

Cyclotron 2

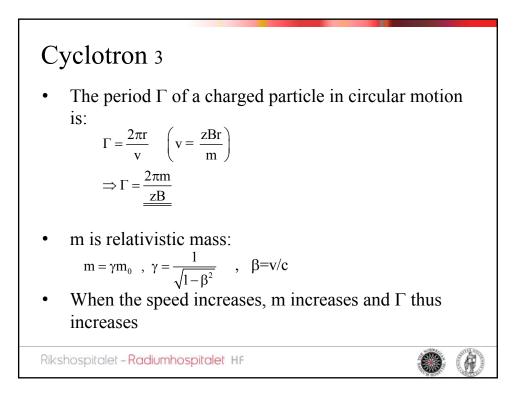
- Particle is kept in circular trajectory with B-field, and accelerated by time depending potential (kV/MHz)
- Potential V gives: $T=zV=\frac{1}{2}mv^2 \Rightarrow v^2 = \frac{2zZ}{m}$
- Combined with the Lorentz force: $(\vec{F}=z\vec{v}\times\vec{B})$

$$|F| = zvB = ma = \frac{mv^2}{r} \Rightarrow v^2 = \left(\frac{zBr}{m}\right)$$
$$\frac{2zV}{m} = \left(\frac{zBr}{m}\right)^2 \Rightarrow r^2 = \frac{2mV}{zB^2}$$

- Stronger magnetic field: implicitly higher acceleration

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Cyclotron 4

• Energy considerations:

$$T_{a} = T_{b} + zV \quad \left(V = \int \vec{E} \cdot d\vec{l} \quad , \ T = (\gamma - 1)m_{0}c^{2}\right)$$

$$\Rightarrow (\gamma_{a} - 1)m_{0}c^{2} = (\gamma_{b} - 1)m_{0}c^{2} + zV$$

$$\Rightarrow \gamma_{a} = \gamma_{b} + \frac{zV}{m_{0}c^{2}}$$

$$\Rightarrow \Gamma = \frac{2\pi m}{zB} = \frac{2\pi \gamma_{a}m_{0}}{zB} = \frac{2\pi m_{0}}{zB} \left(\gamma_{b} + \frac{zV}{m_{0}c^{2}}\right)$$

Cyclotron 4 Increase in period: ~zV/m₀c² Example: zV = 100 keV Proton: zV/m₀c² ~ 0.01 % Electron: zV/m₀c² ~ 20 % → close to 50 % rise in one round → Time dependent E-field will have the wrong direction relative to velocity of electron The E-field frequency can be synchronized with the rise in period → synchrocyclotron / synchrotron

