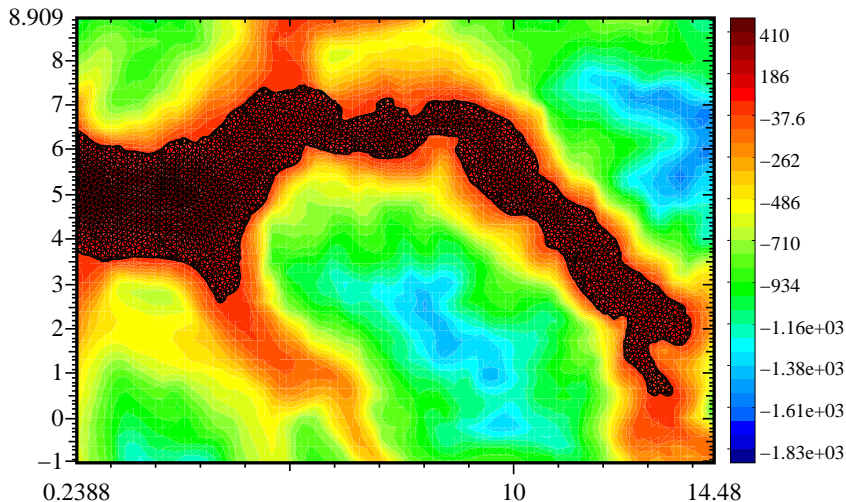
○ overflate

— strøm

| strøm

Skritt for skritt fram i tid:

- 1 Summerer strøm inn og ut \Rightarrow ny overflate
 - 2 Forskjeller mellom overflater i nabobokser \Rightarrow trykkforskjeller
 \Rightarrow akselerasjoner \Rightarrow nye strømhastigheter
- Tillegg: adveksjon av bevegelsesmengde

Finite Elements *FEM*

Simple representation of unknowns in each element, less common than FDM

mathematical challenges

- 1 Large domains, costal resolution down to meters \Rightarrow millions and millions of grid points
Parallel, local refinement, coupling of models
- 2 Many details (breaking, friction, interaction with structures) require full models – impossible
Must be incorporated in approximate models
- 3 Inundation on land \Rightarrow moving computational boundaries
- 4 Sources are difficult
- 5 High efficiency desirable; Use in tsunami warning leaves only minutes for computation
- 6 Increased complexity, real applications \Rightarrow new problems concerning instability and performance arise

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Tsunamien blant andre bølger

Sammenlikning (h =havdyp, T =periode)

type	hastighet	mekanisme
lys/radio...	300000 km/s	elektromagnetisme
lyd(luft)	340m/s=1200km/t	trykk/kompresjon
lyd(vann)	1500m/s	trykk/kompresjon
seismiske	2-7000m/s	Spenning/deform.
tsunami ($h = 5000$ m)	220m/s=800 km/t	Fri overflate/tyngde
dønning ($T = 20$ s)	31 m/s=110 km/t	Fri overflate/tyngde

Media: tsunamier er ufattelig raske bølger

Bølger er raske, tyngdebølger, som tsunamier, er blant de treigere
 ⇒ viktig for varslings.

Tsunami blant havbølger

	Høyde maks. (m)	Bølge- lengde	Periode
Vindsjø	25	0.1-500 m	0.1-20 s
Dønning	8	0.1- 1 km	13-30 s
Flodbølger	30/500 ¹	1-100 km	1-30 min
Stormflo	5	50-200 mil	6-12 timer
Tidevann	15	100-1000 mil	12-24 timer

Bølge lang i forhold til dyp: (nesten) uniform bevegelse til bunnen, fart avhenger av dyp

Bølge kort i forhold til dyp: mest bevegelse nær overflaten, fart avhenger av bølgelengde

¹: maks oppskylling av jordskjelv/skred tsunami

Tsunami i variabelt dyp

Enkle betraktninger av perioder og energi \Rightarrow

dyp	høyde	lengde	bølgehast	strøm
4000m	1.0m	100km	713km/t	0.18km/t
1000m	1.4m	50km	356km/t	0.5km/t
250m	2.0m	25km	180km/t	1.4km/t
100m	2.5m	16km	113km/t	2.8km/t
50m	3.0m	11km	80km/t	4.8km/t
20m	3.8m	7km	50km/t	9.4km/t
10m	4.4m	5km	36km/t	26.8km/t

Tsunami kontra dønning

Dersom lik amplitude i dyphav: samme energitetthet

Tsunami: større energitransport, starter vekst på dypere vann

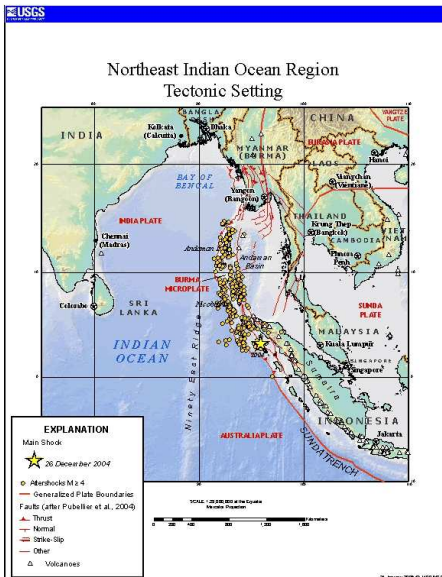
Bryting ved strand: dønningen (kort) spises opp, tsunami (lang) er mindre påvirket

Tsunami skyller mye lengre inn

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The 2004 earthquake (fra USGS)



Magnitude:
9.0-9.3

Marine earthquakes

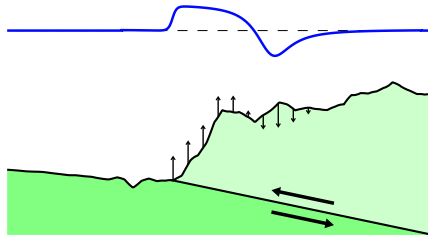


Illustration based on the Dec. 26'th 2004 event

- Sequake: compression waves in water; do not penetrate shallow waters
- Lasting vertical uplift of sea bed \Rightarrow tsunamis
- Generally: Earthquake fast; gravity waves slow \Rightarrow tsunamis can be modelled from initial sea surface elevation at rest

Computation of sea-bed uplift

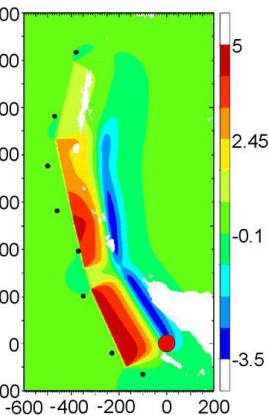
Okadas formula

Uplift \sim m, depth \sim km \Rightarrow tsunami generation is a linear process.

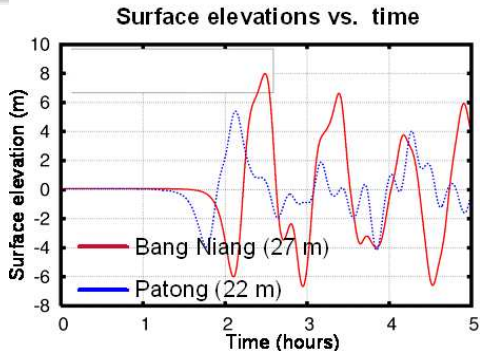
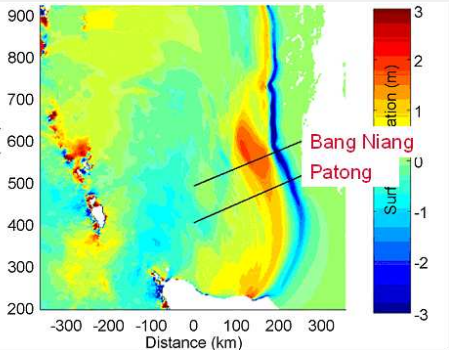
Okadas formula: Green function for crust surface deformation from straight fault between semi-infinite elastic plates.

Input: fault length, depth, slip, strike and dip components etc.

In true applications sub-faults may be combined.
Example to the left: representation of the 26th December event (NORSAR/NGI/ICG)



2004 simulation



- Wide source \Rightarrow shallow water theory
- Against Thailand: leading depression (other direction leading elevation)
- Source length \gg source width \Rightarrow strong directionality

Animations

- 2D animation of tsunami from a an earthquake with large dip angle (50° as compared to $12 - 14^\circ$ for the 2004 event)
- Japanese animation of simulation of the 1960 Chile tsunami Magnitude 9.5 makes this the strongest earthquake recorded

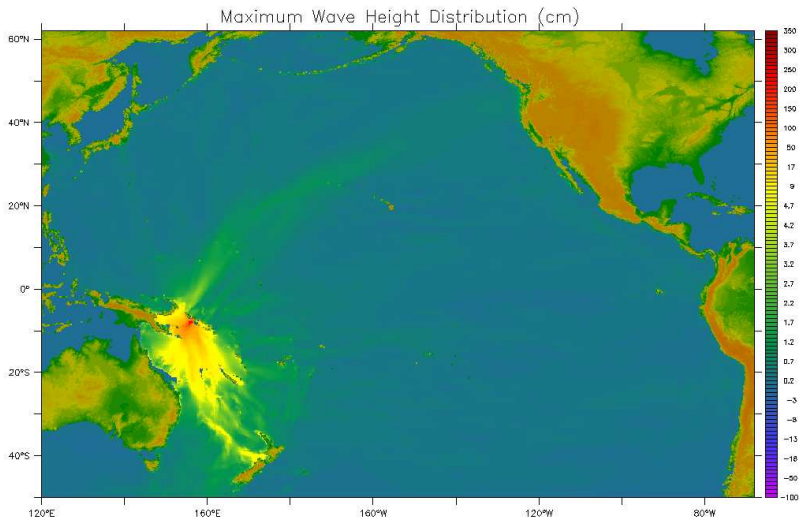
Other examples

- 17th July, 1998, Papua New Guinea
 $M = 7.0$: weak earthquake, slide is to blame, 2.600 fatalities
- 27th March, 2005, Sumatra
 $M = 8.7$: strong!, local 4 m max. runup, no fatalities ?
- 17th July, 2006, South Java
 $M = 7.8$: slow earthquake, 20 m max. runup, 700 fatalities
- 13th Januray, 2007, Kuril Islands
 $M = 8.1$: Small waveheights
- 1th April, 2007, Solomon Islands
 $M = 8.1$: 52 fatalities

No strict relation magnitude \Rightarrow tsunami

Warning cannot be based on seismic information alone.

Solomon Islands, Max. amplitude (NOAA)



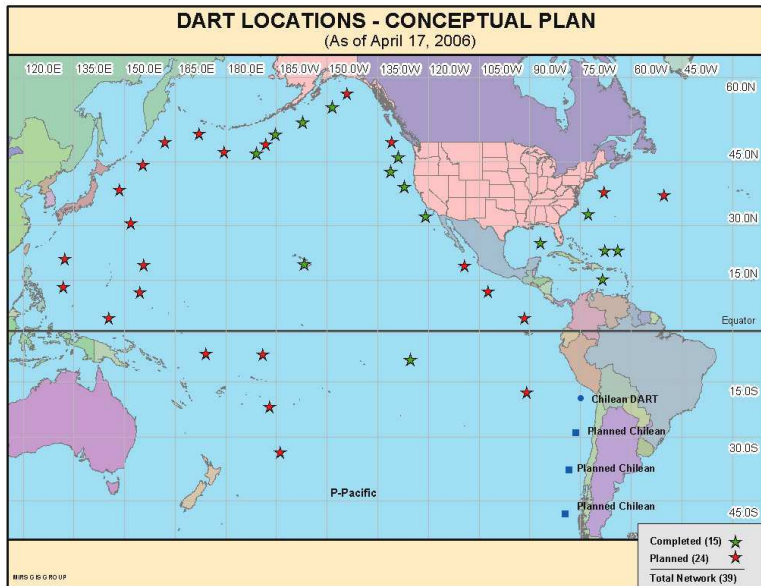
Java 2006, photo: C. Harbitz ICG/NGI



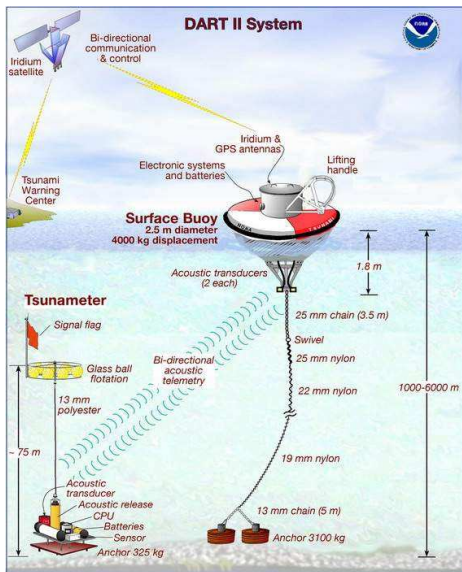
Java 2006 (C. Harbitz)



Warning system, (source NOAA/PMEL)



Dart buoys, (source NOAA/PMEL)



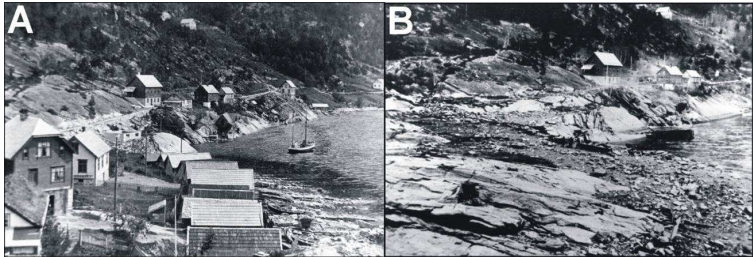
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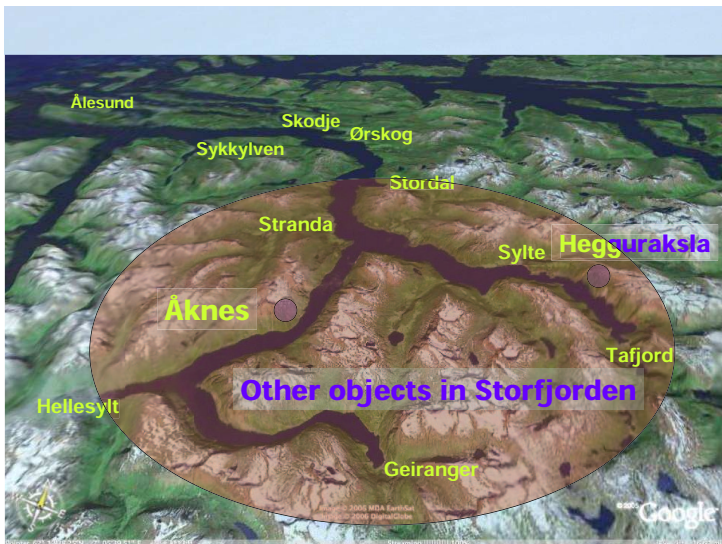
Tsunamis from rock-slides

Local events, but with very high wave amplitudes.
Occur in mountain basins and fjords

Example: village damaged by event in 1934, Tafjord, Norway



Monitored cite; Åkneset (L. Blikra)



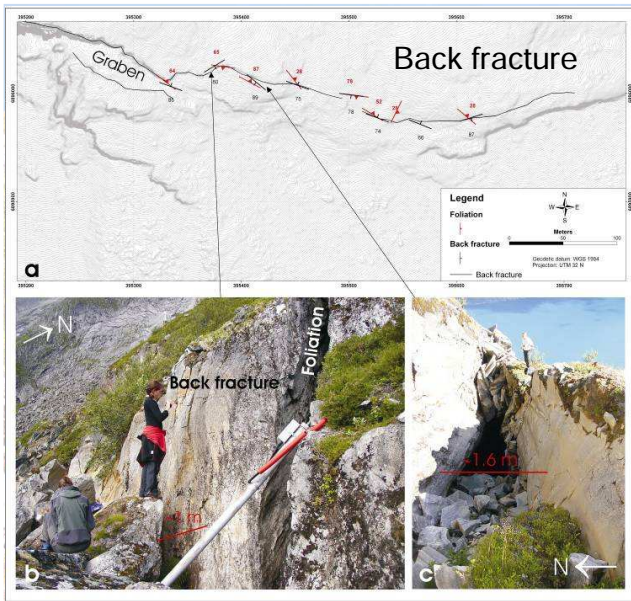


Figure:
Guri Venvik
Ganerød, NGU

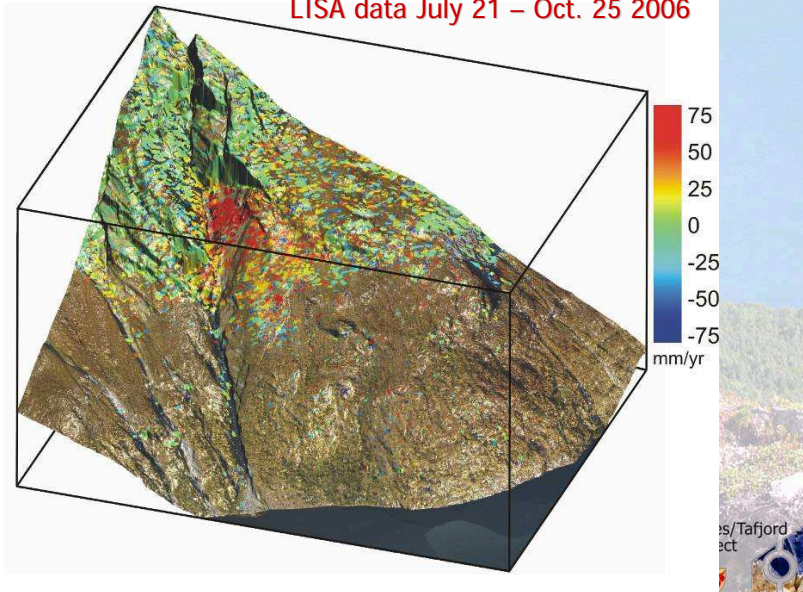
Åknes/Tafjord
project

Radar across the fjord (Blikra)

Movement pattern: LISA Radar



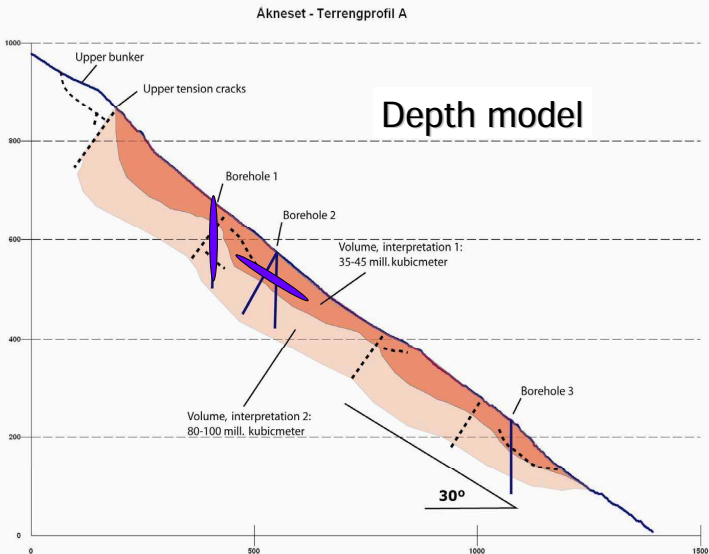
LISA data July 21 – Oct. 25 2006



Core samples with breccia (Blikra)

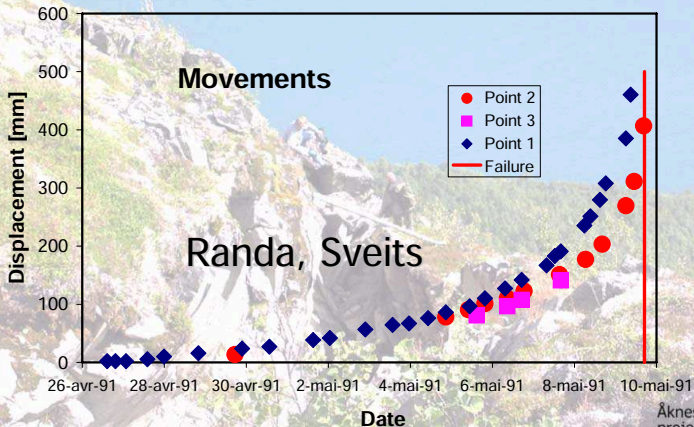


(Blikra)



Release of slide in Randa (Jogerud/Blikra)

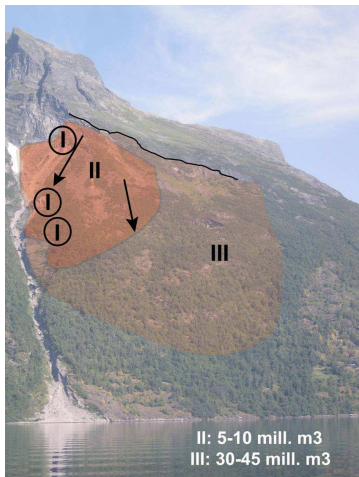
The early-warning is based on the fact that large rockslides gives many pre-failure signals



Åknes/Tafjord
project



Scenarios



- I: Small failures at margin
- II: 5-25 Mm³
- III: 30-80 Mm³

II and III \Rightarrow disaster

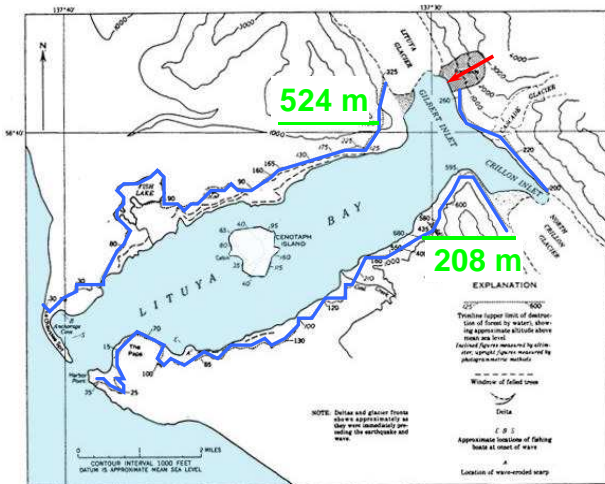
Tafjord 1934: 1.5–3 Mm³,
41 perished

The Åkersneset project

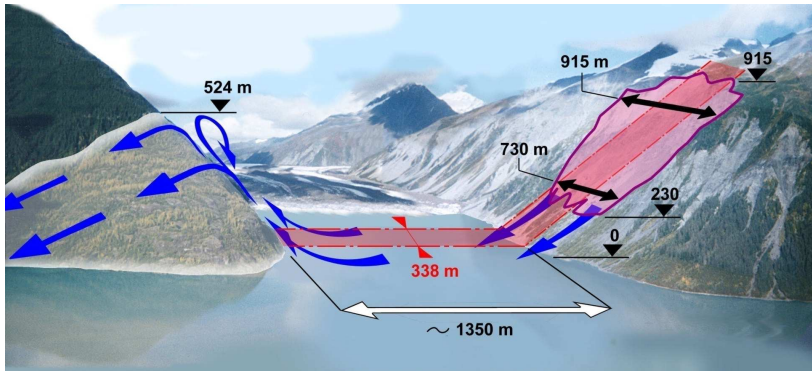


- Ongoing
- Geological surveillance
- 2D exp. Dep. Math. UiO
- 3D exp. at SINTEF
- Modeling, analysis

Lituya Bay, Alaska 1958; From H. Fritz

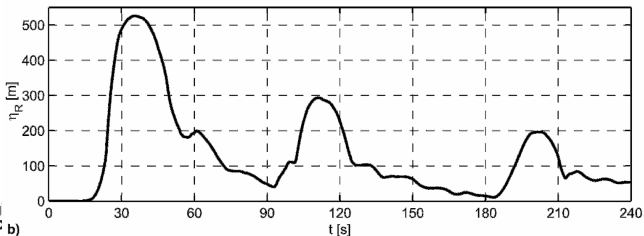
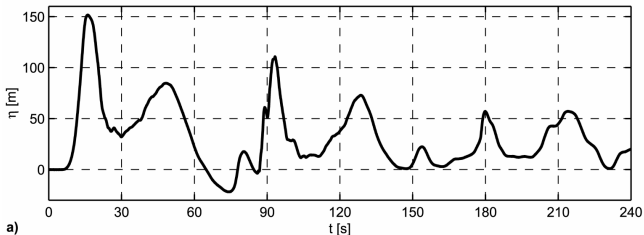


Lituya Bay impact and run-up site

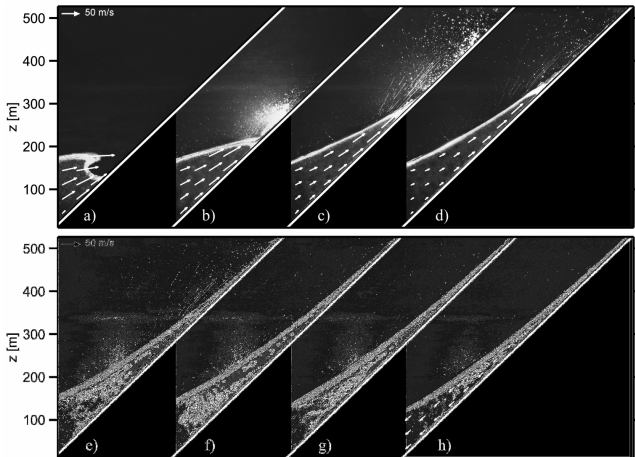


Omregnet til fullskala (H. Fritz)

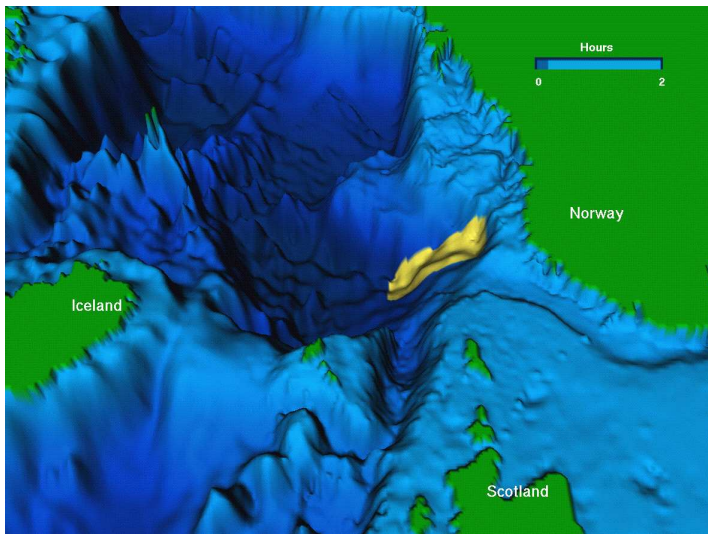
Wave and Run-up Gauge Records

Georg
Tec

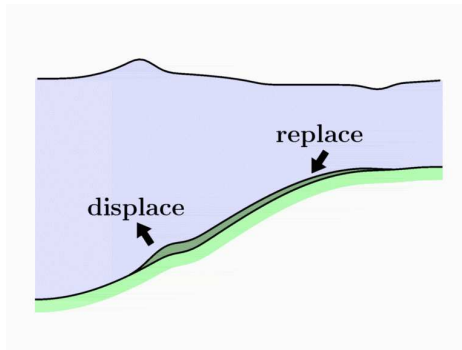
530m Tsunami Wave Run-up



The Storegga slide



Tsunamis from slide at continental margin



Simplest case: dense, progressive slide

Source at front sink in the rear of the slide body

Leading drawdown at adjacent coast

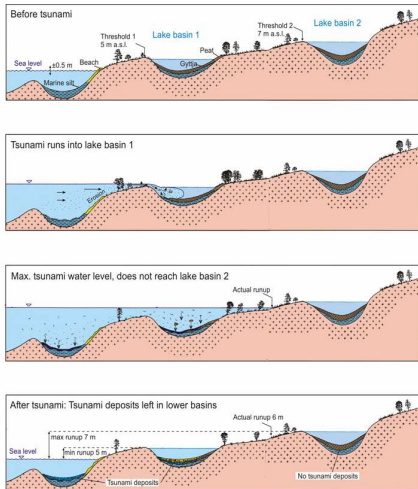
Important: Froude number = $(\text{speed of slide}) / (\text{local wave speed})$

Storegga tsunami



Numerical simulation. LSW
Volume= $2 \cdot 10^{12} \text{ m}^3$

Geological evidence of tsunami



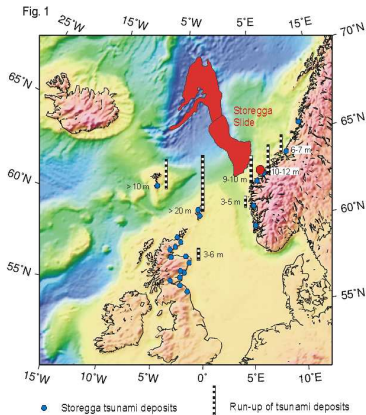
Land uplift \Rightarrow ponds detached from fjords

Tsunami intrusion easily detected in sweet-water sediments

Altitude of basins with tsunami traces \Rightarrow run-up height

From S. Bondevik

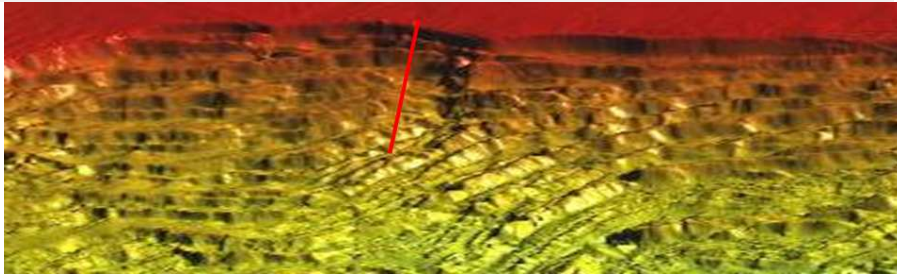
LSW model versus core samples.



cite	obs.	mod.
Gurskøy	9–13	17
Ålesund	10–12	13.5
Bjugn	6–8	7
Scotland	3–6	4

Bondevik et al. (2004)

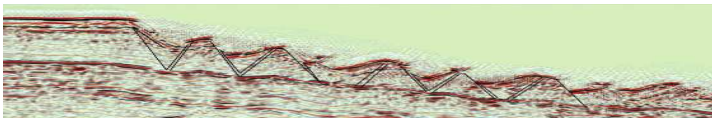
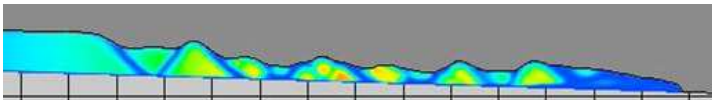
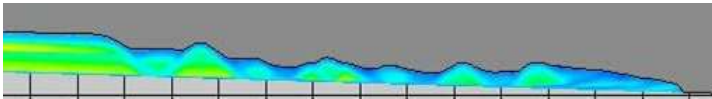
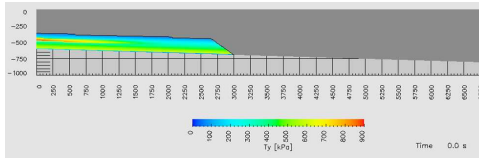
The real Storegga slide



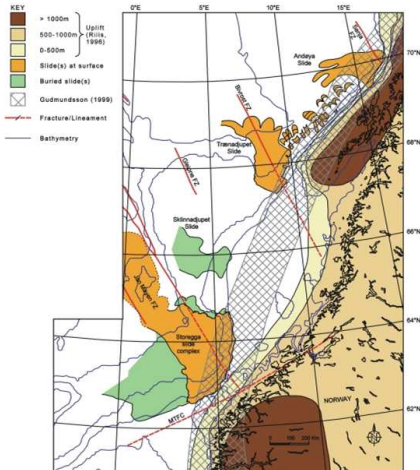
Model by Gauer et al.

- Two phase model; water and slide body
- Rheology in slide: Bingham fluid with a history dependent yield strength
- Slide released due to initial supercritical stress.
Real slide probably destabilized by earthquake

Retrogressive slide



Identified slides



Orange: surface slides

Green : buried slides (earlier glaciations)

Griding: high crustal stress due to land lift

Potential slides: North Sea Fan

(After Bugge)

The LaPalma case

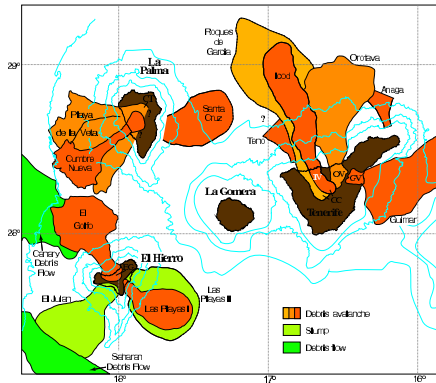
Potential mega-tsunami

- Large public interest and mass media attention
- Low probability event, but with potentially large consequences

La Cumbra Vieja volcano, La Palma island

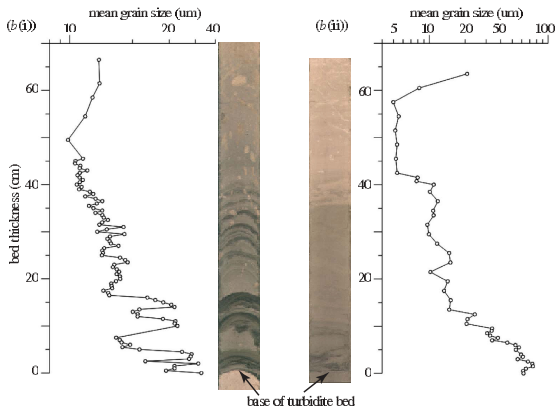
- Alarming investigation by Ward and Day (2001)
 - Surface elevations up to 30 m along the coast of America
 - Geological basis questioned by others (Wynn and Masson, 2003; Masson et al., 2006)
- Other authors report order of magnitude smaller waves (Mader, 2001; Gisler et al., 2006)

Canary Island landslides (from Masson et al. 2006)



- Many landslides, occurrence cycle $\sim 100\,000$ years
- Geological evidence of multistage development

Core sediment samples (from Masson et al. 2006)

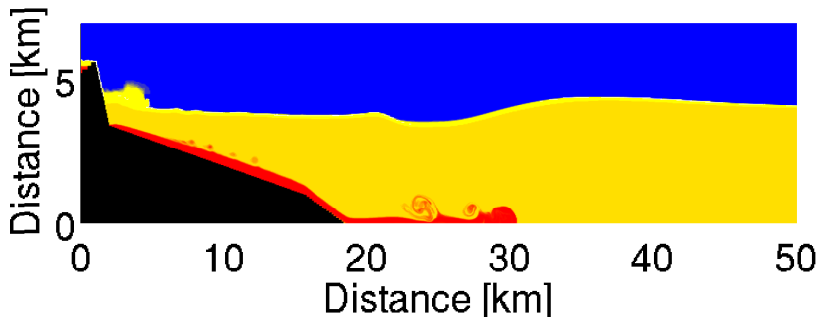


- Canaries (left), and Saharan landslides (right)
- Stack sequence of fining-upwards beds at the Canary Islands
- Debris avalanches, multi-stage development over hours or days

Wave generation

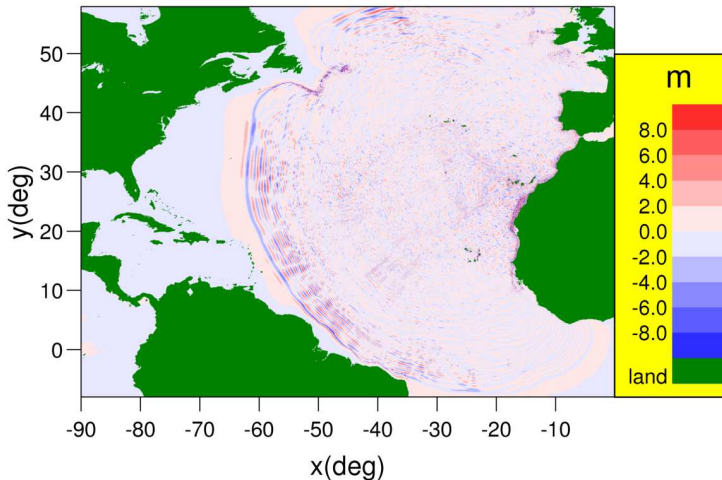
SAGE multi-material simulation

- Slide volume of 375 km^3 , modified from Ward and Day (2001)
- $u_{max,slide} \approx 150 \text{ m/s}$, almost critical slide motion
- Debris flow combined with turbidity currents

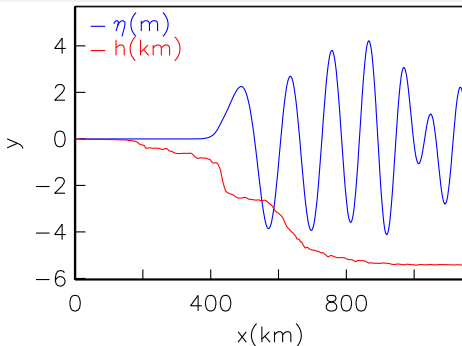


Atlantic propagation

Time: 5h 45.1min; grid: 2.0min



Example; E-W transect at 32° N (Georgia/South Carolina)



Series of incident waves

- Heights of several meters outside continental shelf
- Leading crest not largest (typical feature in present case)
- Typical lengths ~ 100 km and more
- **Reminiscent of waves from series of strong earthquakes**

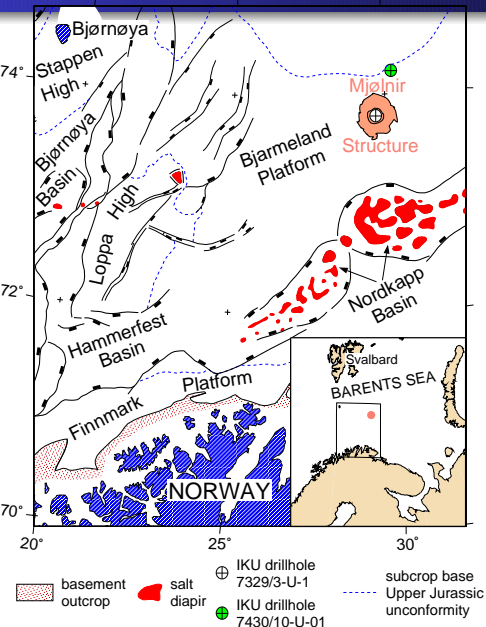
List of Topics

6 Impact generated tsunamis

Marine impacts

- 170 known impact craters, 34 are marine
- Most recent: 1 km impactor, Bellinghausen Sea (off southern Chile), 5000 m depth, 1.8 mill. years ago
Chemical and ejecta evident, but no crater. Simulations points to local amplitudes up to 1 km (Shuvalov; Gisler et al.)
- Most famous: The Chicxulub impact (Yucatan), 65 mill. years ago.
Marks the K/T boundary and held responsible for mass extinction of species
- Studied at UiO/SIMULA/ICG: the Mjølnir impact

Jurassic tsunami



LOCATION

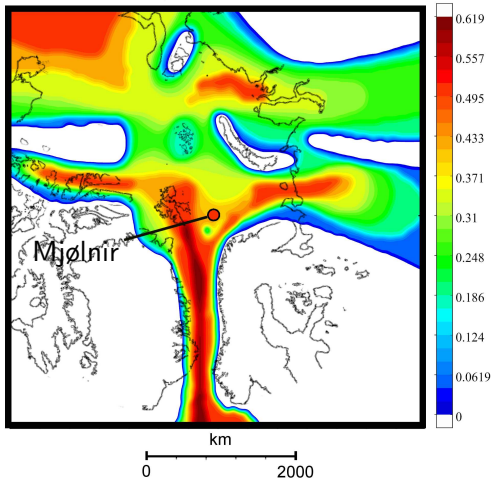
The Mjøltnir structure was first detected in seismic survey. (Gudlaugsson 1993)

Age: 142 million years. (Dated by fossils in sediment layers)

Paleo Barents Sea (142Myears ago)

Bathymetry, paleo-Arctic Seas

depth in kilometer



Reconstructed bathymetry

Gentle gradients.

Depths $h < 600$ m.

Desirable resolution:

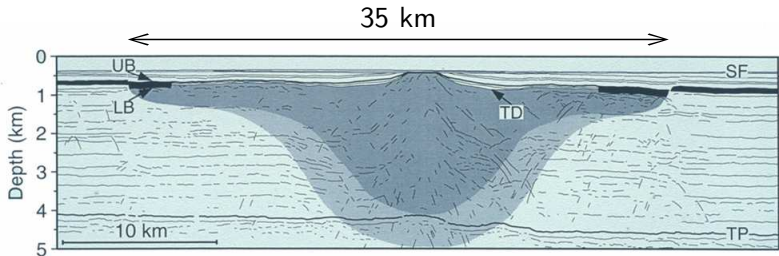
$\Delta x \sim 200$ m,

Domain size:

2000×2000 km²

$\Rightarrow 100$ Mpoints.

The Mjølner structure



Interpretations:

Thin lines: constant seismic velocity.

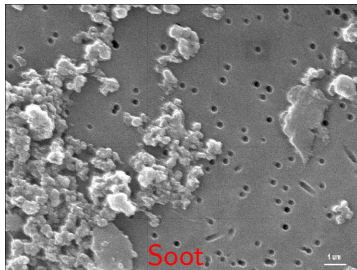
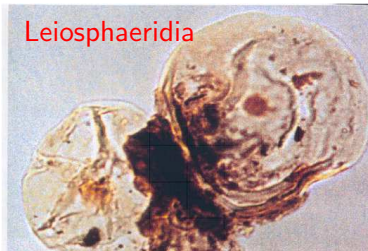
Shades: re-configured by impact.

Assumed characteristics:

Water depth: 400 m (time of impact).

Diameter of asteroid: 1.6 km.

Core samples



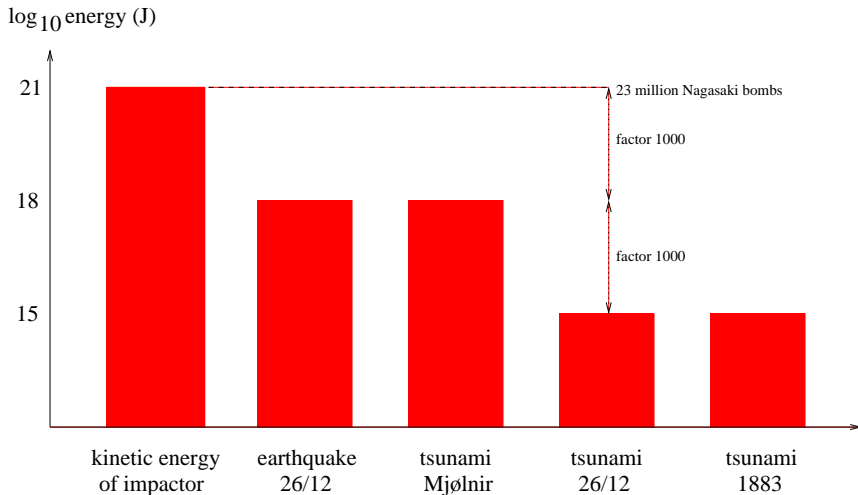
Also found

Breccia.

Iridium anomaly.

Enrichment in sulphides and
Ni, V, Cr above iridium layer.

Energy in impact



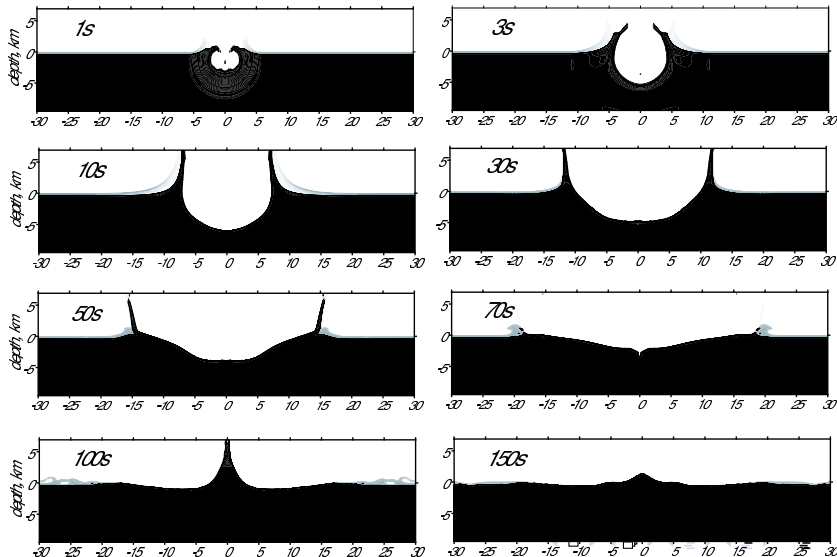
Asteroid

Radius: 800m density: 3kg/l speed: 25km/s

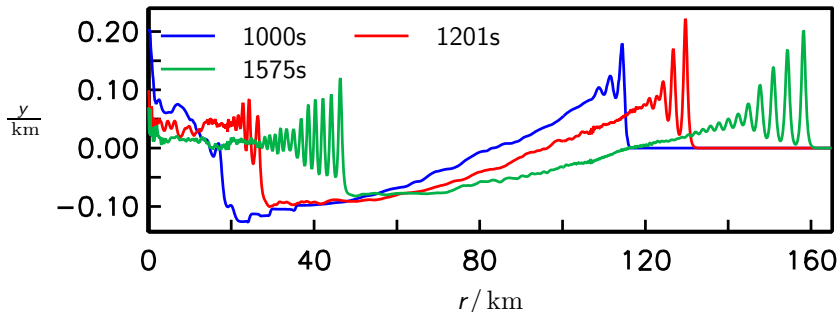
Models

- Impact: Multi-material code
 - Crust with Bingham model
 - Ocean, atmosphere and ejecta included
 - Run in 3D version for initial stages of impact
 - With radial symmetry: longer time, larger horizontal extent; still very coarse grids
- Tsunami propagation
 - Nonlinear dispersive long wave equations (Boussinesq)
 - Full potential theory
 - Ray theory for solitary waves

Impact simulation



Boussinesq solution ($t > 1000$ s)



Two undular bores (front wave and resurge), fission into solitary waves

Amplitude growth followed by decrease (radial spread).

Second bore close to breaking.

Wave heights ~ 200 m, fluid velocities ~ 100 km/h

Full potential models indicate 10% errors in Boussinesq solutions.

Environmental consequences

Regional consequences of distribution of vapor and dust in the atmosphere.

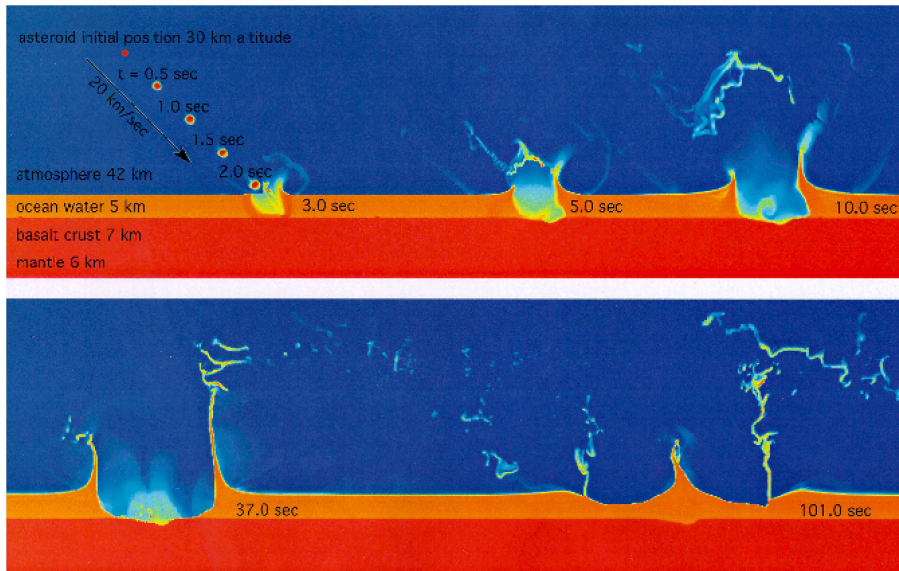
Run-up is not analyzed – must have been monstrous.

The tsunami caused series of current pulses; 30–70 km/h.

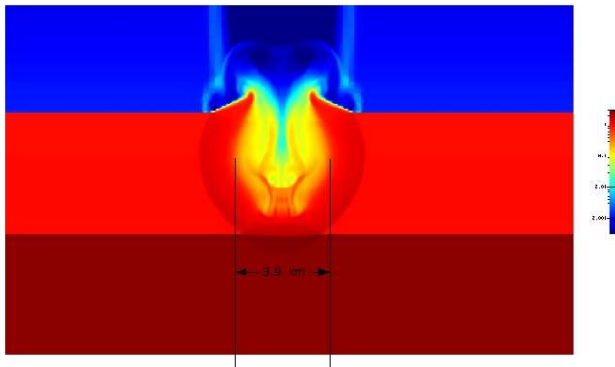
Sea floor was a thick succession of unconsolidated, organic rich clays.

Release of nutrients and toxins \Rightarrow changes in marine environment (bloom of Leiosphaeridia).

An oblique deep water impact



Normal impact, dunite (1 km, 20 km/s), at 0.57 s, in depth 5km



Asteroid has been completely decelerated and destroyed.

Density less than 1.0 is water vapor

The vaporization is due to shock wave and subsequent rarefaction