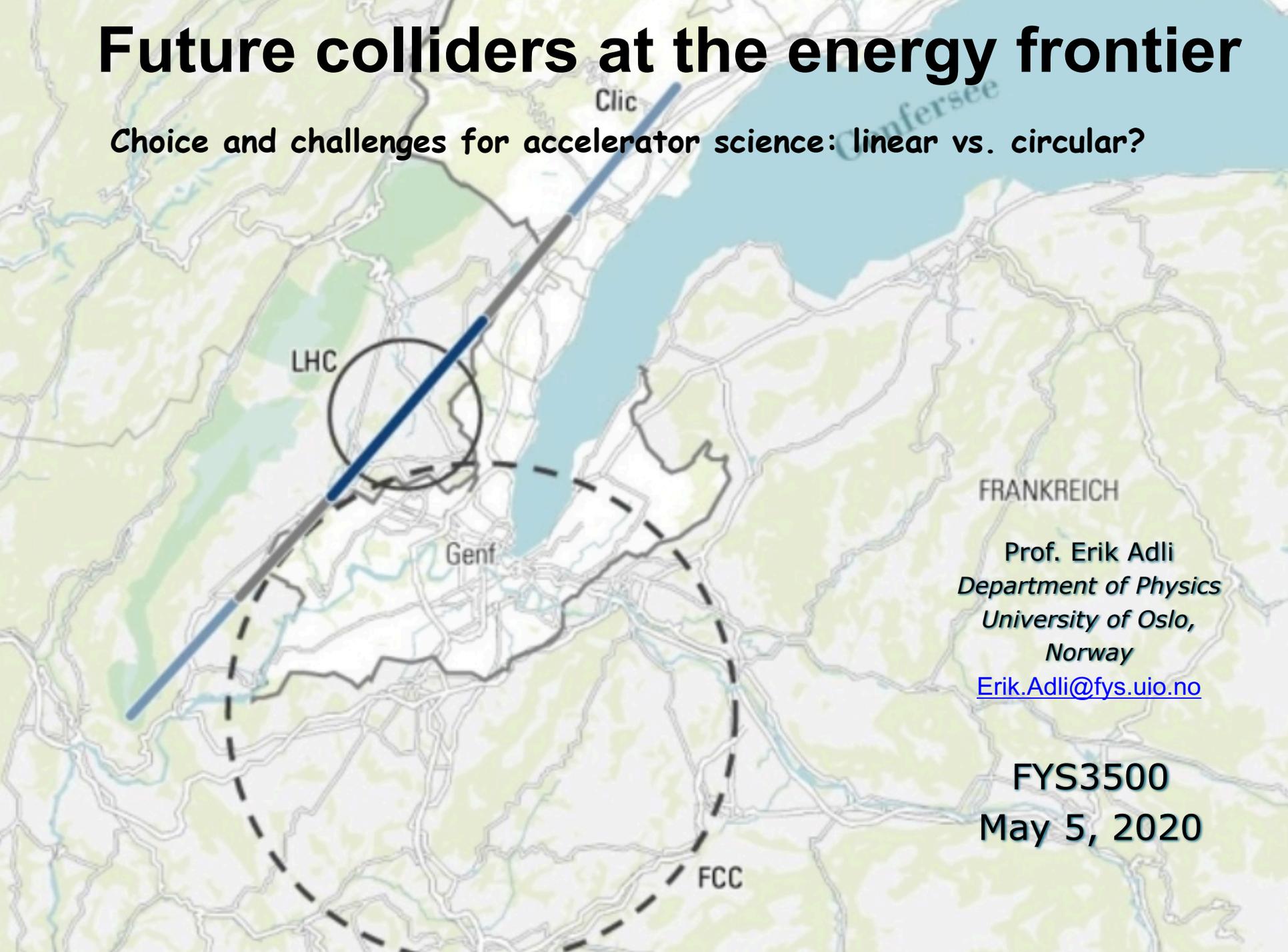


# Future colliders at the energy frontier

Choice and challenges for accelerator science: linear vs. circular?



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FYS3500  
May 5, 2020

# Particle acceleration: how many volt does your particle gain?

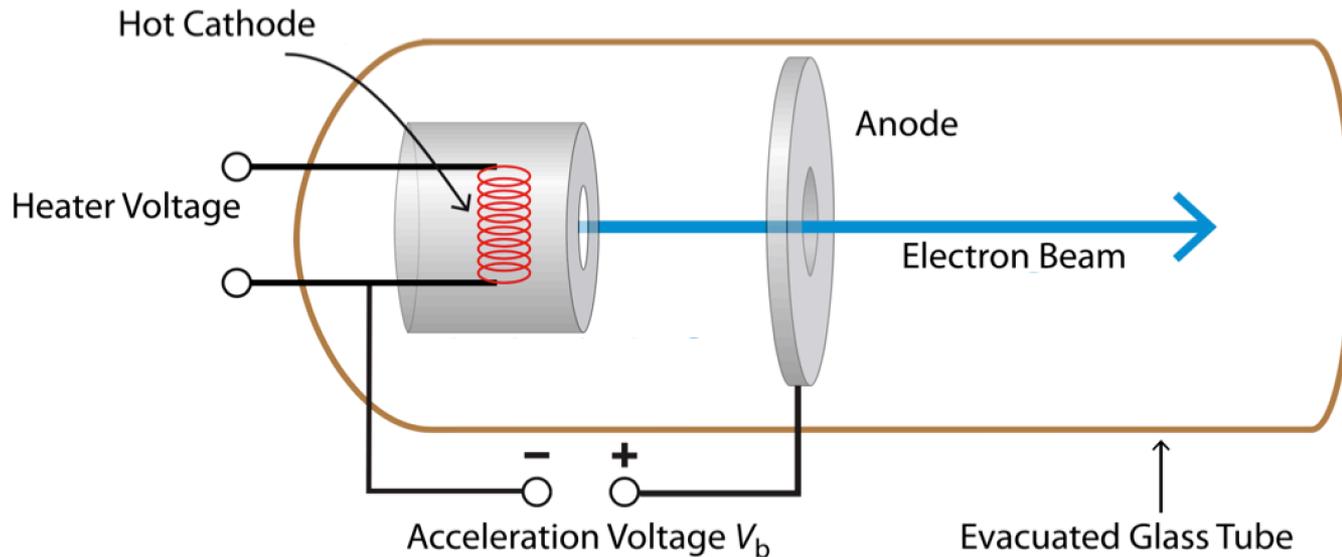
A particle accelerated by one volt has a kinetic energy of one electron volt (**eV**).

1000 eV = 1 **keV** (kiloelectronvolt)

1'000'000 eV = 1 **MeV** (Megaelectronvolt)

1'000'000'000 eV = 1 **GeV** (Gigaelectronvolt)

1'000'000'000'000 eV = 1 **TeV** (Teraelectronvolt)



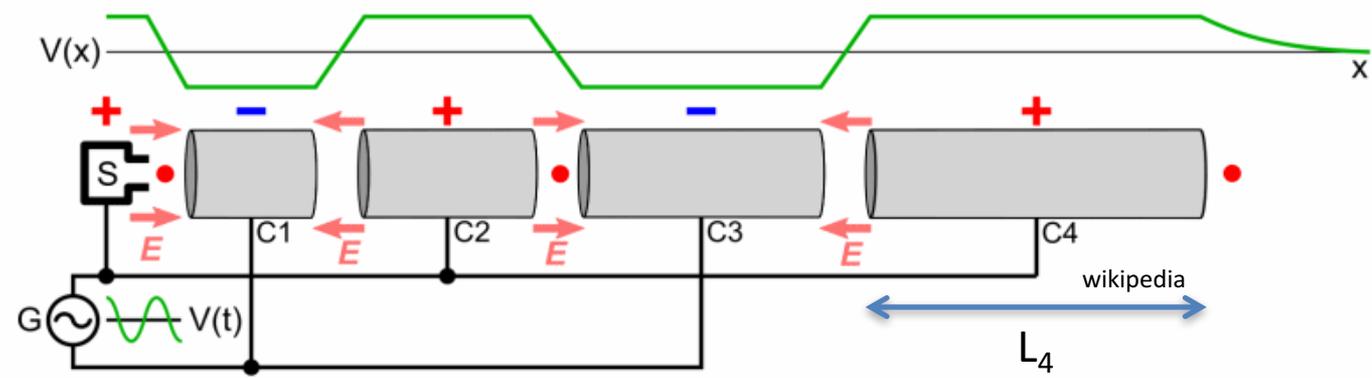
A simple way to make an electron accelerator: electrostatic acceleration with a cathode emitting electrons and an anode, at a higher potential, pulling the electrons towards it.

Voltage for **cathode ray televisions**: few 10 keV

# Radio-frequency linear accelerators

By using time-varying fields, oscillating at radiofrequency (RF), particles can in principle be accelerated to any energy, using a limited peak voltage.

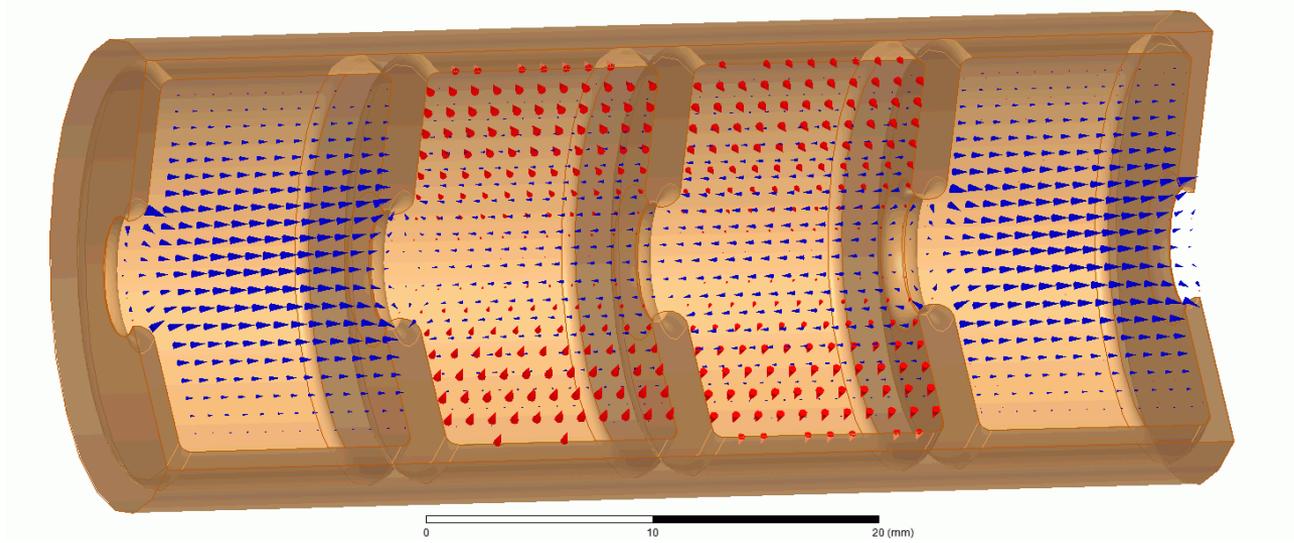
$$\frac{1}{2} T_{RF} v = L$$



Widerøe-type RF-linac.

RF-cavities is used in all high-energy particle accelerators today.

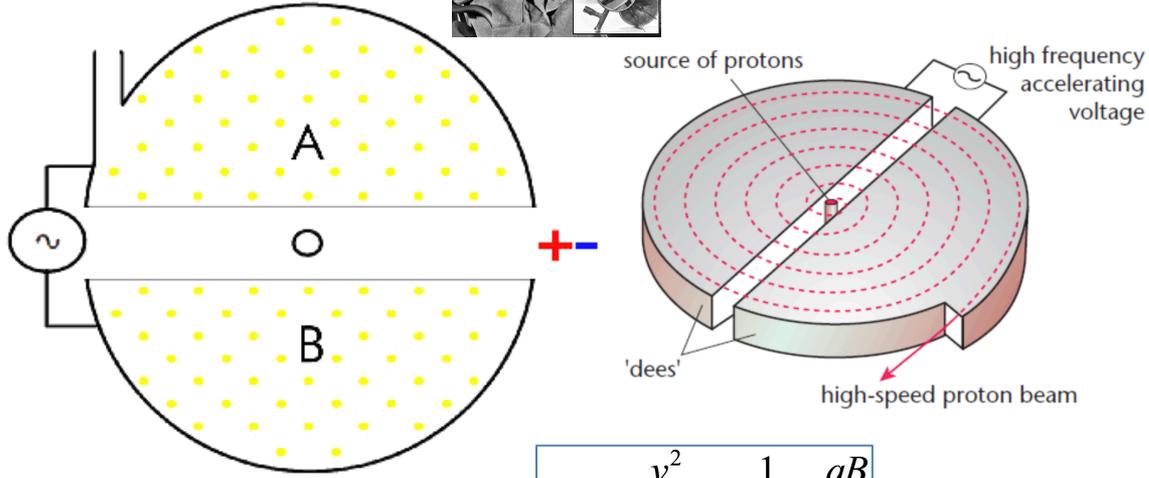
**Typical voltage:**  
**~ 10 MV/m**



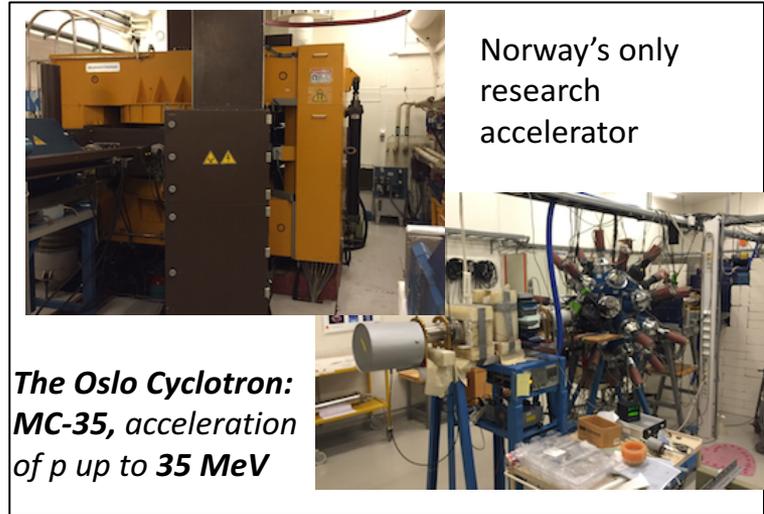
Later development: enclose RF-fields in metal cavities (RF cavities)

# Circular accelerators

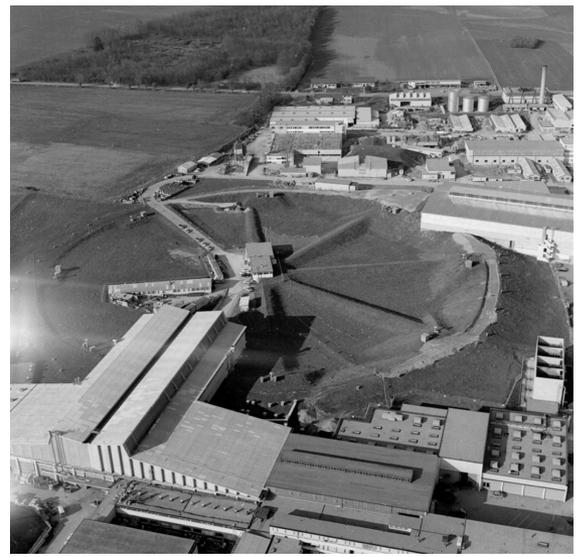
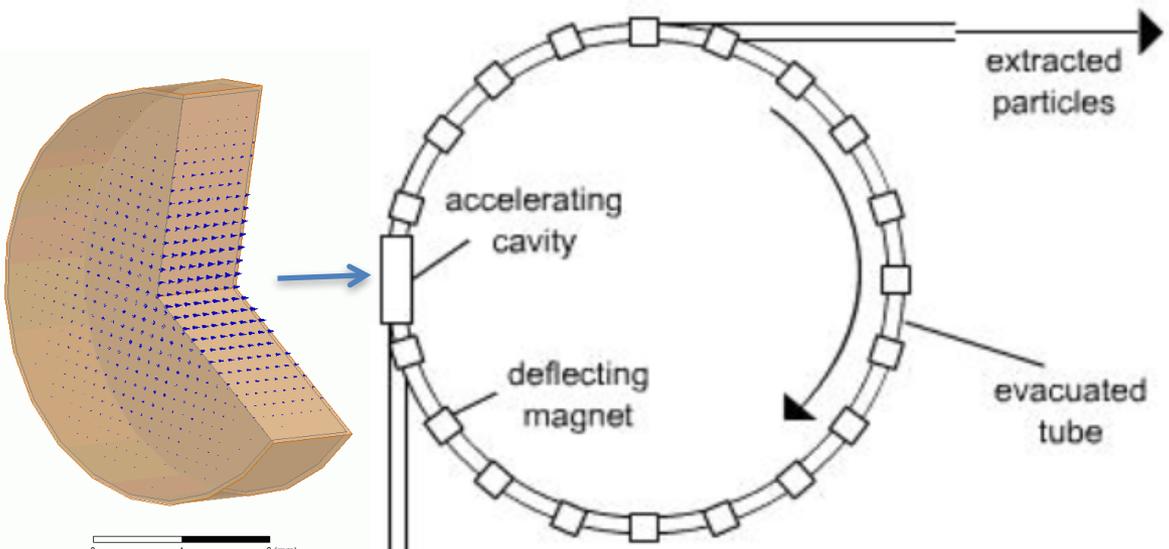
## Cyclotrons :



$$F_B = m \frac{v^2}{\rho} \Rightarrow \frac{1}{\rho} = \frac{qB}{p}$$



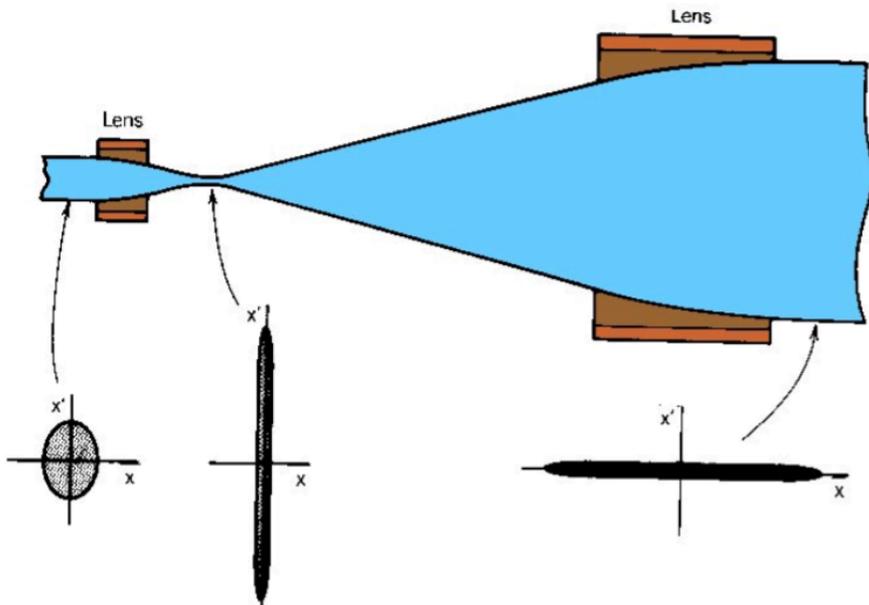
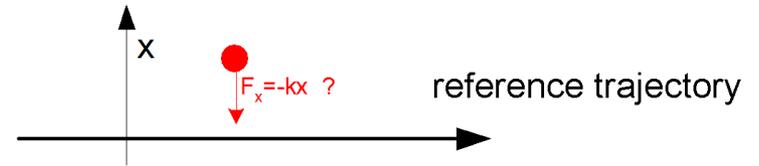
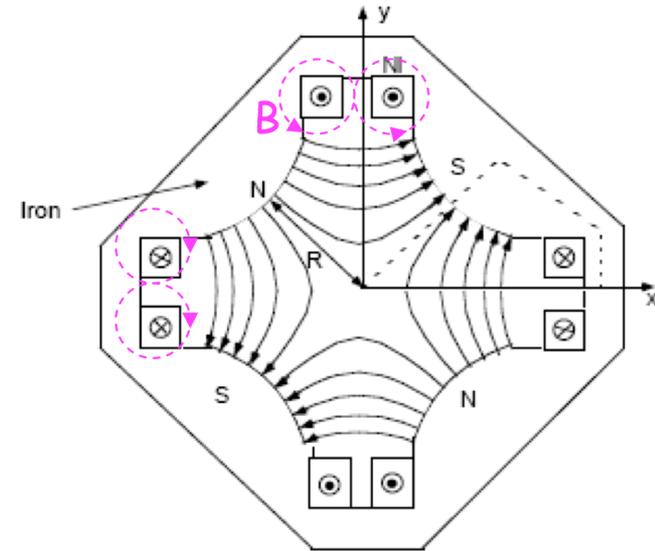
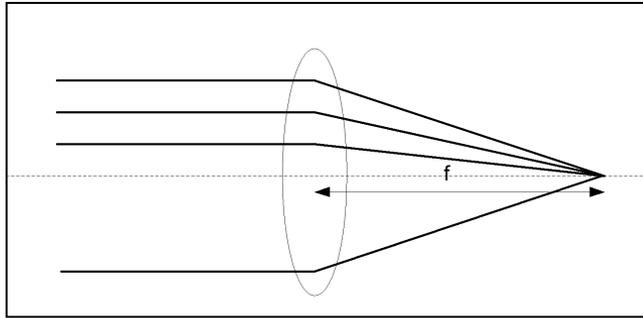
## Synchrotrons :



**The CERN Proton-Synchrotron (1959, 628 m) 28 GeV (28 billion volts)**

# Focusing of particle beams

Magnetic lenses, often **quadrupole magnets**, are used to focus the particle beams. Analogous to optical lenses.



$$\sigma(s) = \sqrt{\epsilon_{rms} \beta(s)}$$

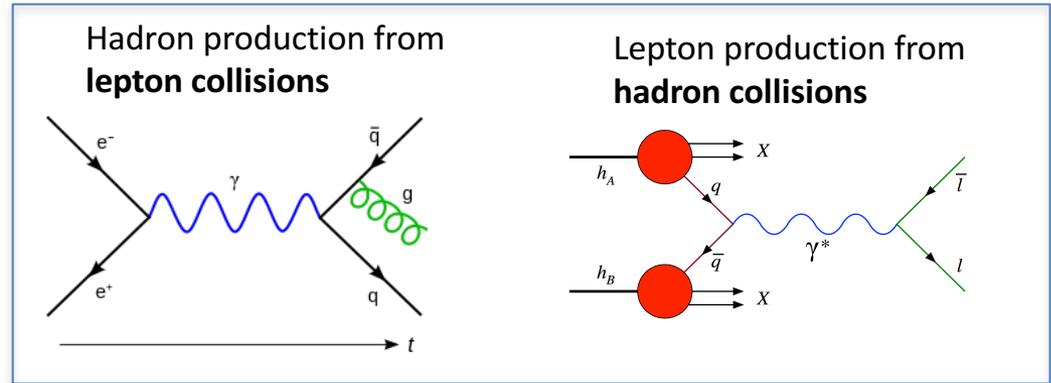
Lattice

Beam quality: emittance

# What characterizes a particle collider?

## I) Particle type

$p, p_{\text{bar}}, Pb, Au...$   
 $e^-, e^+, \mu, \gamma...$



## II) Centre of mass energy

Centre-of-mass energy sufficient for particle production:

$$E_{\text{CM}} \geq mc^2$$

Wavelength of probe should be smaller than the object you want to study. De Broglie wavelength:  $\lambda = h / p$  ( $\sim 1 \text{ \AA}$  for 100 MeV  $e^-$ )

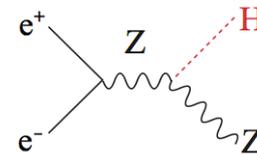
## III) Luminosity

Small cross sections  $\rightarrow$  production rate as important as energy

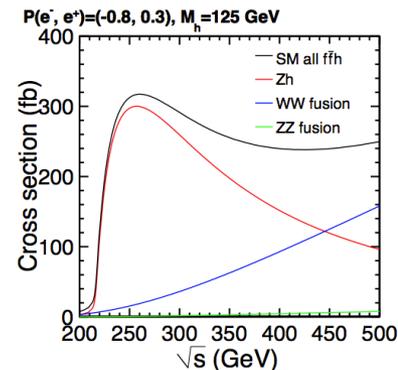
$$R = \mathcal{L} \sigma$$



$$\mathcal{L} = f \frac{n_1 n_2}{4\pi\sigma_x \sigma_y}$$

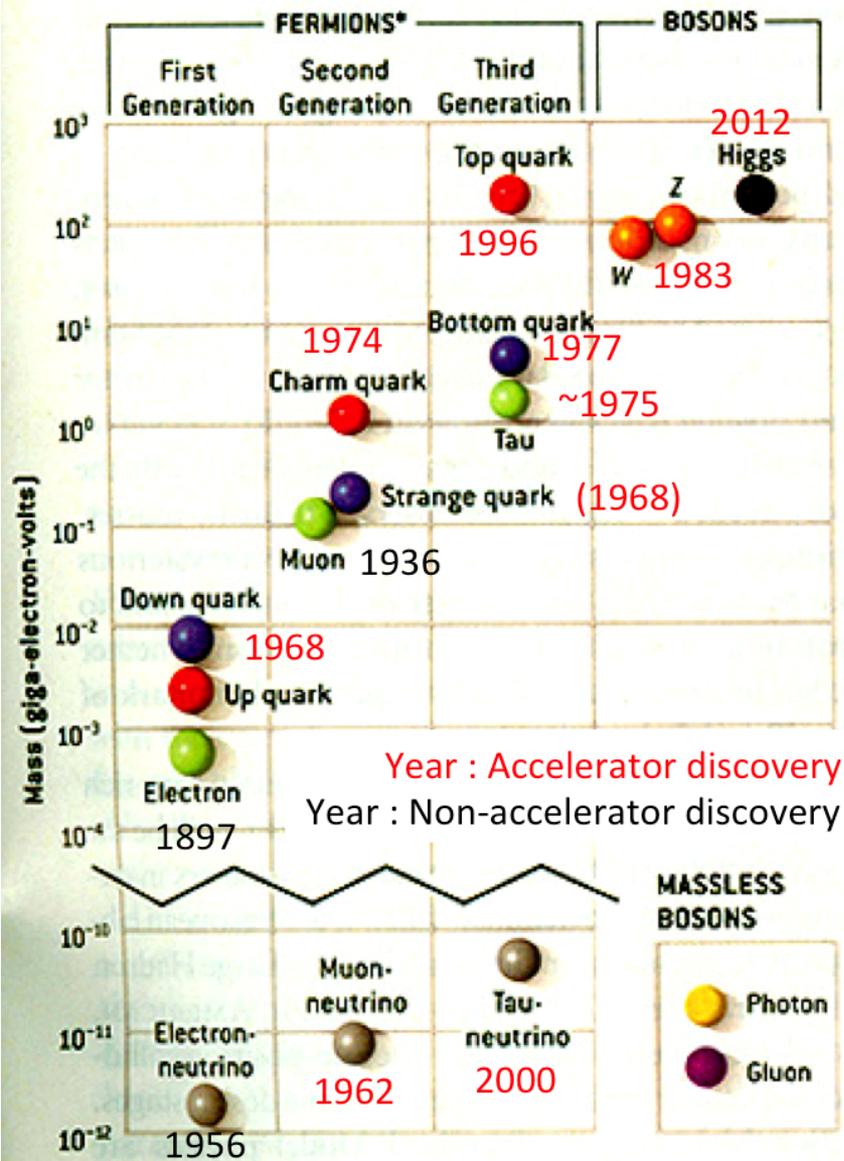


- \*  $n_1, n_2$ : particles per bunch
- \*  $\sigma_x, \sigma_y$ : bunch transverse size at the interaction point
- \* bunch collision rate ( f )

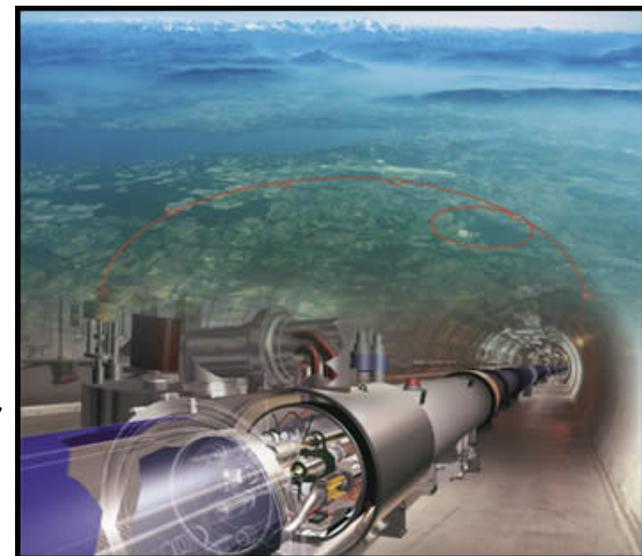


The **development of particle accelerators** has been driven by the quest for the understanding of the **fundamental origins of matter**.

## Up to 14 trillion volt (LHC)



*The Stanford Linear Accelerator (1966, 3 km) 50 GeV electrons and positrons  
 $L \sim 10^{30}/\text{cm}^2/\text{s}$*

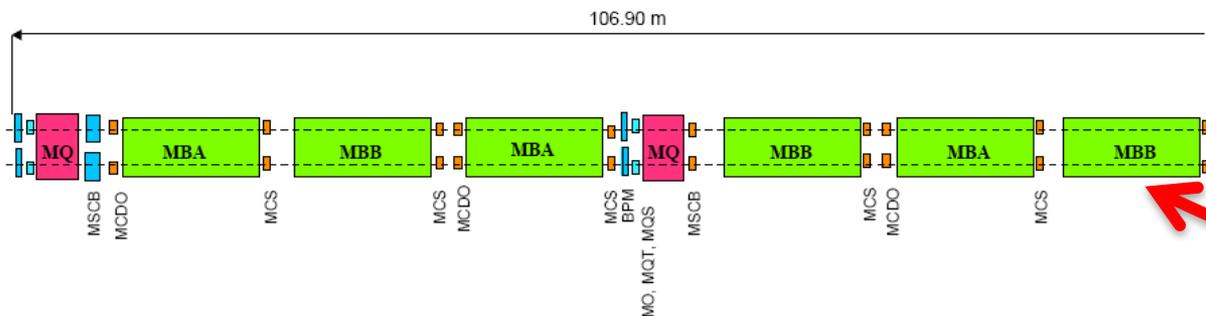
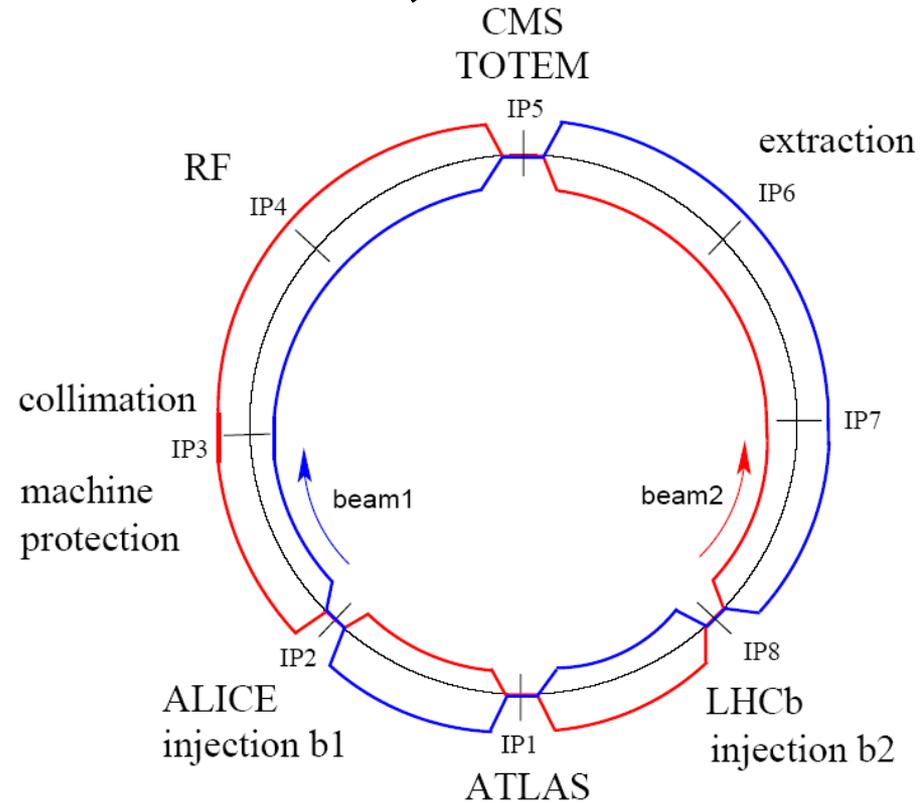


*The Large Hadron Collider, CERN (2008, 27 km)  
 6.5 TeV protons  
 $L \sim 10^{34}/\text{cm}^2/\text{s}$*

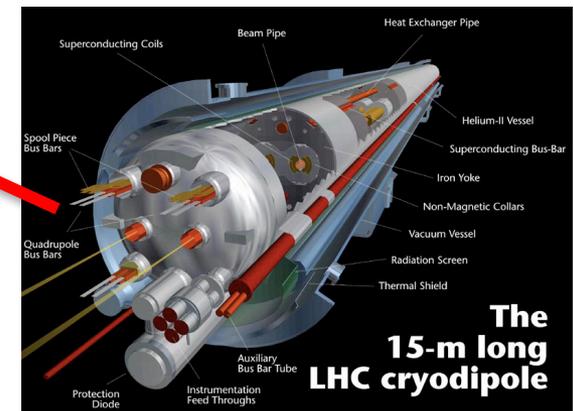
# The Large Hadron Collider

# The Large Hadron Collider, LHC

- Circumference = 26.7 km
- Four interactions points, where the beams collide, and massive particle physics experiments record the results of the collisions (ATLAS, CMS, ALICE, LHCb)
- Eight straight sections, containing the IPs, around 530 m long
- The arcs uses **1200 superconducting dipole magnets** to bend the paths of the protons



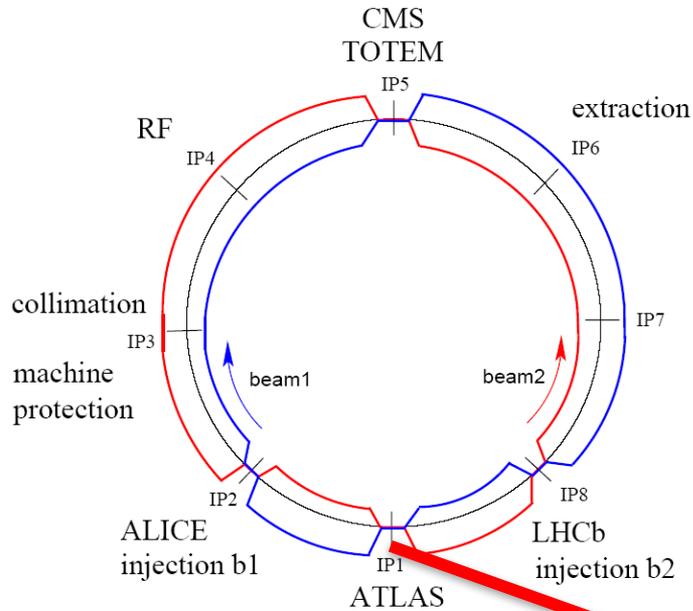
**B=8.3 T** maximum field, limits proton beam energy to **7 TeV**. Generated by a current of **12 kA** in the superconducting Rutherford coils.



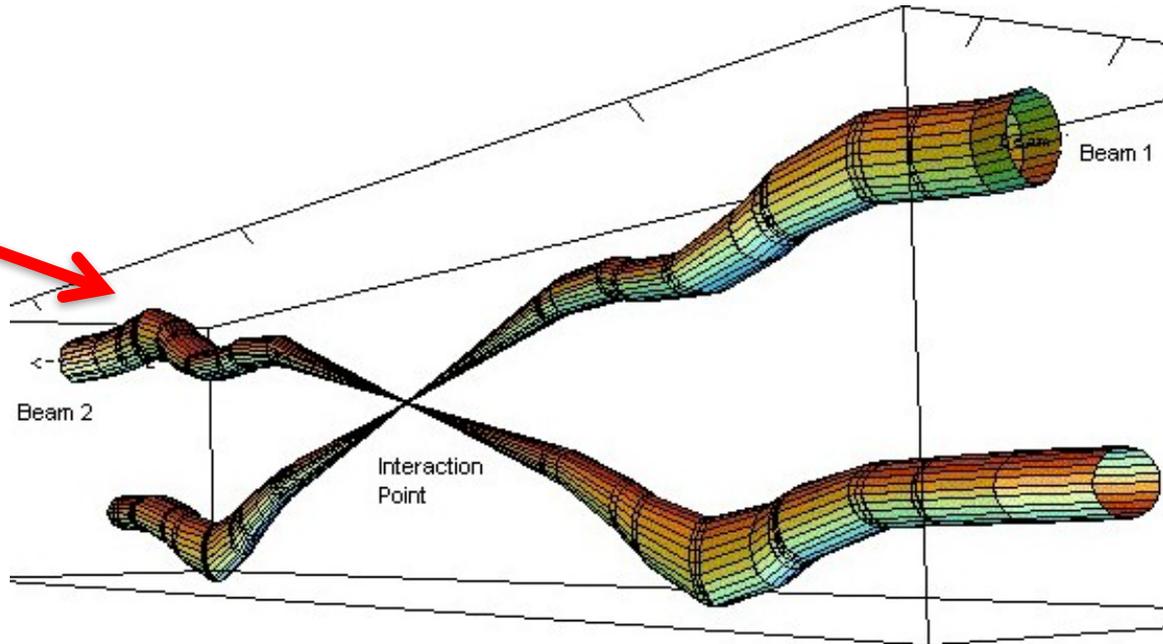
**The 15-m long LHC cryodipole**

# LHC beam focusing

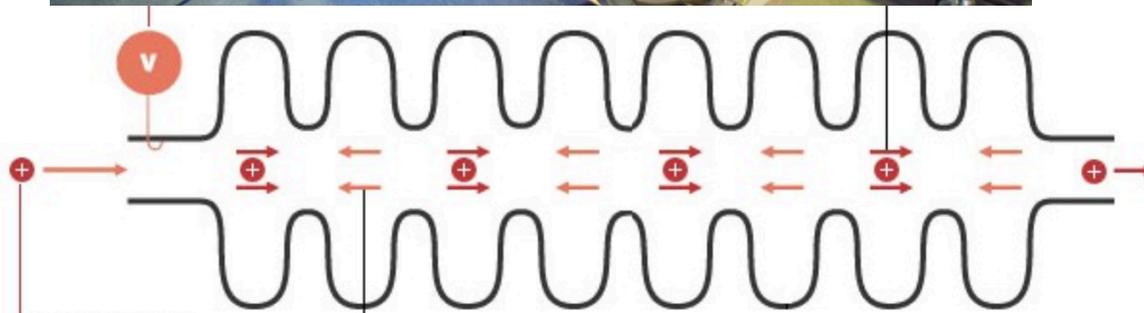
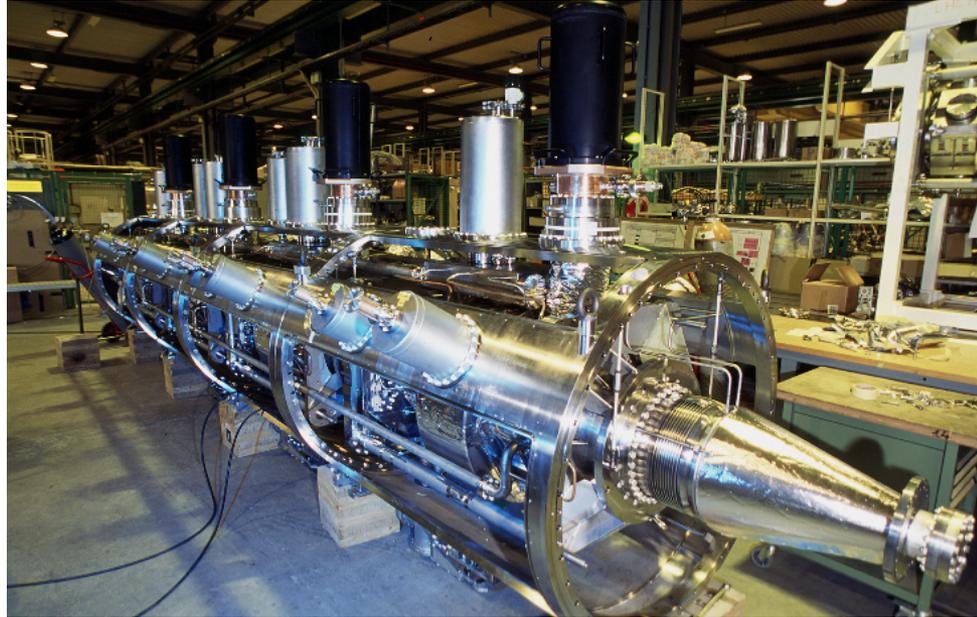
Bunches with  $n=1e11$  protons, at  $f=40$  MHz, are focused to 1 mm  $\sigma$  in arcs, squeezed down to  $\sigma=20$   $\mu\text{m}$  at the IP.



$$\mathcal{L} = f \frac{n_1 n_2}{4\pi\sigma_x \sigma_y}$$



# LHC cavities

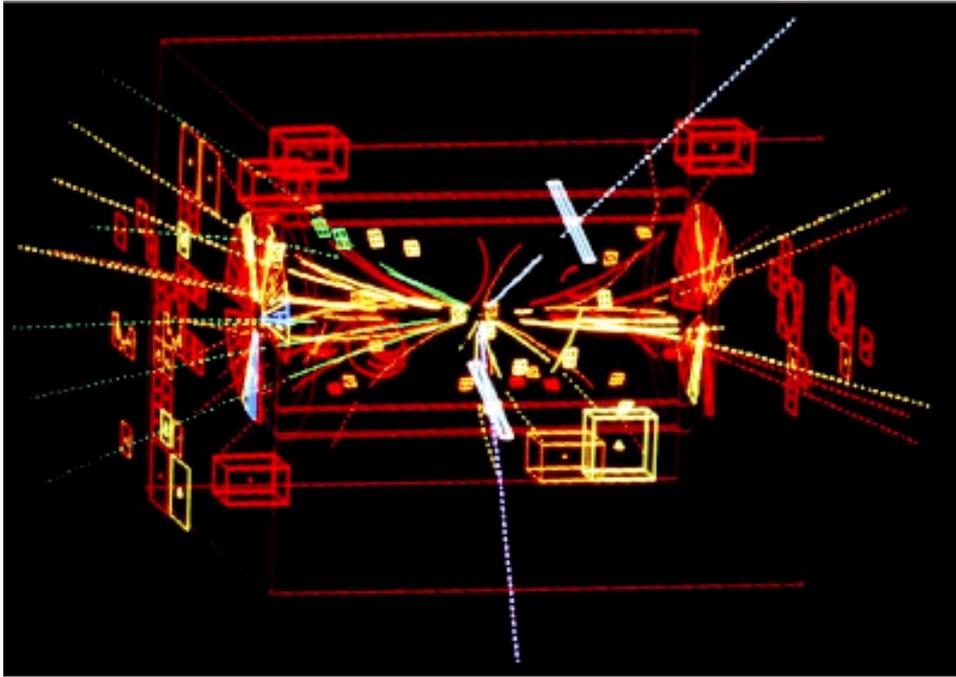


- Superconducting RF cavities. Standing wave,  $f = 400$  MHz
- Each beam: one cryostat at 4.5 K, 4+4 cavities in each cryostat
- **5 MV/m accelerating gradient**, 16 MeV energy gain per turn

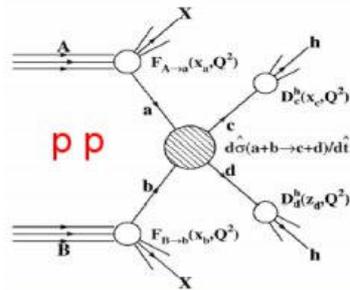
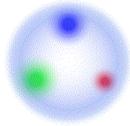
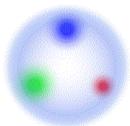
# Future Colliders

# Example of physics at **Lepton Colliders vs Hadron colliders**

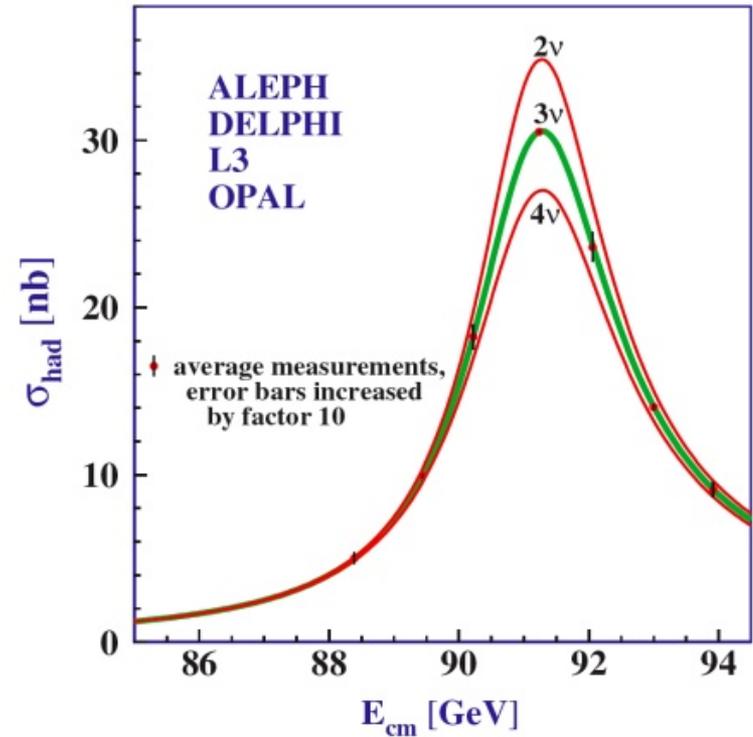
1983



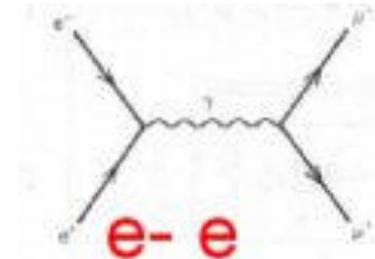
Hadron collider  $Sp\bar{p}S$ ,  $\sqrt{s}=540$  GeV,  
 $W^{+/-}$  and  $Z^0$  discovery



1990s

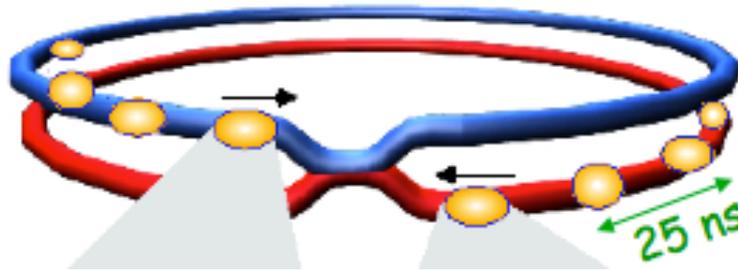


Lepton collider LEP,  $\sqrt{s}_{\max}=209$  GeV,  
 precision measurements of  $Z^0$   
 decay width



# Hadron versus lepton, Linear versus circular colliders

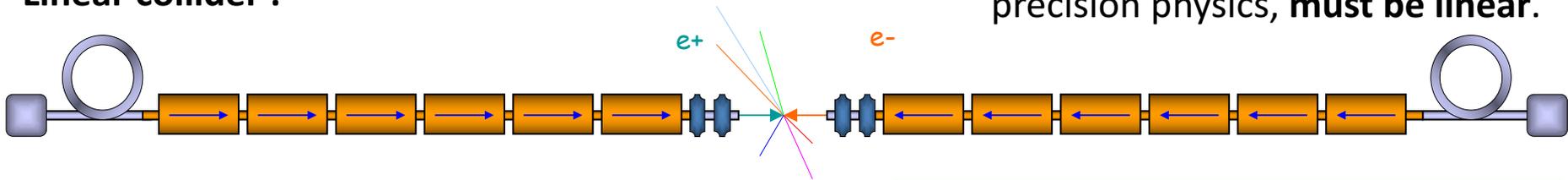
Circular collider :



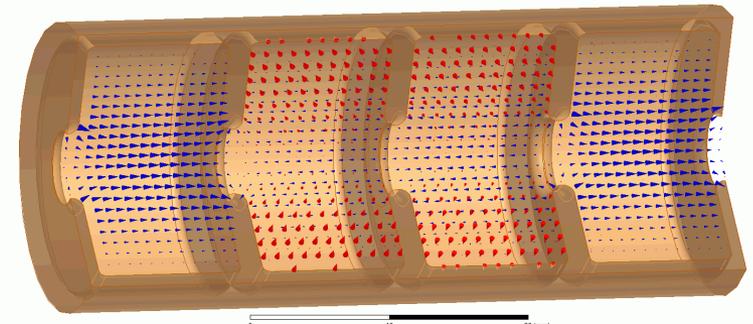
$$P_e = \frac{e^2 c}{6\pi\epsilon_0} \frac{1}{(m_0 c^2)^4} \frac{E^4}{R^2}$$

Due to **synchrotron radiation**, a TeV-scale electron-positron collider, for precision physics, **must be linear**.

Linear collider :

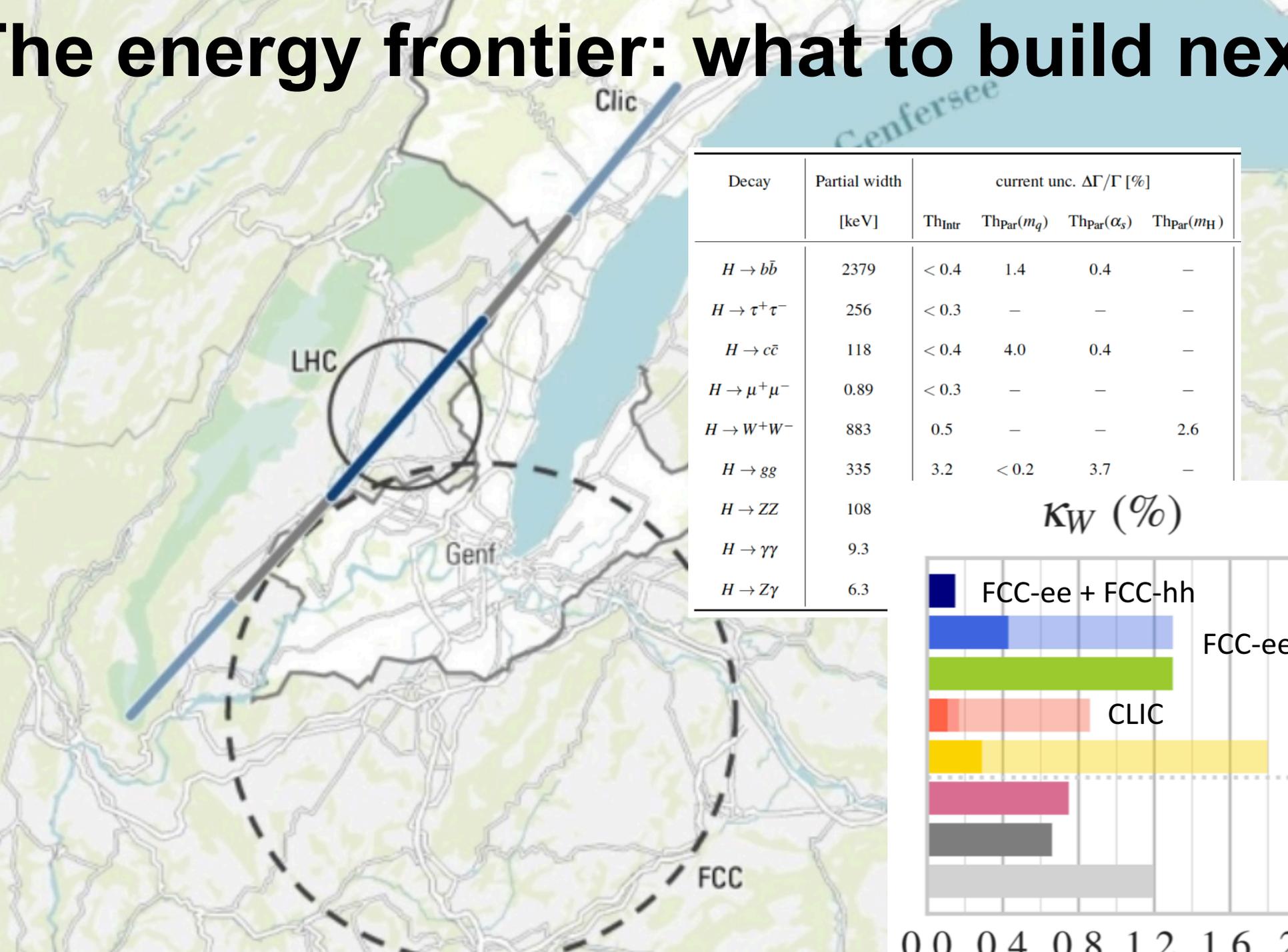


**Length of a linear collider:** Each cavity accelerates each bunch only once. Collider length is driven by how large electric field can be sustained in a metallic cavity.

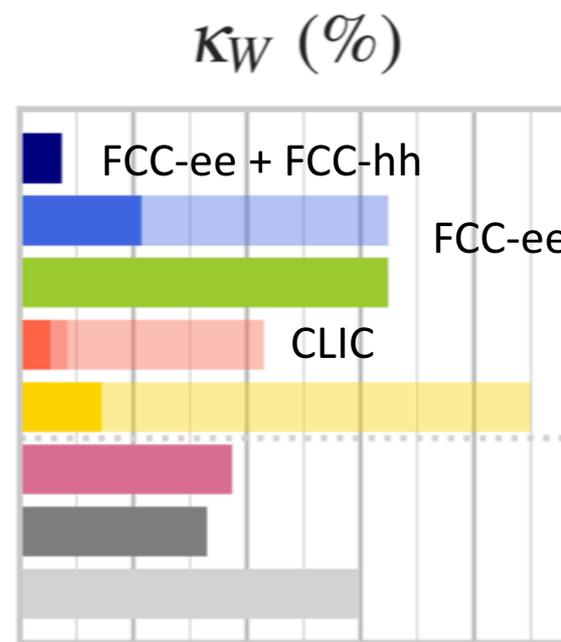


Electromagnetic field break down :  
Limits acceleration to **10 - 100 MV/m**

# The energy frontier: what to build next



Decay	Partial width [keV]	current unc. $\Delta\Gamma/\Gamma$ [%]			
		$\text{Th}_{\text{intr}}$	$\text{Th}_{\text{Par}}(m_q)$	$\text{Th}_{\text{Par}}(\alpha_s)$	$\text{Th}_{\text{Par}}(m_H)$
$H \rightarrow b\bar{b}$	2379	< 0.4	1.4	0.4	–
$H \rightarrow \tau^+\tau^-$	256	< 0.3	–	–	–
$H \rightarrow c\bar{c}$	118	< 0.4	4.0	0.4	–
$H \rightarrow \mu^+\mu^-$	0.89	< 0.3	–	–	–
$H \rightarrow W^+W^-$	883	0.5	–	–	2.6
$H \rightarrow gg$	335	3.2	< 0.2	3.7	–
$H \rightarrow ZZ$	108				
$H \rightarrow \gamma\gamma$	9.3				
$H \rightarrow Z\gamma$	6.3				

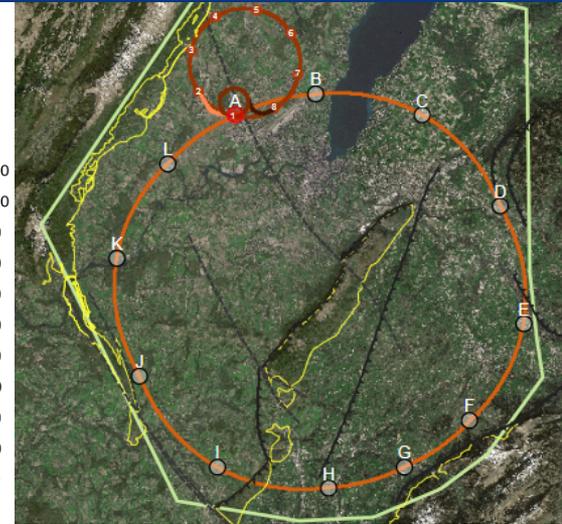
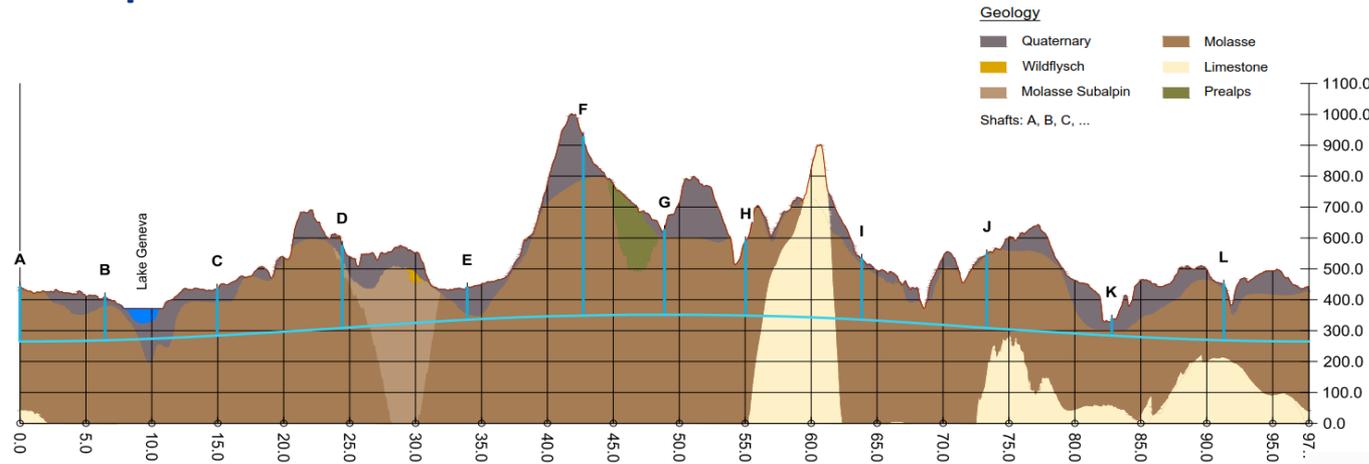


00 04 08 12 16 20

# The Future Circular Collider

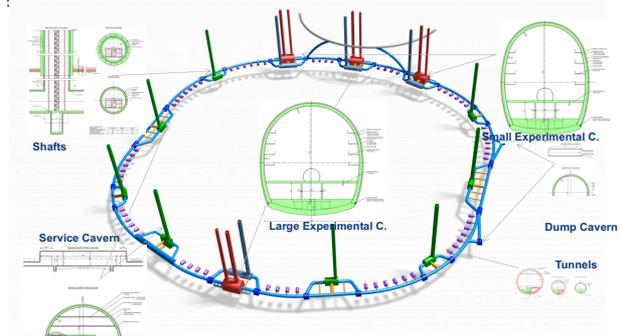
## FCC integrated program inspired by succesful LEP – LHC programs at CERN

### Implementation studies in Geneva basin:



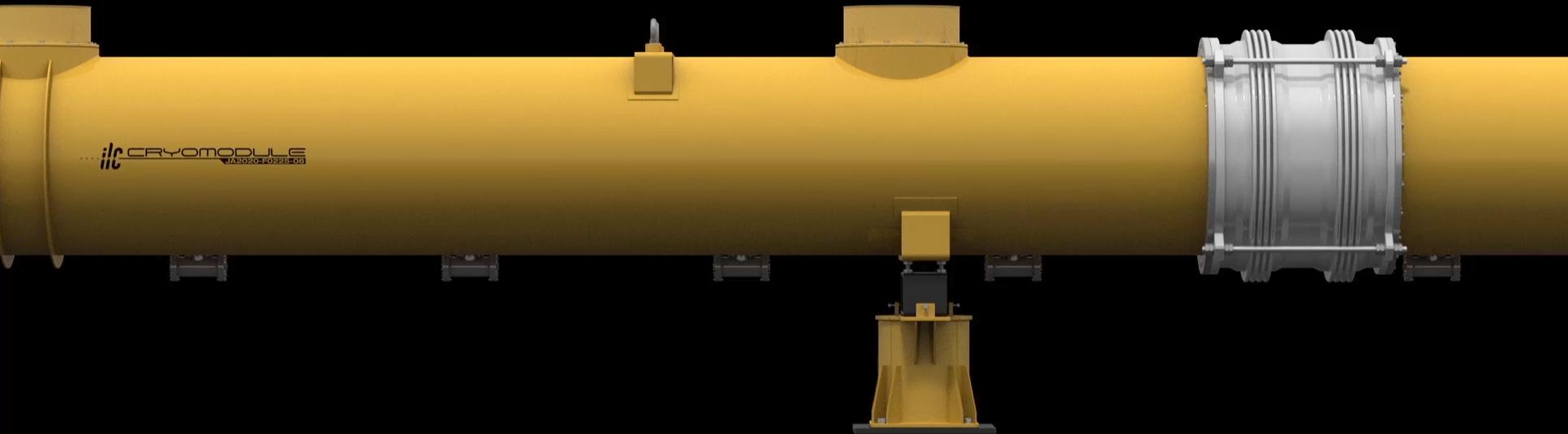
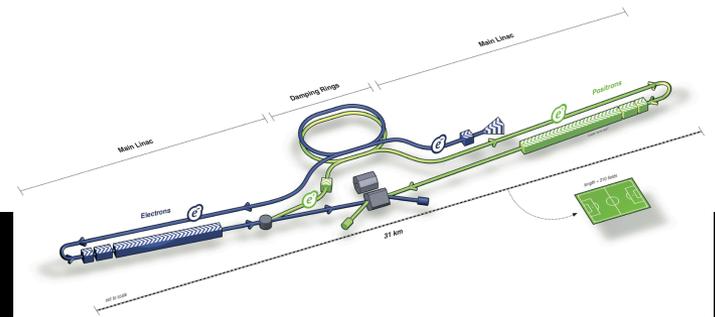
### baseline position was established considering:

- minimum risk for construction, fastest and cheapest construction
- efficient connection to CERN accelerator complex
- Total construction duration 7 years
- First sectors ready after 4.5 years



**Up 100 TeV protons, with 16 T Nb<sub>3</sub>Sn magnets (time scale ~ 40 years)**  
**Up to 365 GeV electrons-positron collisions (time scale ~ 15 years)**

# The International Linear Collider: Fly-through of how to make 500 GeV collisions with superconducting RF technology

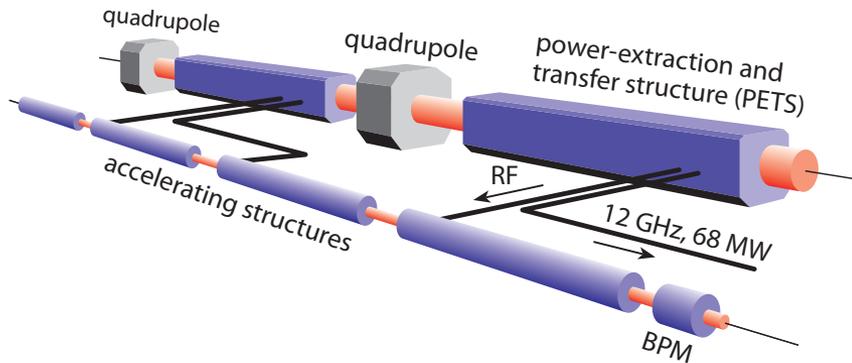


At some point cost and practical considerations will limit the size of future colliders.

# Linear Collider Projects

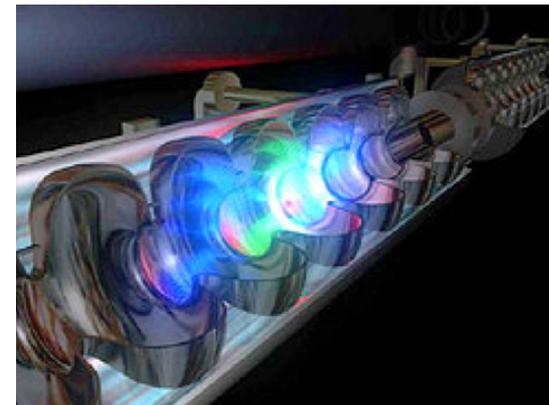
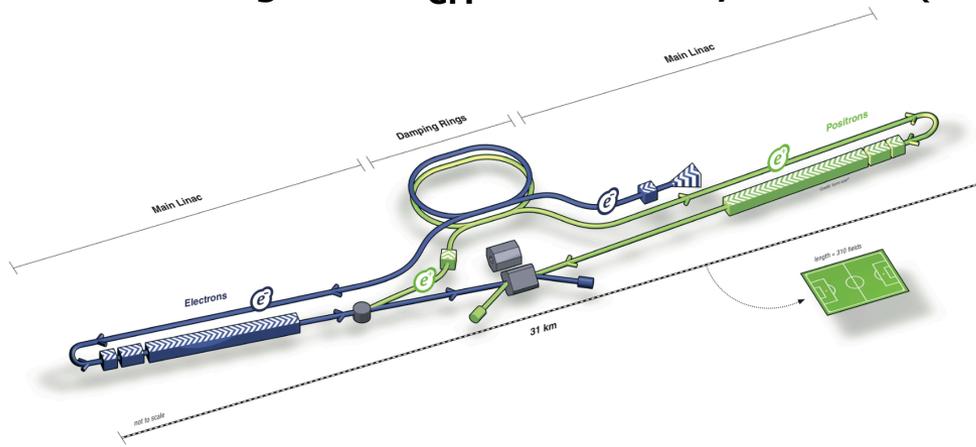
## The Compact Linear Collider, CLIC

Main linac technology: two-beam scheme. **Normal conducting Cu RF 12 GHz TW cavities, 100 MV/m.** Nominal design for  $E_{CM} = 3 \text{ TeV}$ , 50 km (375 GeV to 3 TeV)

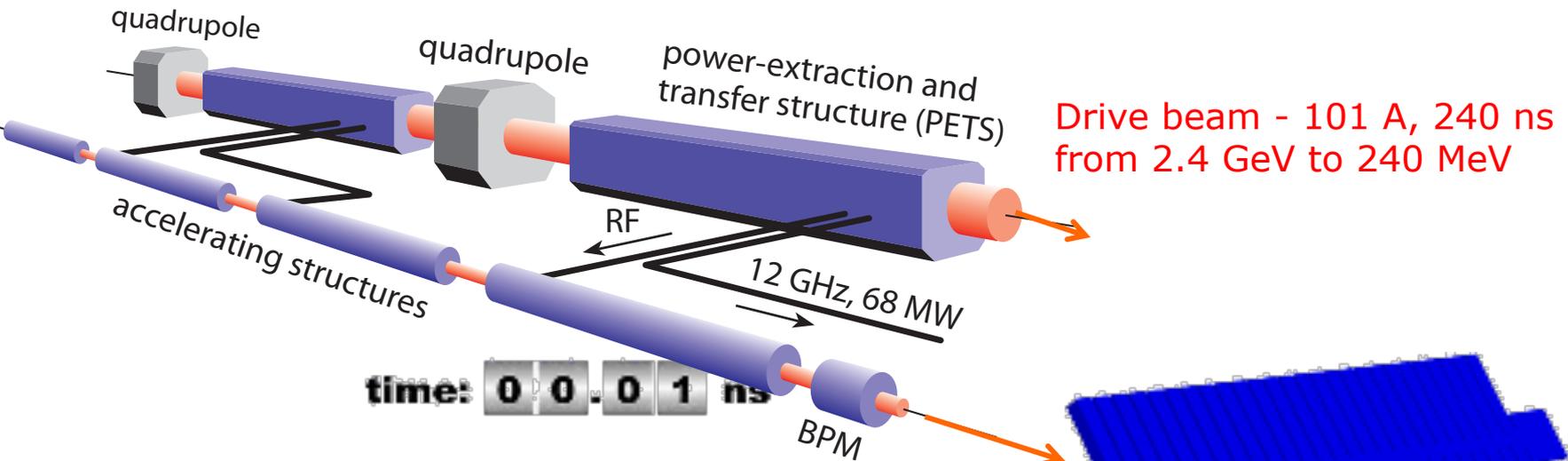


## The International Linear Collider, ILC

Main linac technology: **super conducting RF 1.3 GHz SW cavities, 31.5 MV/m**  
Nominal design for  $E_{CM} = 0.5 \text{ TeV}$ , 31 km (250 GeV to 1 TeV)



# The CLIC Two-Beam scheme



Main beam - 1 A, 156 ns from 9 GeV to 1.5 TeV

CLIC: "Transformer ratio" of  $\sim 1.5 \text{ TeV} / 2.4 \text{ GeV} = 15$



Demonstrated experimentally at the CLIC Test facility at CERN.

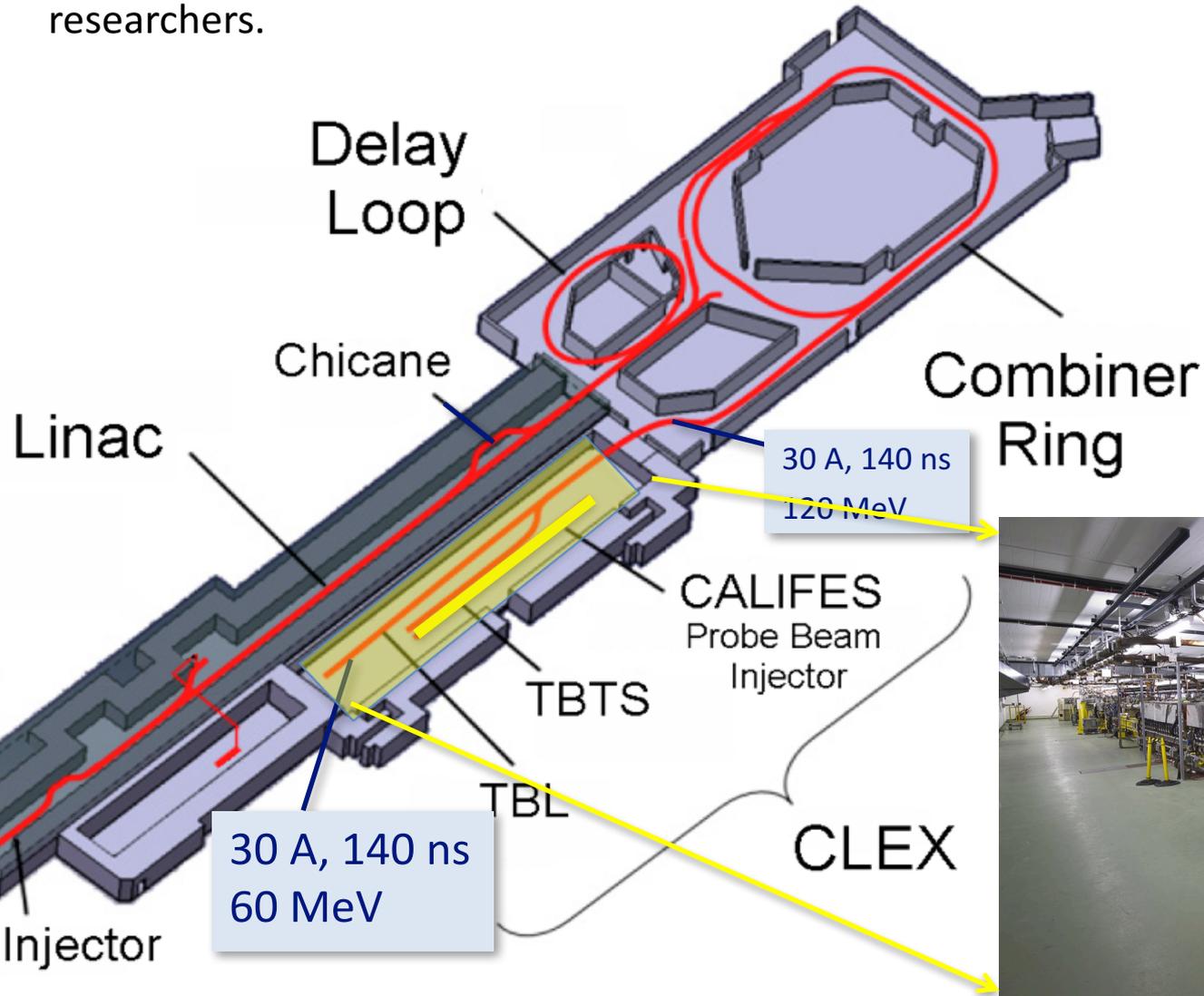
Animation courtesy SLAC ACD group (A. Candel)



# CLIC Test Facility and CLEAR

Test beam facility at CERN.

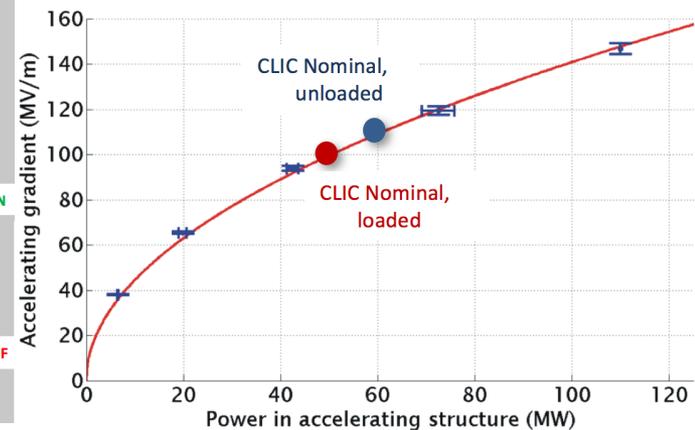
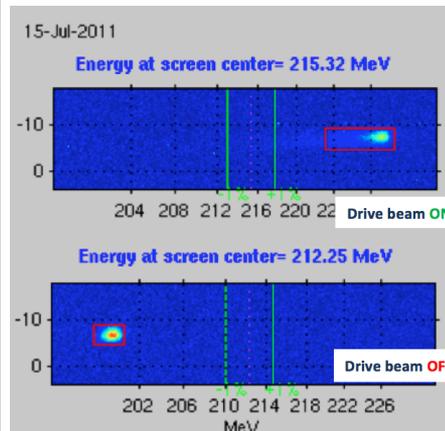
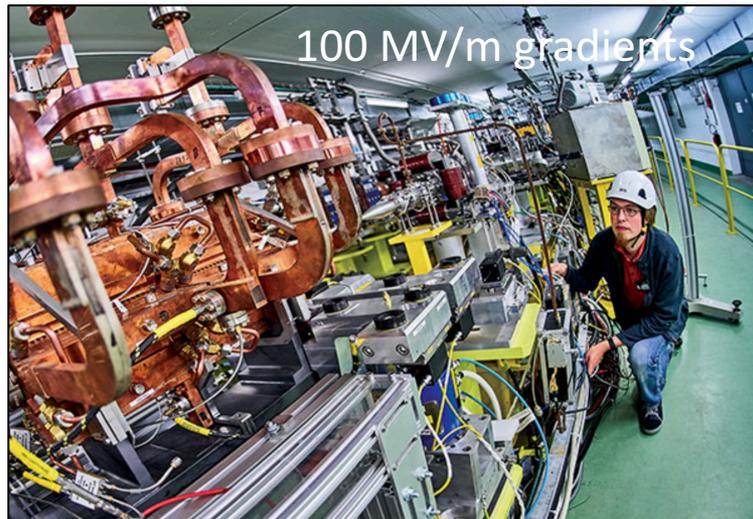
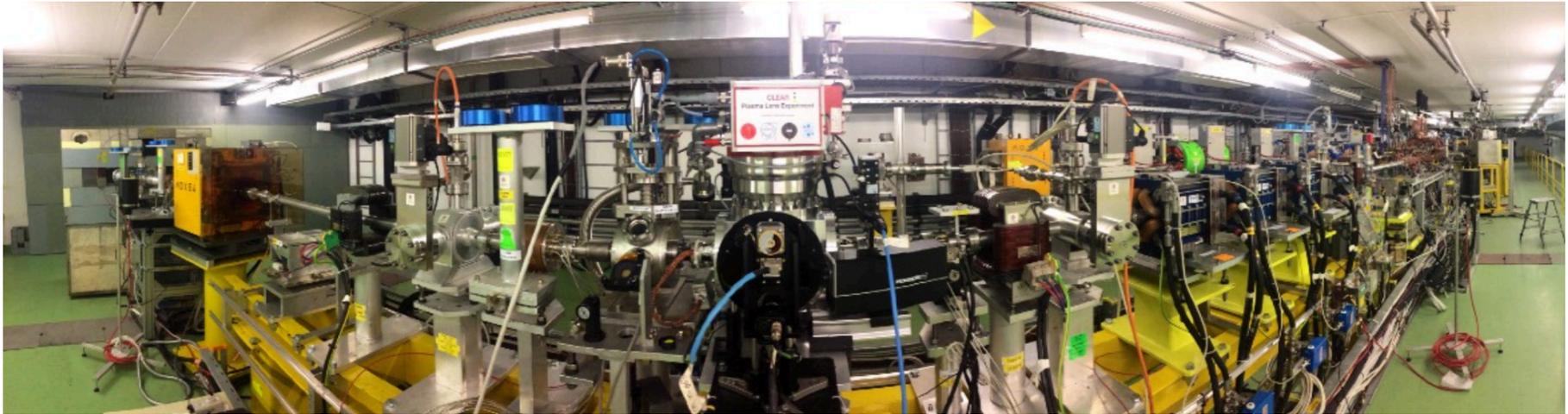
Research performed by Oslo students and Oslo researchers.



**CLEAR consists of the experimental hall, CLEX, housing the 200 MeV S-band electron CALIFES linac.**



# Experiments at the CLIC test-facility

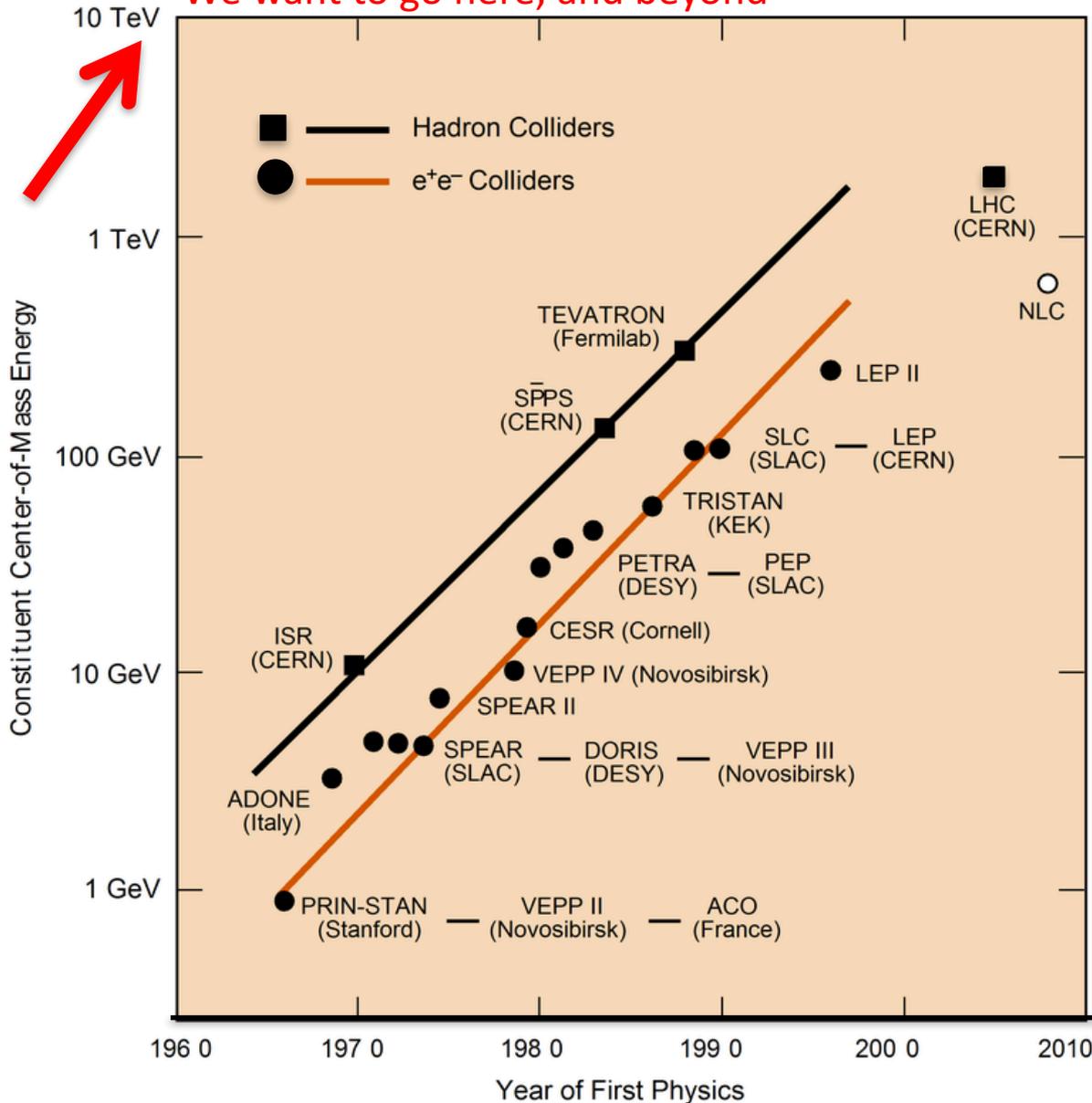


# Novel Accelerator Concept:

- plasmas acceleration
- **muon** colliders

# Particle collider Livingstone plot

We want to go here, and beyond



Particle accelerators have seen a tremendous improvement in performance since the 1960s.

-> research required to overcoming limits in luminosity/intensity and energy/power.

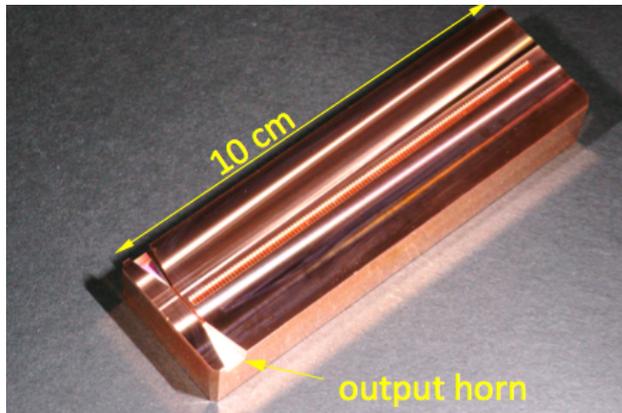
Great success of accelerator physics and technology.

# Novel accelerator research

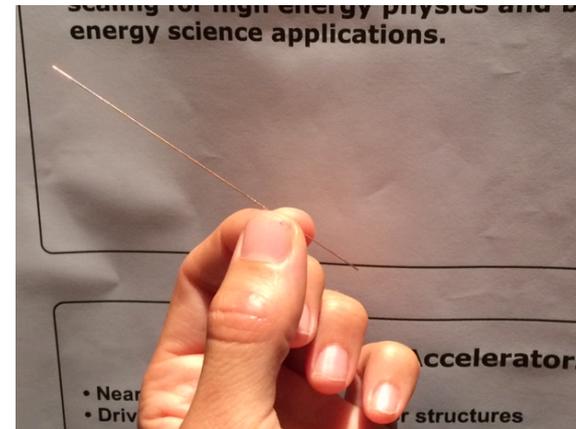
Cutting edge accelerator physics research, with the objective of **overcoming limitations** of conventional accelerator technology.

**Very high frequency** normal conducting rf structures ( $\sim 100$  GHz to  $\sim$ THz)

116 GHz structure (SLAC)

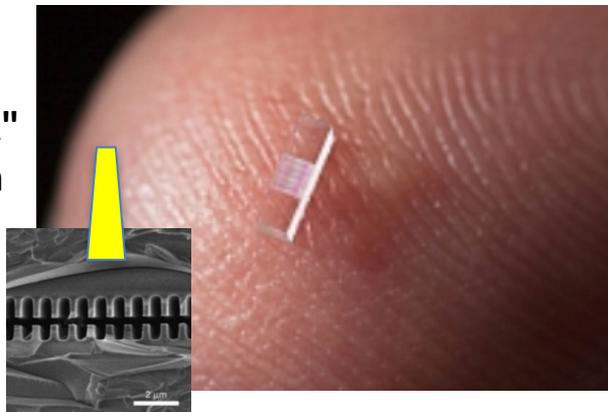


## Dielectric structures

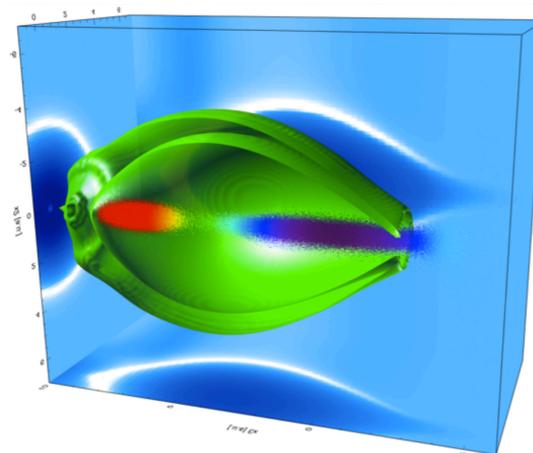


SiO<sub>2</sub>  
 $\sim 1.0$  THz,  
1-10GV/m

**Laser based acceleration "DLA"**  
Several 100 MV/m demonstrated (SLAC)



Feed of laser beam into Si structure



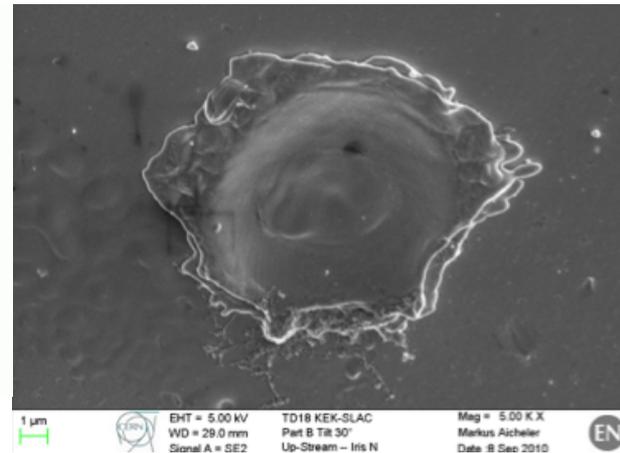
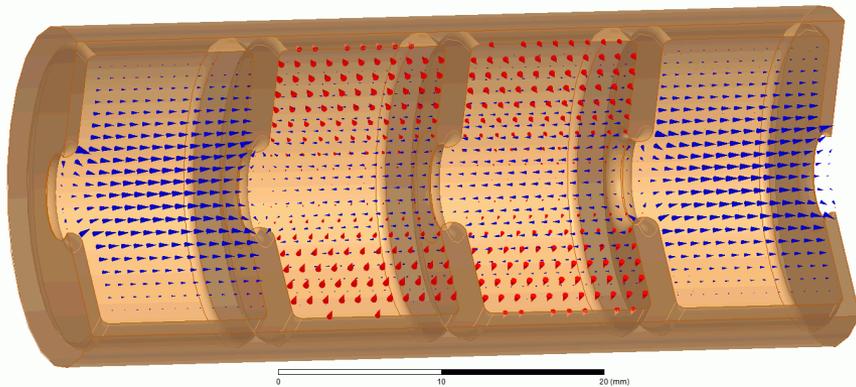
**Plasma wakefield acceleration**

The topic here.

# Breakdown limits and plasma

In **metallic structures** : break down of the surfaces, creating electric discharge. Field cannot be sustained. **Current practical limit (CLIC): order of 100 MV/m gradients..**

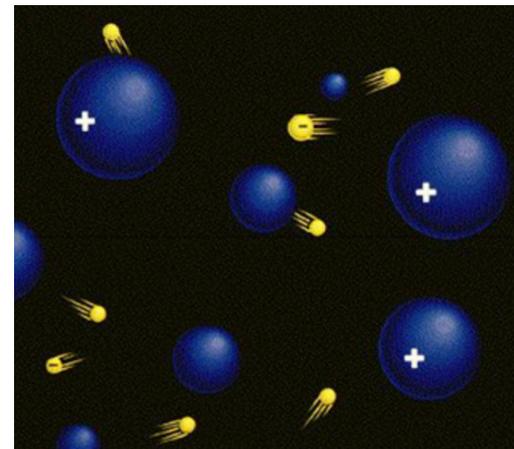
*Break down of field limits the gradient.*



## Alternative to high fields in vacuum: high fields in plasmas:

collection of free ions and electrons.

- Plasmas of a large range of densities can be produced. Fields scales with density. **Very high fields can be generated.**
- Material is already broken down. The plasma can **sustain the very high fields.**



# Gauss law : estimate fields in a plasma wave

Assume that the **plasma electrons are pushed out** of a small volume of neutral plasma, with plasma density  $n_0 = n_e = n_{\text{ion}}$  :

## Scale of electrical fields (1D) :

Gauss' law:

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0} \sim \frac{en_{\text{ions}}}{\epsilon_0} \sim \frac{en_0}{\epsilon_0}$$

Assume wave solutions:

$$\mathbf{E} \sim \mathbf{E}_0 \exp(-i\omega_p/cz)$$

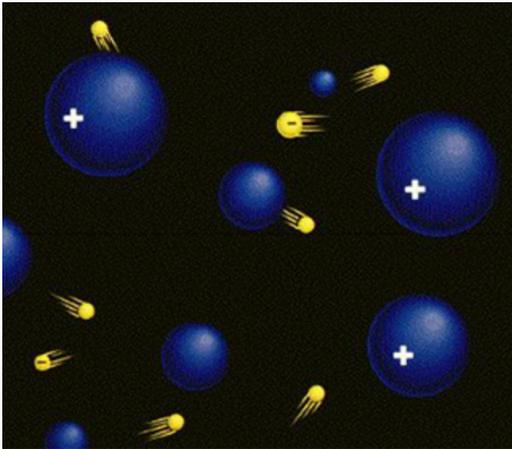
Apply Gauss' law:

$$\frac{en_0}{\epsilon_0} = E_0 \frac{\omega_p}{c} \Rightarrow E_{WB} = \frac{ecn_0}{\epsilon\omega_{0p}} \sim \sqrt{n_0}$$

**Field scale,  $E_{WB}$**   
"wave breaking field"

Plasma electron frequency :

$$\omega_p = \sqrt{\frac{n_0 e^2}{m_e \epsilon_0}}$$



Typical plasma density, available by many types of plasma source :

$$n_0 = 1e17/\text{cm}^3 : \mathbf{E}_{WB} = \mathbf{30 GV/m}$$

# Plasma Wakefield acceleration

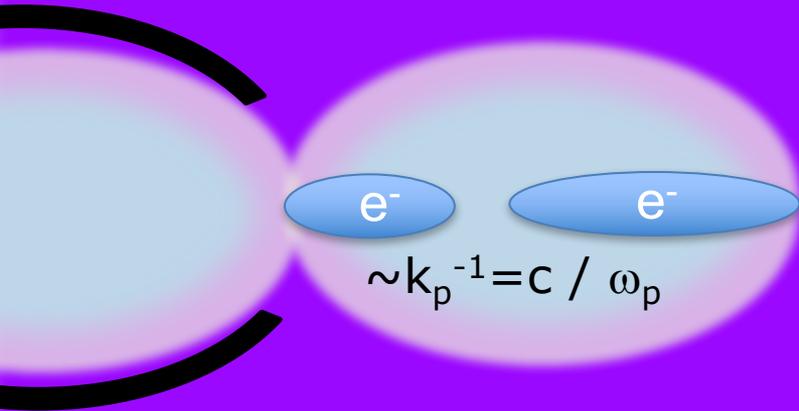
## Typical scales :

$$n_0 \sim 10^{14}-10^{18}/\text{cm}^3$$

$$\text{Fields: } E_{\text{WB}} \sim \mathbf{1-100 \text{ GV/m}} \sim \sqrt{n_0}$$

$$\text{Length : } k_p^{-1} = \lambda_p/2\pi \sim \mathbf{5-500 \text{ }\mu\text{m}} \sim \sqrt{n_0}$$

$$\text{Focusing : } F_r = \frac{1}{2}en_0r/\epsilon_0c \sim \mathbf{0.03-30 \text{ MT/m}}$$

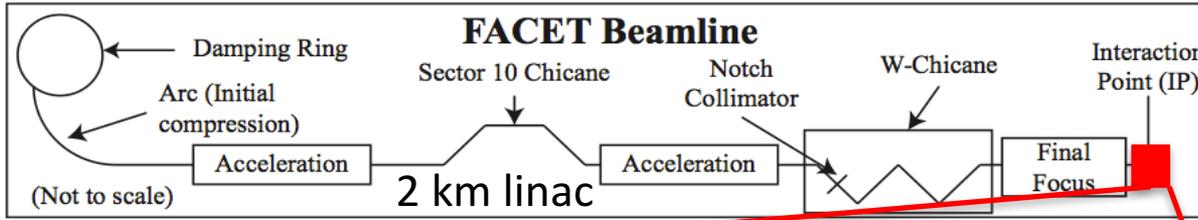


Ideas of **100s GV/m** electric fields in plasma, using  $10^{18} \text{ W/cm}^2$  lasers: 1979

**T.Tajima and J.M.Dawson** (UCLA), Laser Electron Accelerator, Phys. Rev. Lett. 43, 267–270 (1979).

Using particle beams as drivers: P. **Chen et al.** Phys. Rev. Lett. 54, 693–696 (1985)

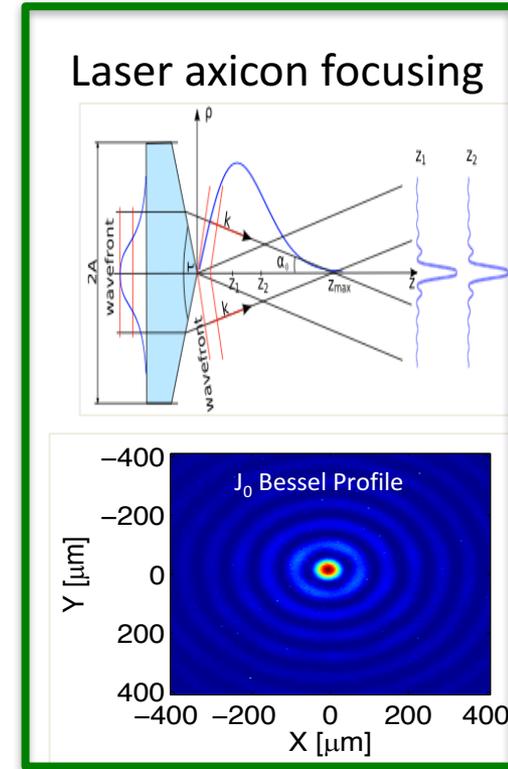
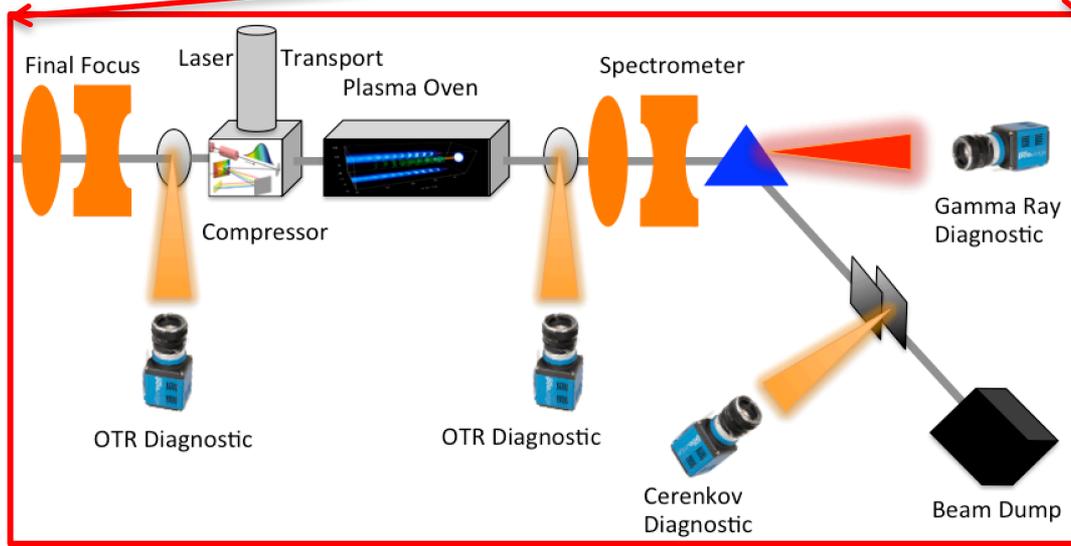
# Development of novel accelerators



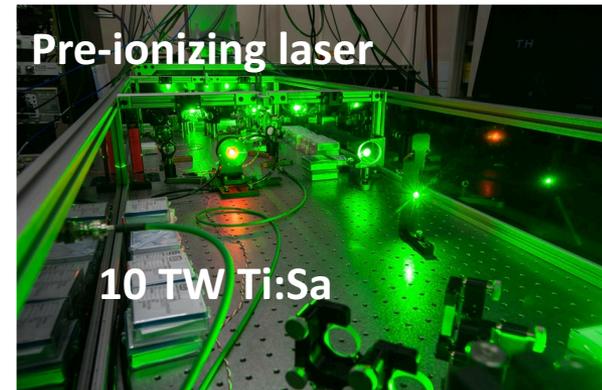
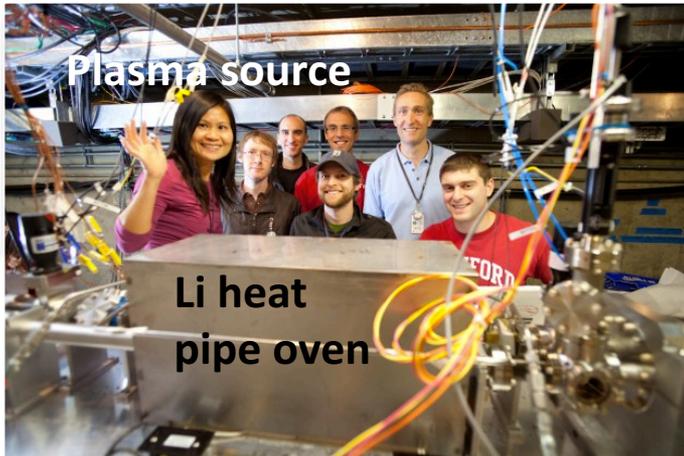
Electron, or Positron bunch



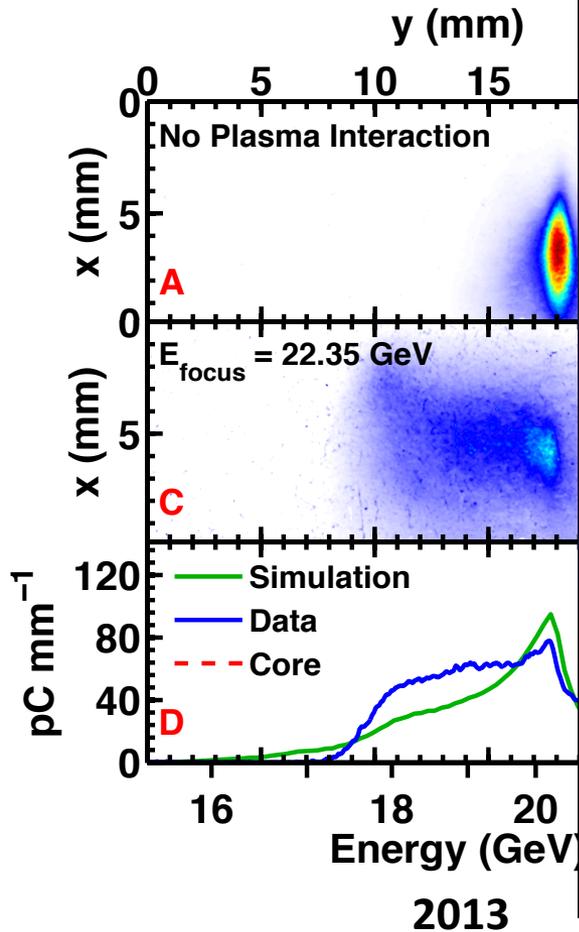
$E = 20 \text{ GeV}$   
 $Q = 3 \text{ nC}$   
 $\sigma_{z,\text{min}} = 20 \text{ }\mu\text{m}$   
 $\sigma_{r,\text{min}} = 20 \text{ }\mu\text{m}$   
 $\varepsilon_n \sim 100 \text{ }\mu\text{m}$



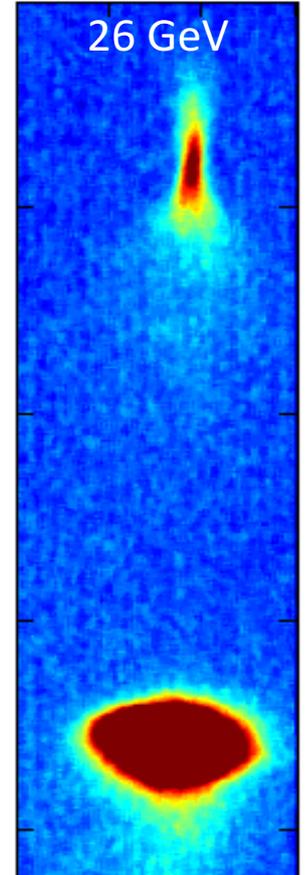
Plasma densities,  $n_0$ ,  $10^{16}$ - $10^{17} \text{ cm}^{-3}$   
 $\sim 1 \text{ m}$  length



# FACET two-bunch results



1.3 m plasma



2014

## Active plasma lenses

- Active plasma lenses consist of three main parts:
  - A **hollow capillary**, typically made from sapphire for durability
  - **Gas inlets** to fill the capillary with a low density gas (~mbar)
  - **Electrodes** on either side (upstream/downstream) to break down the gas and provide current.
- Works equally well for electrons and positrons

$$g = \frac{\partial B_\phi}{\partial r} = \frac{\mu_0 I_z}{2\pi R^2}$$

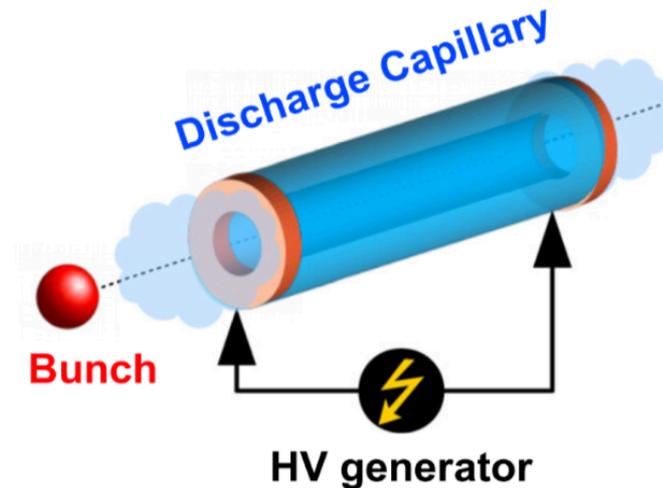


Image source: R. Pompili, *Appl. Phys. Lett.* 100 104101 (2017)

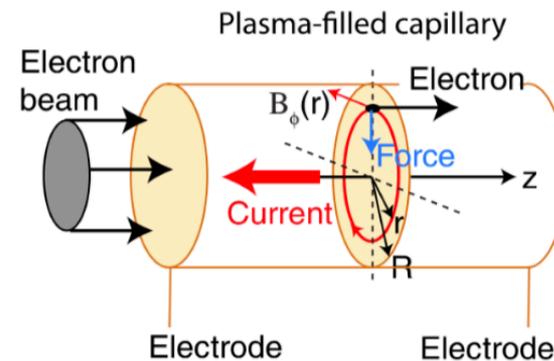


Image source: J. van Tilborg, *Phys. Rev. Lett* 115, 184802 (2015)

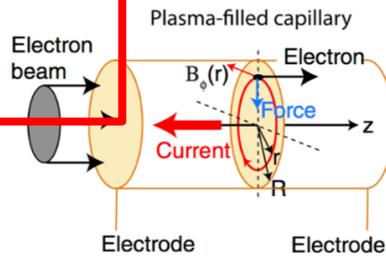
# The Oslo plasma lens experiment at CLEAR, CERN

a) Normal conducting magnetic focusing quadrupole at the FACET high energy test facility

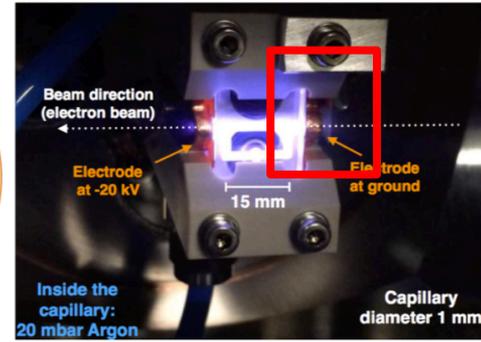


100 cm

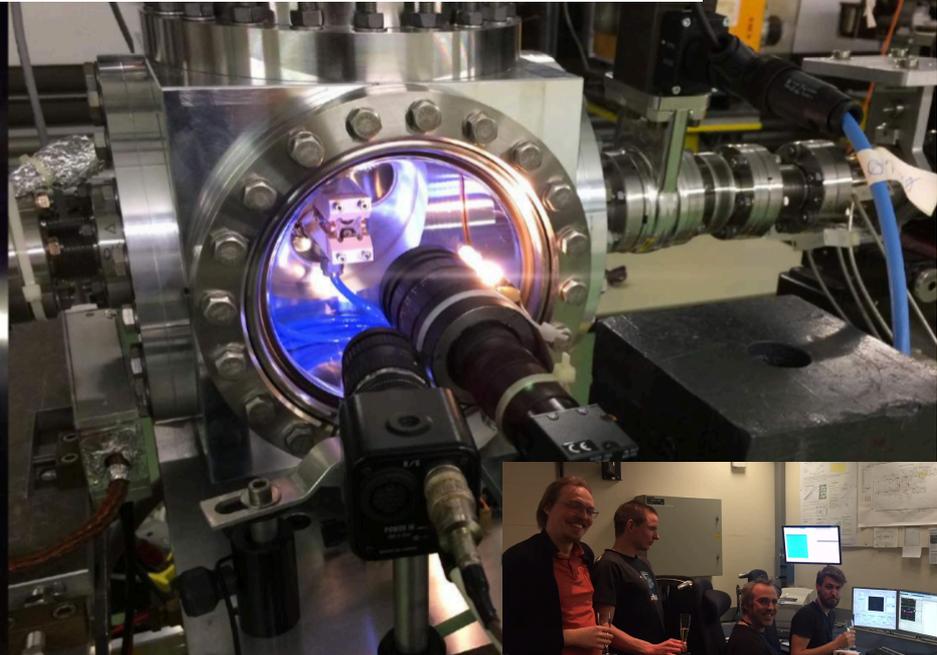
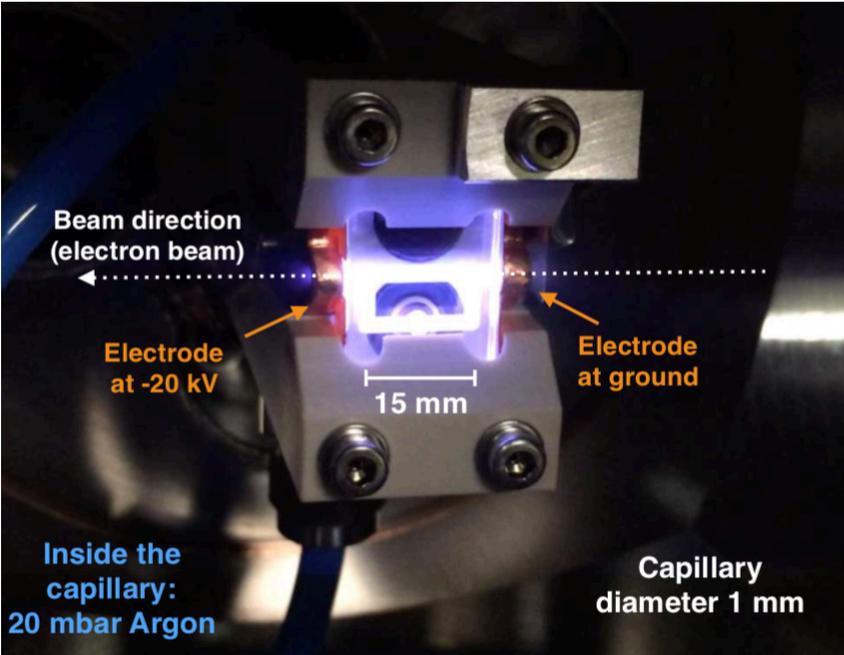
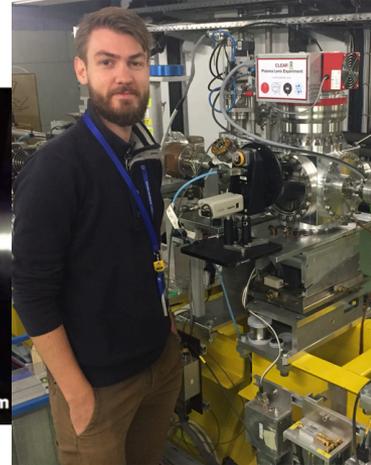
c) Principle of an active plasma lens



b) The Oslo active plasma lens focusing device



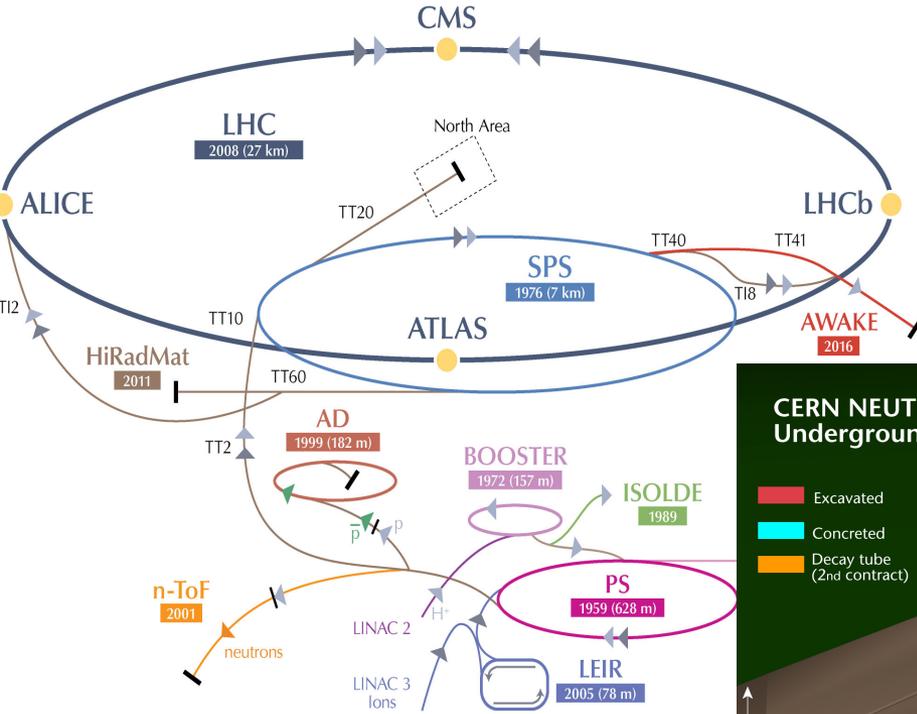
15 mm



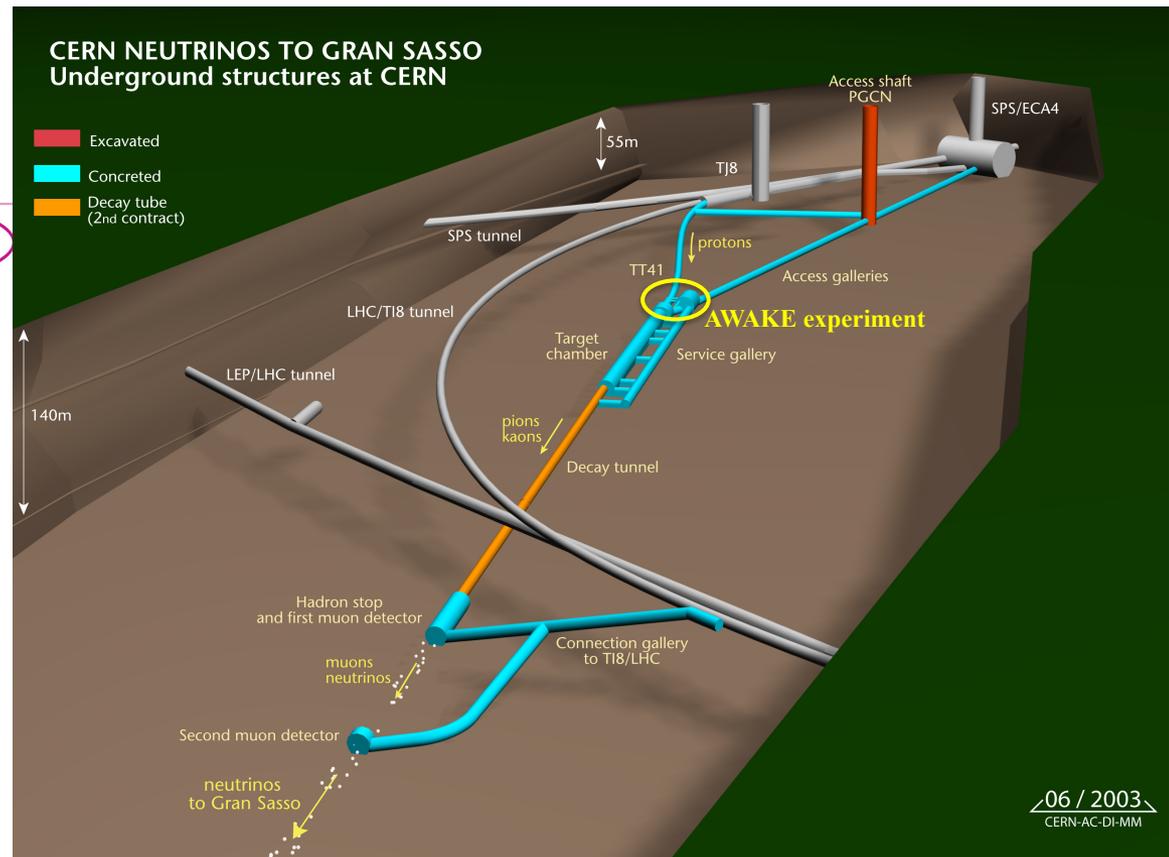
- An experiment to test the operation and characteristics of an active plasma lens.

# AWAKE: proton driven plasma wakefield at CERN

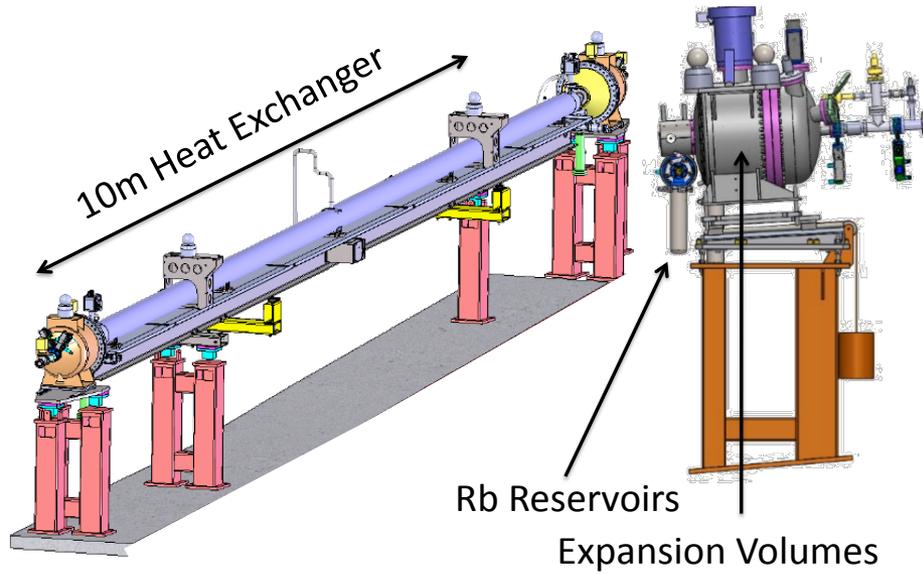
Department of Physics, UiO is member of AWAKE



**AWAKE is installed in CNGS Facility (CERN Neutrinos to Gran Sasso)**  
 → CNGS physics program finished in 2012



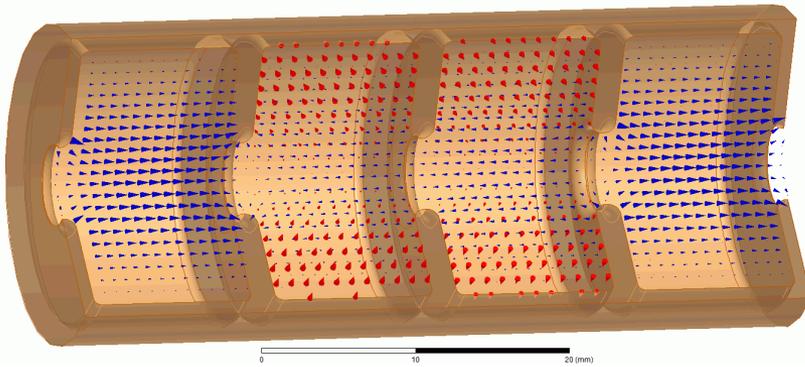
# The AWAKE experiment



# Summary

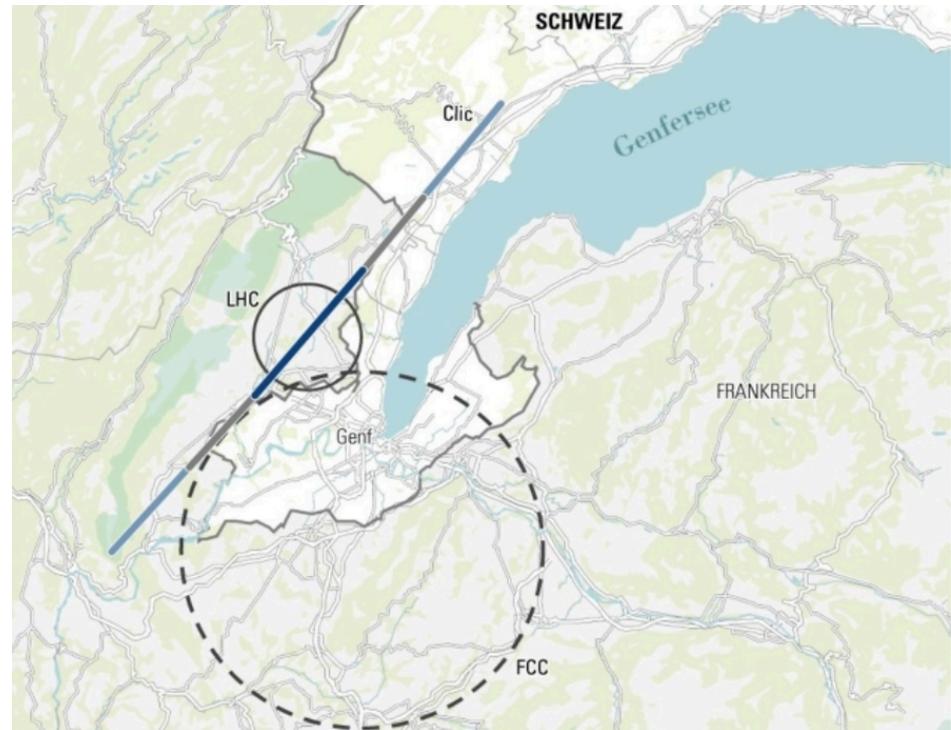
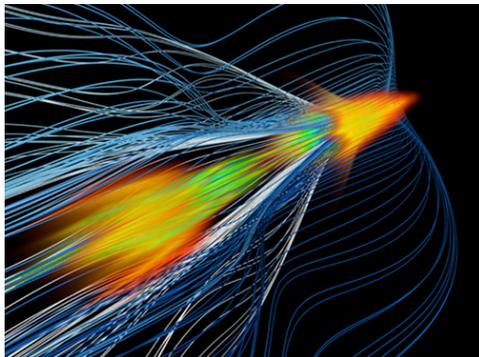


*The compact linear collider, CLIC*



*CLIC 100 MV/m accelerating structure*

*Plasma wave with accelerating fields*



*Size of possible future particle colliders, compared to the LHC*

Extra

# Advanced accelerator movies

Two-bunch:

<https://www.youtube.com/watch?v=N2lmtSk-rYE>

Positrons:

<https://www.youtube.com/watch?v=LVXj5hRyP8s>

Accelerator on a chip:

<https://www.youtube.com/watch?v=V89qvy8whxY>

AWAKE TEDX:

<https://www.youtube.com/watch?v=5Ryp6UTCeUo>

# The energy frontier: what machine to build next

	$T_0$		+5		+10		+15		+20		...	+26
ILC	0.5/ab 250 GeV			1.5/ab 250 GeV			1.0/ab 500 GeV	0.2/ab $2m_{top}$	3/ab 500 GeV			
CEPC	5.6/ab 240 GeV			16/ab $M_Z$	2.6 /ab $2M_W$						SppC =>	
CLIC	1.0/ab 380 GeV				2.5/ab 1.5 TeV				5.0/ab => until +28 3.0 TeV			
FCC	150/ab ee, $M_Z$	10/ab ee, $2M_W$	5/ab ee, 240 GeV		1.7/ab ee, $2m_{top}$			hh,eh =>				
LHeC	0.06/ab			0.2/ab		0.72/ab						
HE-LHC	10/ab per experiment in 20y											
FCC eh/hh	20/ab per experiment in 25y											

Project	Start construction	Start Physics (higgs)
CEPC	2022	2030
ILC	2024	2033
CLIC	2026	2035
FCC-ee	2029	2039 (2044)
LHeC	2023	2031

Proposed dates from projects

Would expect that technically required time to start construction is O(5-10 years) for prototyping etc.