Research-based Particle Physics

FYS5555 – FYS9555

Spring 2020 Eirik Gramstad, University of Oslo Collider Physics II

Hadron collisions at Tevatron and LHC, Parton distribution functions and parton-parton collisions, Physics results

High pT Physics at hadron colliders Modern Particle Physics, M. Thomson

Drell-Yan process: $q\bar{q} \rightarrow \mu^+\mu^-$

You calculated the process

 $e^+e^- \rightarrow \mu^+\mu^-$; $e^+e^- \rightarrow q\overline{q}$

• Corresponding cross section for $q \overline{q} \rightarrow \mu^+ \mu^-$

$$\sigma(q\bar{q} \rightarrow \mu^{+}\mu^{-}) = \frac{1}{N_{c}}Q_{q}^{2}\frac{4\pi\alpha^{2}}{3\hat{s}}$$

- N_c=3 accounts for conservation of color charge
 - Implying that of the 9 possible color combinations of the qqbar system, annihilation process only occurs for 3: rrbar, ggbar, bbbar
- Parton Distribution Functions
 - u-quark within proton with momentum fraction $x_1 \rightarrow x_1 + \delta x_1$
 - anti-u-quark within anti-proton with momentum fraction $x_2 \rightarrow x_2 + \delta x_2$
- CoM energy of hard process

$$\hat{\mathbf{s}} = (\mathbf{x}_1 \mathbf{p}_1 + \mathbf{x}_2 \mathbf{p}_2)^2 = \mathbf{x}_1^2 \mathbf{p}_1^2 + \mathbf{x}_2^2 \mathbf{p}_2^2 + 2\mathbf{x}_1 \mathbf{x}_2 \mathbf{p}_1 \cdot \mathbf{p}_2$$

$$\mathbf{p}_1^2 = \mathbf{p}_2^2 = \mathbf{m}_p^2 \approx 0 \Longrightarrow \hat{\mathbf{s}} \approx 2\mathbf{x}_1 \mathbf{x}_2 \mathbf{p}_1 \cdot \mathbf{p}_2 = \mathbf{x}_1 \mathbf{x}_2 \mathbf{s}$$

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$$p\overline{p} \rightarrow \mu^{+}\mu^{-} + X$$

$$d^{2}\sigma_{u} = Q_{u}^{2} \frac{4\pi\alpha^{2}}{9\hat{s}} u^{p}(x_{1}) dx_{1}\overline{u}^{p}(x_{2}) dx_{2}$$

$$\overline{u}^{p}(x) = u^{p}(x) = u(x)$$

$$d^{2}\sigma_{u} = \frac{4}{9} \frac{4\pi\alpha^{2}}{9\hat{s}} u(x_{1}) u(x_{2}) dx_{1} dx_{2}$$



 Accounting for (smaller) contribution from ubar from proton and u from anti-proton and contribution from ddbar annihilation:

$$d^{2}\sigma = \frac{4\pi\alpha^{2}}{9x_{1}x_{2}s} \left\{ \frac{4}{9} \left[u(x_{1})u(x_{2}) + \overline{u}(x_{1})\overline{u}(x_{2}) \right] + \left[d(x_{1})d(x_{2}) + \overline{d}(x_{1})\overline{d}(x_{2}) \right] \frac{1}{9} \right\} dx_{1}dx_{2}$$
$$d^{2}\sigma = \frac{4\pi\alpha^{2}}{9x_{1}x_{2}s} f(x_{1}, x_{2})dx_{1}dx_{2}$$

In terms of experimental observables:

Rapidity & invariant mass of di-muons

$$\boldsymbol{M}^2 = \hat{\boldsymbol{S}} = \boldsymbol{X}_1 \boldsymbol{X}_2 \boldsymbol{S}$$

$$y = \frac{1}{2} \ln \left(\frac{E_3 + E_4 + p_{3z} + p_{4z}}{E_3 + E_4 - p_{3z} - p_{4z}} \right) = \frac{1}{2} \ln \left(\frac{E_q + E_q + p_{qz} + p_{qz}}{E_q + E_q - p_{qz} - p_{qz}} \right)$$

$$p_q = \frac{\sqrt{s}}{2} (x_1, 0, 0, x_1) \quad ; \quad p_q = \frac{\sqrt{s}}{2} (x_2, 0, 0, -x_2)$$

$$\Rightarrow y = \frac{1}{2} \ln \left(\frac{(x_1 + x_2) + (x_1 - x_2)}{(x_1 + x_2) - (x_1 - x_2)} \right) = \frac{1}{2} \ln \left(\frac{x_1}{x_2} \right)$$
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$$\sum_{n=1}^{\infty} \mathbf{x}_{1} = \frac{\mathbf{M}}{\sqrt{\mathbf{s}}} \mathbf{e}^{\mathbf{y}} \quad ; \quad \mathbf{x}_{2} = \frac{\mathbf{M}}{\sqrt{\mathbf{s}}} \mathbf{e}^{-\mathbf{y}}$$

- Differential cross section: $dx_1 dx_2 \rightarrow dy dM$
 - Determination of the Jacobian matrix



$$d^2\sigma = \frac{4\pi\alpha^2}{9x_1x_2s}f(x_1,x_2)dx_1dx_2$$

$$d^2\sigma = \frac{4\pi\alpha^2}{9M^2s}f(x_1, x_2)\frac{2M}{s}dy dM$$

$$\frac{d^2\sigma}{dy\,dM} = \frac{8\pi\alpha^2}{9\,Ms^2}\,f(x_1,x_2)$$

- As in project 2
 - Z-exchange (and any other exchange, Z', ...) can be added
- Experimental distribution
 - CDF @ Tevatron (1989-2011), showing Z-resonance
 - ATLAS (a) LHC ($pp \rightarrow \mu^+ \mu^- + X$)



$pp \rightarrow e^+e^- + X$ at 8 TeV, ATLAS at LHC

Gluons and QCD

- See M. Thompson: chapter 10 on QCD
- Short summary on how to calculate QCD processes
- Fys5555-19-OcdProcesses

pp→jet-jet+X: qq→qq

- Example of hard QCD scattering
 - Contributing to 2-jet cross section
 - Back-to-back in transver plane (no p_{T})
 - Boost in the other view (momentum of colliding partons along beam axis)

Many other contributions, gg, qg, qqbar, ... (see later)

$$\begin{array}{c} \mathbf{q}\mathbf{q} \xrightarrow{\mathbf{g}} \mathbf{q}\mathbf{q}:\\ \hat{\mathbf{s}} = \mathbf{x}_1 \mathbf{x}_2 \mathbf{s} , \mathbf{Q}^2 = -\mathbf{q}^2 \end{array} \right\} \begin{array}{c} \mathbf{d}\sigma \\ \mathbf{d}\overline{\mathbf{Q}}^2 = \frac{4\pi\alpha_s^2}{9\mathbf{Q}^4} \left[1 + \left(1 - \frac{\mathbf{Q}^2}{\hat{\mathbf{s}}}\right)^2 \right] \end{array}$$

$$pp \to qq...: \frac{d\sigma}{dQ^2} = \frac{4\pi\alpha_s^2}{9Q^4} \left[1 + \left(1 - \frac{Q^2}{x_1 x_2 s}\right)^2 \right] g(x_1, x_2) dx_1 dx_2$$

$$g(x_1, x_2) = \left[u(x_1) u(x_2) + u(x_1) d(x_2) + d(x_1) u(x_2) + d(x_1) d(x_2) \right]$$

$$\frac{d^3\sigma}{dQ^2 dx_1 dx_2} = \frac{4\pi\alpha_s^2}{9Q^4} \left[1 + \left(1 - \frac{Q^2}{x_1 x_2 s}\right)^2 \right] g(x_1, x_2)$$

$$(\mathbf{Q}^2, \mathbf{X}_1, \mathbf{X}_2) \rightarrow (\mathbf{p}_T, \mathbf{y}_3, \mathbf{y}_4)$$



Exercise

- **10.6** The observed events in the process pp \rightarrow two-jets at the LHC can be described in terms of the jet p_T and the jet rapidities y_3 and y_4 .
 - (a) Assuming that the jets are massless, $E^2 = p_T^2 + p_z^2$, show that the four-momenta of the final-state jets can be written as

$$p_3 = (p_T \cosh y_3, +p_T \sin \phi, +p_T \cos \phi, p_T \sinh y_3),$$

$$p_4 = (p_T \cosh y_4, -p_T \sin \phi, -p_T \cos \phi, p_T \sinh y_4).$$

(b) By writing the four-momenta of the colliding partons in a pp collision as

$$p_1 = \frac{\sqrt{s}}{2}(x_1, 0, 0, x_1)$$
 and $p_2 = \frac{\sqrt{s}}{2}(x_2, 0, 0, -x_1),$

show that conservation of energy and momentum implies

$$x_1 = \frac{p_T}{\sqrt{s}}(e^{+y_3} + e^{+y_4})$$
 and $x_2 = \frac{p_T}{\sqrt{s}}(e^{-y_3} + e^{-y_4}).$

(c) Hence show that

$$Q^2 = p_{\rm T}^2 (1 + e^{y_4 - y_3}).$$

10.7 Using the results of the previous question show that the Jacobian

$$\frac{\partial(y_3, y_4, p_1^2)}{\partial(x_1, x_2, q^2)} = \frac{1}{x_1 x_2}.$$

Exercise

$$(Q^{2}, \mathbf{x}_{1}, \mathbf{x}_{2}) \rightarrow (\boldsymbol{p}_{T}, \boldsymbol{y}_{3}, \boldsymbol{y}_{4})$$
$$\boldsymbol{p}^{\mu} = (\boldsymbol{E}, \boldsymbol{p}_{x}, \boldsymbol{p}_{y}, \boldsymbol{p}_{z}) = (\boldsymbol{m}_{T} \cosh \boldsymbol{y}, \boldsymbol{p}_{T} \cos \boldsymbol{\phi}, \boldsymbol{p}_{T} \sin \boldsymbol{\phi}, \boldsymbol{m}_{T} \sinh \boldsymbol{y})$$

• m=o
$$\rightarrow$$
 m_T=p_T \Rightarrow $p_3 = (p_T \cosh y_3, p_T \cos \phi, p_T \sin \phi, p_T \sinh y_3)$
 $p_4 = (p_T \cosh y_4, p_T \cos \phi, p_T \sin \phi, p_T \sinh y_4)$

• Conservation of E/P $p_1 = \frac{\sqrt{s}}{2}(x_1, 0, 0, x_1)$; $p_2 = \frac{\sqrt{s}}{2}(x_2, 0, 0, -x_2)$

$$\begin{split} x_1 &= \frac{p_{\rm T}}{\sqrt{s}} (e^{+y_3} + e^{+y_4}) \\ x_2 &= \frac{p_{\rm T}}{\sqrt{s}} (e^{-y_3} + e^{-y_4}) \\ Q^2 &= p_{\rm T}^2 (1 + e^{y_4 - y_3}) \,, \end{split}$$

Exercise

$$(\mathbf{Q}^2, \mathbf{X}_1, \mathbf{X}_2) \rightarrow (\mathbf{p}_T, \mathbf{y}_3, \mathbf{y}_4)$$

$$\begin{split} x_1 &= \frac{p_{\rm T}}{\sqrt{s}} (e^{+y_3} + e^{+y_4}) \\ x_2 &= \frac{p_{\rm T}}{\sqrt{s}} (e^{-y_3} + e^{-y_4}) \\ Q^2 &= p_{\rm T}^2 (1 + e^{y_4 - y_3}) \,, \end{split}$$

$$dx_1 dx_2 dQ^2 = \frac{\partial(y_3, y_4, p_T^2)}{\partial(x_1, x_2, Q^2)} dp_T^2 dy_3 dy_4$$
$$= \frac{1}{x_1 x_2} dp_T^2 dy_3 dy_4$$

- Add all other contributions
 - 2-jet cross section!
 - Need higher orders QCD!





QCD matrix elements – point-like scattering of partons

	Process	$ A ^2$	Value at $\theta = \pi/2$
 Point-like partons have 	$q+q' \rightarrow q+q'$	$\frac{4}{9}[s^2 + u^2]/t^2$	2.22
Rutherford like	$q + q \rightarrow q + q$	$\frac{4}{9}[(s^2+u^2)/t^2+(s^2+t^2)/u^2]-\frac{8}{27}(s^2/ut)$	3.26
behavior	$q + \overline{q} \to q' + \overline{q}'$	$\frac{4}{9}[t^2+u^2]/s^2$	0.22
	$q + \overline{q} \to q + \overline{q}$	$\frac{4}{9}[(s^2+u^2)/t^2+(t^2+u^2)/s^2]-\frac{8}{27}(u^2/st)$	2.59
	$q + \overline{q} \to g + g$	$\frac{32}{27}[t^2 + u^2]/tu - \frac{8}{3}[t^2 + u^2]/s^2$	1.04
$\sigma \sim \pi(\alpha_1 \alpha_2) A ^2/s$	$g + g \to q + \overline{q}$	$\frac{1}{6}[t^2 + u^2]/tu - \frac{3}{8}[t^2 + u^2]/s^2$	0.15
	$g + q \rightarrow g + q$	$-\frac{4}{9}[s^2+u^2]/su+[u^2+s^2]/t^2$	6.11
 A ² ~ 1 at y=0 (θ=π/2). 	$g + g \rightarrow g + g$	$\frac{9}{2}[3-tu/s^2-su/t^2-st/u^2]$	30.4
	$q + \overline{q} \to \gamma + g$	$\frac{8}{9}[t^2+u^2]/tu$	
	$g + q \to \gamma + q$	$-\frac{1}{3}[s^2+u^2]/su$	
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Proton structure functions (se

- Assume proton is incoherent sum of "valence" u and d quarks, radiated gluons, and a "sea" of quark and anti-quark pairs.
- Proton quantum numbers satisfied if proton is bound state of u + u + d "valence" quarks.
- The "sea" can arise from radiation by the valence quarks and the antiquarks and subsequent gluon "splitting" or virtual decay into quark-antiquark pairs.
- "Hard" p_T , scales well above the binding energy scale, $P_T >> \Lambda_{QCD}$



- For large E_T/P_T, or short distances, the proton can be treated as containing partons defined by distribution "structure" functions.
- f(x) is the probability distribution to find a parton with momentum fraction x

$$\mathbf{x} = \frac{\mathbf{p}_{parton}}{\mathbf{p}_{proton}} \qquad \sqrt{\mathbf{s}} = \sqrt{(\mathbf{p}_{A} + \mathbf{p}_{B})^{2}} \\ \sqrt{\mathbf{s}} = \mathbf{x}_{1}\mathbf{x}_{2}\sqrt{\mathbf{s}}$$

Parton distribution functions

- Assume very weak binding of the u,u,d "valence" quarks in the proton \rightarrow all 3 quarks same velocity
 - x=p_{parton}/p_{proton} ~1/3 f(x) δ-function



But quarks are bound \rightarrow

$$\Delta x \Delta p_x \approx \hbar$$
$$\Delta x = 1 fm \rightarrow \Delta p_x = 0.2 GeV \approx \Lambda_{QCD}$$

- m_{a} ~5MeV \rightarrow relativistic system
 - valence quarks can radiate gluons (xg(x) ~ constant for small x)
 - gluons can split into q-qbar pairs (including strangeness with xs(x) ~ constant)
- The parton distribution is, in principle, calculable but not perturbatively
 - In practice measured in lepton-proton scattering

Proton structure functions - pictorial



Experimental determination of parton distribution functions

- In proton, u & d quarks have largest probability density at large x
 - residual memory of x~1/3 for valence quarks
 - reduction due to gluon emission
- Gluons and "sea" anti-quarks have large probability at low

Χ.

- gluons carry ~ 50% of proton momentum
- Simple parameterisations



Parton Distribution Functions

- Ultimately the parton distribution functions are obtained from a fit to all experimental data including e-p and e-n scattering, neutrino-nucleon scattering,
 - Hadron-hadron collisions also give information, especially on gluon pdf g(x)
 - different experimental measurements give access to different PDFs

Fit to all data: constraints imposed by theoretical QCD framework such as DGLAP evolution equations Note:



Experimental determination of parton distribution functions

- g dominates for x < 0.2</p>
- at large x, u dominates over d and g
- "sea" dominates for x < 0.03 over valence





Lines: different fits to experimental data Points: simple xg(x) parameterization

 $\mathbf{X}\mathbf{G}(\mathbf{X}) = \frac{7}{2}(1-\mathbf{X})^6$

- In CompHEP:
 - can run different distribution functions (MRST, CTEQ, ...) for same process.

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Structure functions and ep-collider HERA

- Parton distributions (xf(x,Q²)) are obtained from (QCD) fits to cross section of various measured processes (ep NC, CC, high PT jet production, charm production, ...)
 - And theoretical extrapolations, DGLAP evolution equations





Parton kinematics – overview





- The LHC data probe regions of the distribution functions which were not explored by fixed target and HERA experiments
- It is important to have a reliable set of verified PDF in order to model new physics and SM backgrounds.

F₂(x,Q²) structure function Results

★ No evidence of rapid decrease of cross section at highest Q²

 *R*_{quark} < 10⁻¹⁸ m

 ★ For x > 0.05, only weak dependence of *F*₂ on Q² : consistent with the expectation from the quark-parton model

 ★ But observe clear scaling violation

 But observe clear scaling violation at high and low values of x

$$F_2(x,Q^2) \neq F_2(x)$$



Proton-Proton Collisions at the LHC

- Measurements of structure functions not only provide a powerful test of QCD, the parton distribution functions are essential for the calculation of cross sections at pp and pp colliders.
- •Example: Higgs production at the Large Hadron Collider LHC
 - The HE-LHC will collide 7 TeV protons on 7 TeV protons
 - However underlying collisions are between partons
 - Higgs production at the LHC dominated by "gluon-gluon fusion"



- Cross section depends on gluon PDFs $\sigma(pp \to HX) \sim \int_0^1 \int_0^1 g(x_1)g(x_2)\sigma(gg \to H)dx_1dx_2$
- Uncertainty in gluon PDFs lead to a ±5 % uncertainty in Higgs production cross section
- Prior to HERA data uncertainty was ±25 %

Hadronic cross-sections

(see D. Green)

- $A+B \rightarrow 1+2+X \rightarrow M+X \rightarrow 3+4+X$
- Cross section is a convolution of matrix elements (ME) and parton distribution functions (PDF)



$$\sigma = \sum_{i,j} \int f_i^A(\mathbf{x}_1) f_j^B(\mathbf{x}_2) d\mathbf{x}_1 d\mathbf{x}_2 \hat{\sigma}_{ij}$$

$$d\sigma_{12} = f_1(\mathbf{x}_1) f_2(\mathbf{x}_2) d\mathbf{x}_1 d\mathbf{x}_2 d\hat{\sigma}(1+2 \rightarrow 3+4)$$

$$\sqrt{s} = \sqrt{(p_A + p_B)^2} = 2P$$

$$\sqrt{\hat{s}} = \sqrt{x_1 x_2 s} = M$$

$$\begin{vmatrix} x = x_1 - x_2 \\ \tau \equiv \frac{M^2}{s} = x_1 x_2 \end{vmatrix} x = 0 \Rightarrow \langle x \rangle = \sqrt{\tau} = \frac{M}{\sqrt{s}}$$

More 2-body kinematics

- 1+2→M→3+4
 - <x> to produce *tt* M~2m_t~350GeV

$$\begin{aligned} \mathbf{x} &= \mathbf{0} \Rightarrow \langle \mathbf{x} \rangle = \sqrt{\tau} = \frac{M}{\sqrt{s}} \\ \hline \textbf{Tevatron}(1.8) &: M = 2m_t \Rightarrow \langle \mathbf{x} \rangle \approx 0.194 \\ \textbf{LHC}(8/14) &: M = 2m_t \Rightarrow \langle \mathbf{x} \rangle \approx 0.044 / 0.025 \end{aligned}$$

- Higher x means higher M
 - To produce mass of 100 GeV with accelerator running at 14 TeV requires <x>=0.007
 - To produce mass of 5 TeV requires x = 0.36
- To produce M at zero rapidity
 - need partons with same x
- M at higher rapidities
 - one parton at higher x, the other one at smaller x

Hadronic cross-sections

- Values x₁ from A and x₂ from B picked out of probability distributions with the joint probability f₁f₂ to form a system of mass M moving with momentum fraction x
 - C is a color factor.
- Change of variable in order to express σ in terms of variables in final state
 - M and y measured → determine x₁ and x₂

$$\begin{split} d\sigma_{12} &= Cf_1(x_1)f_2(x_2)dx_1dx_2d\hat{\sigma}(1+2 \rightarrow 3+4) \\ dx_1dx_2 &= d\hat{s}/sdy = d\tau dy \\ \tau &= \hat{s}/s = M^2/s \\ d\sigma &= Cf_1(x_1)f_2(x_2)d\tau dy d\hat{\sigma}(1+2 \rightarrow 3+4) \\ y &= 0 \rightarrow x_1 = x_2 = \sqrt{\tau} \\ \left(d\sigma/d\tau dy \right)_{y=0} &= Cf_1(\sqrt{\tau})f_2(\sqrt{\tau})d\hat{\sigma}(1+2 \rightarrow 3+4) \end{split}$$

- On the rapidity plateau, the cross section can be estimated as $d\sigma \sim (d\sigma/dy)_{y=o}\Delta y$
- At fixed energy, value of ∆y varies only slowly with mass ~ ln(1/M)

$2 \rightarrow 2$ cross sections

- Estimate cross section
 - Change of variable
 τ→M
 - Consider $gg \rightarrow gg$

$$\begin{pmatrix} d\sigma/d\tau dy \end{pmatrix}_{y=0} = Cf_1(x_1)f_2(x_2)d\hat{\sigma}(1+2 \rightarrow 3+4) \\ \tau = \hat{s}/s = M^2/s \Rightarrow d\tau = 2MdM/s \\ gg \rightarrow gg : f(x) = g(x) \\ (sd\sigma/2MdMdy)_{y=0} = C[xg(x)]^2/x^2 (d\hat{\sigma}\hat{s}/M^2) \\ x^2 = M^2/s \\ M^3(d\sigma/dMdy)_{y=0} = 2C[xg(x)]^2(d\hat{\sigma}\hat{s}) \\ 2 \rightarrow 2: \\ M^3(d\sigma/dydM)_{y=0} = 2C[xf_1(x)xf_2(x)]_{x=\sqrt{\tau}}(d\hat{\sigma}\hat{s}) \\ d\hat{\sigma} \approx \pi\alpha_1\alpha_2/\hat{s} \\ M^4(d\sigma/dydM^2)_{y=0} \sim C[xf_1(x)xf_2(x)]_{x=\sqrt{\tau}}(\pi\alpha_1\alpha_2)$$

OCD matrix elements – point-like scattering of partons

		Process	$ A ^2$	Value at $\theta = \pi/2$
 Point-like partons have Rutherford like behavior 	$q + q' \rightarrow q + q'$	$\frac{4}{9}[s^2 + u^2]/t^2$	2.22	
	$q + q \rightarrow q + q$	$\frac{4}{9}[(s^2+u^2)/t^2+(s^2+t^2)/u^2]-\frac{8}{27}(s^2/ut)$	3.26	
	$q + \overline{q} \rightarrow q' + \overline{q}'$	$\frac{4}{9}[t^2+u^2]/s^2$	0.22	
	$q + \overline{q} \to q + \overline{q}$	$\frac{4}{9}[(s^2+u^2)/t^2+(t^2+u^2)/s^2]-\frac{8}{27}(u^2/st)$	2.59	
	$q + \overline{q} \rightarrow g + g$	$\frac{32}{27}[t^2+u^2]/tu-\frac{8}{3}[t^2+u^2]/s^2$	1.04	
σ~	$\cdot \pi(\alpha_1 \alpha_2) A ^2/S$	$g + g \rightarrow q + \overline{q}$	$\frac{1}{6}[t^2 + u^2]/tu - \frac{3}{8}[t^2 + u^2]/s^2$	0.15
	$g + q \rightarrow g + q$	$-\frac{4}{9}[s^2 + u^2]/su + [u^2 + s^2]/t^2$	6.11	
-	$ A ^2 \sim 1 \text{ at } y=0$	$g + g \rightarrow g + g$	$\frac{9}{2}[3-tu/s^2-su/t^2-st/u^2]$	30.4
(0-n/2).	$q + \overline{q} \to \gamma + g$	$\frac{8}{9}[t^2+u^2]/tu$		
		$g + q \rightarrow \gamma + q$	$-\frac{1}{3}[s^2+u^2]/su$	
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Low mass LHC rates – design numbers

- Total reaction rate
 - For small x and strong production, the cross section is a large fraction of the inelastic cross section.
 - Therefore, the probability to find a "small Pt "minijet" in an LHC crossing is not small.
- "Minijet" rate (see D. Green)

$$\sigma \sim 100 \ mb$$

 $L \sim 10^{34} / (cm^2 \sec)$
 $\Delta t \sim 25 \ n \sec$
 $\sigma L \sim 10^9 \ Hz$
 $< n_x > \sim 25 \ minbias \ events/ \ crossing$

$$M^{3}(d\sigma/dMdy)_{y=0} = 2[xg(x)]^{2}C(d\widehat{\sigma}\widehat{s})(\hbar c)^{2}$$

$$\Delta\sigma(M > M_{o}) \sim \Delta y[xg(x)]^{2}[\pi\alpha^{2} |A|^{2} / M_{o}^{2}]$$

$$xg(x) \sim 7/2, \Delta y \sim 10, \alpha_{s} \sim 0.1, C = 3$$

for $M_{o} = 10 \ GeV, |A|^{2} = 30 \ (gg \rightarrow gg)$

$$\Rightarrow \Delta\sigma \sim 1 \ mb$$

$$[\sigma] = [L^2] = \left\lfloor \frac{1}{M^2} \right\rfloor = \left\lfloor \frac{1}{s} \right\rfloor$$

$$(\hbar c)^2 = 0.4 (mb.GeV)^2, 1 mb = 10^{-27} cm^2$$

$2 \rightarrow 2$ decay kinematics



The measured values
 of y₃, y₄ and p_T allow to
 solve for x, M and the
 com decay angle,
 hence the initial state
 x₁ and x₂

$$x_{1} = [M / \sqrt{s}]e^{y}, y = (y_{3} + y_{4})/2$$
$$x_{2} = [M / \sqrt{s}]e^{-y}$$

$$y^* = (y_3 - y_4)/2$$
$$\cos\theta^* = \tanh(y^*)$$

gg→gg CompHEP

p_T>50 GeV
 σ=0.013 mb





- **Fixed mass**
 - kinematics: $x_1 x_2 = M^2/s = 0.01$

$2 \rightarrow 1$ Drell-Yan processes

- Resonance (Γ<<M)
 - Partial wave unitarity (D. Green)
 - Integrate over narrow width

$$\int \sigma ds = \pi^2 (2J+1)(\Gamma_{12}/M)$$

$$M^{2}(d\sigma/dy)_{y=0} = C[xf_{1}(x)xf_{2}(x)]_{x=\sqrt{\tau}}[\pi^{2}\Gamma_{12}(2J+1)/M]$$

$$\Gamma_{12}/M \sim \alpha_{12}''$$

$$M^{2}(d\sigma/dy)_{y=0} = C[xf_{1}(x)xf_{2}(x)]_{x=\sqrt{\tau}}[\pi^{2}\alpha_{12}(2J+1)]$$

 "scaling" behavior – cross section depends only on τ and not on M and s separately

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Hadronisation

- Quarks and gluons have color, while hadrons (the asymptotic states) are colorless.
- The process of "hadronization" occurs at energy scales where QCD is strong ~ Λ so that perturbation theory cannot be used.
- This makes direct experimental QCD predictions difficult.



Space

Simulation tools

- A "Monte Carlo" is (a usually) C++ program that generates events
- Events vary from one to the next (random numbers)
 - expect to reproduce both the average behavior and fluctuations of real data
- Event Generators may be
 - parton level:
 - Parton Distribution functions
 - Hard interaction matrix element
 - and may also handle:
 - Initial state radiation
 - Final state radiation
 - Underlying event
 - Hadronisation and decays
- Separate programs for Detector Simulation
 - GEANT most commonly used



A Monte Carlo event




★ Test QCD predictions by looking at production of pairs of high energy jets

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10 ⁷ $\frac{d^2\sigma}{dE_Td\eta}$ (fb/GeV) **QCD** Prediction 10 JETRAD Program 10 5 10 10^{3} $\theta = 62-90^{\circ}$ 10² 10 $\theta = 5.7 - 15^{\circ}$ 1 50 100 150 200 250 300 350 400 450 E_T (GeV)

p

Measure cross-section in terms of

- "transverse energy" $E_T = E_{\text{iet}} \sin \theta$
- "pseudorapidity" $\eta = \ln \left[\cot \left(\frac{\theta}{2} \right) \right]$

Do

Collaboration,

Phys.

Rev.

Lett.

86 (2001

★QCD predictions provide an

excellent description of the data over many orders of magnitude

*****NOTE:

- at low E_{τ} cross-section is dominated by low x partons i.e. gluon-gluon scattering
- at high E_{τ} cross-section is dominated by high x partons

i.e. quark-antiquark scattering

μ

500

Inclusive jet cross section at Tevatron

CDF and Do results









Initial, Final State Radiation

The initial state has ~ no transverse momentum.

Thus a 2 body final state is back-to-back in azimuth.

Take the 2 highest E_T jets.

- LO 3-jet calculation fails to describe very small or very large angle regions
- NLO 3-jet calculation (NLOJET++) does a pretty good job

HERWIG and PYTHIA (with some tuning) also describe the data





- To produce M at rapidity
 - y~0 need partons with same x
 - High y one parton at high x, the other at low x
- Di-jet event in 2 views
 - Back-to-back in transverse plane (no p_T)
 - Boost in the longitudinal view (net momentum of colliding partons along beam axis)



High mass di-jet





Measurement of inclusive jet and dijet cross-sections, ... At LHC

- Inclusive Jet cross sections
 - QCD works well and fits data over orders of magnitude!





Drell-Yan production of W/Z bosons

 $\overline{u} + u \rightarrow Z \rightarrow e^+ + e^-, \ \overline{u} + d \rightarrow W^- \rightarrow e^- + \overline{v}_e$

- Single production of W and Z bosons
- σ_W at the LHC, 10 times more than Tevatron



 $\sigma_{12} \approx \Gamma_{12} / M^3 \approx \alpha_{12} / M^2$

Cross section and width for W:

$$\sigma \sim \pi^2 \Gamma(2J+1)/M^3$$
, $\Gamma \sim 2$ GeV, $\sigma = 47$ nb.

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Z production A_{FB}



- Z couples to LH and RH quarks differently
- Leading to parity violating asymmetry in γ-Z interference.
- Age asymmetry sensitive to Z' arch-based particle physics E. Gramstad

W production at LHC





48

Z production at LHC





W-mass measurement by ATLAS

 Transverse mass: data vs simulation including signal and background contributions





 ATLAS present measurement of m_W compared to SM prediction from global electroweak fit [16] updated using recent measurements of m_t=172.84±0.70GeV [122] and m_H=125.09±0.24GeV [123], and to combined values of m_W measured at LEP [124] and at Tevatron collider [24]

SM Cross section measurements: 7, 8, 13 TeV





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ZZ-production

- Cross-section
 - Steep rise near threshold.
 - 20 fold rise from the Tevatron to the LHC
 - σ_{ZZ}~10pb at LHC
 - Possibility to investigate triple gauge boson coupling
- Not much gain in using anti-protons once the energy is high enough that the gluons or "sea" quarks dominate.



At o.4TeV: <x>~2M_Z/sqrt(s)~o.46 dominated by valence quarks (ppbar > pp)

At LHC: less than 2 difference between pp and ppbar Research-based particle physics - E. Gramstad

Di-Z-boson production at LHC





4-lepton invariant mass at 13 TeV













WW and WZ production







Top quark @ ATLAS ++

Ttbar, cross sections











13

√s [TeV]

8

Tevatron single top summary





Top mass measurements

ATLAS+CMS Preliminary LHCtop WG	m_{top} summary, $\sqrt{s} = 7-8 \text{ TeV}$	Sep 2015
World Comb. Mar 2014, [7]		
stat total uncertainty	total stat	
$m_{top} = 173.34 \pm 0.76 \ (0.36 \pm 0.67) \ GeV$	m _{top} ±total (stat±syst)	√s Ref.
ATLAS, I+jets (*)	172.31±1.55 (0.75±1.35)	7 TeV [1]
ATLAS, dilepton (*)	173.09±1.63 (0.64±1.50)	7 TeV [2]
CMS, I+jets	173.49±1.06 (0.43±0.97)	7 TeV [3]
CMS, dilepton	172.50±1.52 (0.43±1.46)	7 TeV [4]
CMS, all jets	173.49±1.41 (0.69±1.23)	7 TeV [5]
LHC comb. (Sep 2013)	173.29±0.95 (0.35±0.88)	7 TeV [6]
World comb. (Mar 2014)	173.34± 0.76 (0.36± 0.67)	1.96-7 TeV [7]
ATLAS, I+jets	172.33±1.27 (0.75±1.02)	7 TeV [8]
ATLAS, dilepton	173.79±1.41 (0.54±1.30)	7 TeV [8]
ATLAS, all jets	H 175.1±1.8 (1.4±1.2)	7 TeV [9]
ATLAS, single top	172.2±2.1 (0.7±2.0)	8 TeV [10]
ATLAS comb. (Mar 2015)	172.99±0.91 (0.48±0.78)	7 TeV [8]
CMS, I+jets	172.35±0.51 (0.16±0.48)	8 TeV [11]
CMS, dilepton	172.82±1.23 (0.19±1.22)	8 TeV [11]
CMS, all jets	172.32±0.64 (0.25±0.59)	8 TeV [11]
CMS comb. (Sep 2015)	172.44± 0.48 (0.13± 0.47)	7+8 TeV [11]
	[1] ATLAS-CONF-2013-046 [7] arXiv:1	403.4427
	[2] ATLAS-CONF-2013-077 [8] Eur.Ph	ys.J.C (2015) 75:330
	[3] JHEP 12 (2012) 105 [9] Eur.Phys.J.C75 (2015) 158	
(*) Superseded by results shown below the line	[4] Eur.Phys.J.C72 (2012) 2202 [10] ATLA	S-CONF-2014-055
	[5] Eur.Phys.J.C74 (2014) 2758 [11] CMS	PAS TOP-14-022
165 170 17	F 190	105
	5 100	105
m _{top} [GeV]		









(Statistical significance)

Plot number of events or cross section as function of chosen variable

- observed or measured (Data)
- expected "background" (SM or some established theory)
- o ratio observed/SM
- predicted by new physics theory



⊗ New Physics?

- Local probability p_o for a background-only experiment to be more signal-like than the observation as a function of new particle mass
- The higher the Significance, the lower the probability of background fluctuation



Mid-term evaluation

- Feedback most welcome
- Things to improve short-term
- Method
- Projects
- All-hands sessions & tools
- Lectures
- · ...

CERN visit

- See link to preparatory material
- go through the stuff before

Final Projects

See googledoc preparatory document

Higgs production and decay at LHC

f

V*=W*/Z*

~~~~ γ

vvvv 7

Brown y

0000000

0000000

t.

νννν γ

\_V=W/Z



- 125 GeV ... a rather good compromise
- 5/5 production processes
- ≥5 decay channels



.2020

## Higgs mechanism in SM

- For details about Higgs, see Djouadi's book: The Anatomy of Electro–Weak Symmetry Breaking:
  - The Higgs boson in the Standard Model
  - The Higgs bosons in the Minimal Supersymmetric Model

### Higgs couplings SM



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### Higgs decays to fermions and gauge bosons

$$\Gamma_{\rm Born}(H \to f\bar{f}) = \frac{G_{\mu}N_c}{4\sqrt{2}\pi} M_H m_f^2 \beta_f^3 \qquad \beta = (1 - 4m_f^2/M_H^2)^{1/2} \\ N_c = 3\,(1) \text{ for quarks (leptons)}$$

$$\Gamma(H \to VV) = \frac{G_{\mu}M_{H}^{3}}{16\sqrt{2}\pi} \,\delta_{V}\sqrt{1-4x} \left(1-4x+12x^{2}\right) \,, \quad x = \frac{M_{V}^{2}}{M_{H}^{2}}$$

 $\delta_W = 2$  and  $\delta_Z = 1$ 

 $\Gamma(H \to WW + ZZ) \sim 0.5 \text{ TeV} [M_H/1 \text{ TeV}]^3$ 



## Loop induced **Higgs decays**

$$\Gamma(H \to \gamma \gamma) = \frac{G_{\mu} \alpha^2 M_H^3}{128 \sqrt{2} \pi^3} \left| \sum_f N_c Q_f^2 A_{1/2}^H(\tau_f) + A_1^H(\tau_W) \right|^2$$

$$\begin{aligned} A_{1/2}^{H}(\tau) &= 2[\tau + (\tau - 1)f(\tau)]\tau^{-2} & \tau_{i} = M_{H}^{2}/4M_{i}^{2} \text{ with } i = f, W \\ A_{1}^{H}(\tau) &= -[2\tau^{2} + 3\tau + 3(2\tau - 1)f(\tau)]\tau^{-2} \end{aligned}$$

$$f(\tau) = \begin{cases} \arcsin^2 \sqrt{\tau} & \tau \le 1 \\ -\frac{1}{4} \left[ \log \frac{1 + \sqrt{1 - \tau^{-1}}}{1 - \sqrt{1 - \tau^{-1}}} - i\pi \right]^2 & \tau > 1 \end{cases}$$

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## The 125 GeV Higgs cake ...

#### Decays of a 125 GeV Standard-Model Higgs boson



## Higgs discovery?

 $H \rightarrow WW^* \rightarrow |_V|_V$ 



130

140

Events / 2 GeV

Events - Fitted bkg

300

200

100 0 100

-200 E

100

110







Η→ττ

H→bb



160

m<sub>γγ</sub> [GeV]

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#### Understanding of "background" is important

- Most of which is due to important physics at the heart of the gauge structure / symmetry of electroweak interaction
  - Higgs showed up between 2 relatively busy regions! 09.03.2020



### A new particle discovered

- Local probability p<sub>o</sub> for a background-only experiment to be more signal-like than the observation as a function of m<sub>H</sub>
- Combination of all channels
  - ττ and bb not all included yet



- 10σ signal @ M~125.5 GeV
- Probability of background fluctuation: ~10<sup>-23</sup>

Observed local p<sub>o</sub> as a function of the Higgs boson mass  $m_{\mu}$  for the  $\sqrt{s} = 7 \text{TeV}$ data(blue), the  $\sqrt{s}$ = 8TeV data (red) and their combination (black)


progressive significance(p0) plots



progressive significance(p0) plots



progressive significance(p0) plots

#### to the observed data (or higher)



#### 07/2011 EPS 12/2011 CERN Spring 2012 PRD

progressive significance(p0) plots



progressive significance(p0) plots



progressive significance(p0) plots



progressive significance(p0) plots





- Decays to fermions difficult channels with high background – are a priority, especially bb (B~57%!)
- Searches for rare decays started: Zγ, μμ, .... Hidden decays, ...
- Reduced coupling consistent with SM

- Measurements of the signal strength parameter µ for m<sub>H</sub> =125.36 GeV for the individual channels and their combination
- Combination of all channels
- Consistency with SM: 1.18<sup>+0.15</sup>-0.14
- Quantum numbers consistent with Scalar: J<sup>PC</sup>=0<sup>++</sup>



# Higgs to Fermions and bosons



# Higgs boson mass



## Cross sections time branching fraction

- Cross sections time branching fraction for the main Higgs production modes at the LHC (ggF, VBF, VH and ttH+tH) in each relevant decay mode (γγ, WW, ZZ, ττ, bb).
- All values normalized to SM predictions
- In addition, combined results for each production cross-section are also shown, assuming SM values for the BRs into each decay mode

| ATLAS Preliminary                                        | Stat   | <u> </u>           | Svst.           | I SN            |
|----------------------------------------------------------|--------|--------------------|-----------------|-----------------|
| $\sqrt{s} = 13 \text{ TeV}, 24.5 - 79.8 \text{ fb}^{-1}$ | Otat.  |                    |                 | - 01            |
| $m_H = 125.09 \text{ GeV},  y_H  < 2.5$                  |        |                    | _               | _               |
| P <sub>SM</sub> = 7178                                   |        | Total              | Stat.           | Syst.           |
| ggFγγ 🚔                                                  | 0.96   | ±0.14 (            | $\pm \; 0.11$ , | +0.09<br>-0.08) |
| ggF ZZ 🙀                                                 | 1.04   | +0.16<br>-0.15 (   | $\pm  0.14$ ,   | $\pm 0.06$ )    |
| ggF WW 📥                                                 | 1.08   | ±0.19 (            | $\pm 0.11,$     | ±0.15)          |
| ggFττ μ <b>μαρι</b> μ                                    | 0.96   | +0.59<br>-0.52 (   | +0.37<br>-0.36, | +0.46<br>-0.38) |
| ggF comb.                                                | 1.04   | ± 0.09 (           | $\pm \ 0.07$ ,  | +0.07<br>-0.06) |
| VBF γγ H                                                 | 1.39   | +0.40<br>-0.35 (   | +0.31<br>-0.30, | +0.26<br>-0.19) |
| VBF ZZ                                                   | 2.68   | +0.98<br>-0.83 (   | +0.94<br>-0.81, | +0.27)          |
| VBF WW                                                   | 0.59   | +0.36<br>-0.35 (   | +0.29<br>-0.27, | ± 0.21 )        |
| VBF ττ ι                                                 | 1.16   | +0.58<br>-0.53 (   | +0.42<br>-0.40, | + 0.40 )        |
| VBF bb                                                   | 3.01   | + 1.67<br>- 1.61 ( | +1.63<br>-1.57, | +0.39<br>-0.36) |
| VBF comb.                                                | 1.21   | +0.24<br>-0.22 (   | +0.18<br>-0.17, | +0.16<br>-0.13) |
| VH γγ 📫                                                  | 1.09   | +0.58<br>-0.54 (   | +0.53<br>-0.49, | +0.25<br>-0.22) |
| VH ZZ                                                    | 0.68   | + 1.20<br>- 0.78 ( | +1.18<br>-0.77, | +0.18 )         |
| VH bb 📕                                                  | 1.19   | +0.27<br>-0.25 (   | +0.18<br>-0.17, | +0.20 )         |
| VH comb.                                                 | 1.15   | +0.24<br>-0.22 (   | ±0.16,          | +0.17<br>-0.16) |
| ttH+tH γγ 📻                                              | 1.10   | +0.41<br>-0.35 (   | +0.36           | +0.19<br>-0.14) |
| ttH+tH VV                                                | 1.50   | + 0.59<br>- 0.57 ( | +0.43           | +0.41 )         |
| ttH+tH ττ μ                                              | 1.38   | + 1.13<br>- 0.96 ( | +0.84<br>-0.76, | + 0.75          |
| ttH+tH bb                                                | 0.79   | +0.60              | $\pm \ 0.29$ ,  | ± 0.52 )        |
| <i>ttH</i> + <i>tH</i> comb. ➡                           | 1.21   | +0.26<br>-0.24 (   | ±0.17,          | +0.20 )         |
|                                                          |        |                    | 1 1             |                 |
| 2 0 2 4                                                  | 4      | 6                  |                 | 8               |
| Parameter norm                                           | alized | to S               | SM <sup>,</sup> | valu            |

### ttH signal in diphoton invariant mass spectrum



- Assume theoretical prediction, at 139 fb<sup>-1</sup>, LHC should have produced
- ~ 7,000,000 Higgs bosons
- ~ 70,000 via ttH production
- ~ 160 in the ttHγγ channel ATLAS





The signal strength (obs/SM) is measured to be  $\mu_{t\bar{t}H} = 1.38 \stackrel{+0.41}{_{-0.36}} = 1.38 \stackrel{+0.33}{_{-0.31}} (\text{stat.}) \stackrel{+0.13}{_{-0.11}} (\text{exp.}) \stackrel{+0.22}{_{-0.14}} (\text{theo.})$ 

# Higgs cross-section at LHC



### Is the new boson a Higgs?

- Measure its quantum numbers! Spin, parity, c-parity: J<sup>PC</sup>=? If Higgs: o<sup>++</sup>
- Decay angle of  $H \rightarrow \gamma \gamma$ 
  - Expected



### data (background not subtracted)



- "The hypothesis of a spin-2 particle (Graviton-like) produced by gluon fusion is excluded at 99% CL"

- Spin 1 cannot decay to  $\gamma\gamma$   $\Box$ 

## Is the new boson a Higgs?

- Define production & decay angle for  $H \rightarrow ZZ \rightarrow 4I$ 
  - Beam axis in the lab frame, the Z<sub>1</sub> and Z<sub>2</sub> in X rest frame and leptons in their corresponding parent rest frames

Likelihood
ratio for
various
hypotheses





- Higgs-like boson found to be compatible with SM expectation of o<sup>+</sup> when compared pair-wise with o-, 1+, 1-, 2+, and 2-
- o<sup>-</sup> and 1<sup>+</sup> states are excluded at the 97.8% C.L.
- WW analysis leads to similar conclusions

# Any New Physics out there?

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## 8.2 TeV-Mass di-jet event



Run: 305777 Event: 4144227629 2016-08-08 08:51:15 CEST

### What & How?

- Heavy gauge bosons, Z' and W',
  - From higher symmetry (e.g. E6) breaking, and more
- Composite models for quarks, q\*, and leptons, l\*
  - with substructure scale  $\Lambda$
- Randal-Sundrum gravitons, G\* and
- G<sup>\*</sup><sub>bulk</sub>, from warped extra dimensions
- Low-scale strings with large EDs,
  - and TeV<sup>-1</sup> Kaluza-Klein excitations of ©/Z
- Technicolor, Chiral bosons (W\*/Z\*)
- Quantum black holes, ADD, Contact Interactions (non resonant) ...



- "Simple"
  - ΙΙ, γγ, ΖΖ, WW, …
- Traditional
  - Jets or Rutherford Hammer method
  - Missing
- Mix

- "Leptons-quarks-gauge bosons-missing"
- Innovate
  - "Lepton-jets"

### New phenomena in di-jets

- New physics
  - new particles could be produced,
  - new interactions between particles could manifest themselves,
  - interactions resulting from the unification of SM with gravity could appear in the TeV range
  - probe the structure of the fundamental constituents of matter at the smallest distance scales
    - Modification of di-jet mass and angular distributions
    - experimental test of the size of quarks, excited quarks

## **Di-jet invariant mass**





### Search for new phenomena in dijet mass and angular distributions

- Di-jet production dominated by t-channel gluon exchange
  - Steeply falling di-jet mass



Standard Model QCD background

► 
$$f(z) = p_1 (1-z)^{p_2} / z^{p_3}$$
:  $z = m_{jj} / \sqrt{s}$ 

 Angular distributions, b-quark jets (appendix)



### Di-jet results at 13 TeV



### Search for new phenomena in dijet angular distributions

- Di-jet production dominated by tchannel gluon exchange
  - ➤Angular distribution peaked at |cosθ<sup>\*</sup>|=1
- Variable χ=e<sup>2|y\*|</sup> ~ (1+cosθ\*)/(1-cosθ\*) in bins of m<sub>ii</sub> y\*=(y<sub>3</sub>-y<sub>4</sub>)/2
- Sensitivity to BSM scenarios
  - Contact interaction excited quarks
  - ➢ Quantum Black Hole
  - ➤ Extended gauge sector (W', Z')





#### Search for new phenomena in dijet mass and angular distributions



## New di-lepton resonances?



