

## I. PROBLEM SESSION 3

### A. Problem 3.1

Cohesive energy of bcc and fcc neon:

Using the Lennard Jones potential, calculate the ratio of the cohesive energies of neon in the bcc and fcc structures ( $Ans = 0.958$ ). The lattice sums for the bcc structure are  $\sum_j' p_{ij}^{-12} = 9.11418$   $\sum_j' p_{ij}^{-6} = 12.2533$ .

### B. Problem 3.2

Solid molecular hydrogen:

For  $H_2$  one finds from measurements on the gas that the Lennard-Jones parameters are  $\epsilon = 50 * 10^{-16}$ erg and  $\sigma = 2.96\text{\AA}$ . Find the cohesive energy in kJ per mole of  $H_2$ , do the calculation for an fcc structure. Treat each  $H_2$  molecule as a sphere.

The observed cohesive energy is  $0.751\text{kJ/mol}$ , much less than calculated from our simple model. Thus quantum corrections should be important.

### C. Problem 3.3

-Recall the definition of the stress tensor,  $\hat{\sigma} = \sigma_{ij}$ .

-How can the force acting on a unit area with normal vector  $\vec{n}$  be expressed through  $\hat{\sigma}$ .

-Let us rotate the coordinate frame by an angle  $\alpha$  in the  $xy$  plane. Find how the stress tensor  $\hat{\sigma}$  is transformed.

-Show that the trace ( $\sum_i \sigma_{ii}$ ) of this tensor has not changed.

Define the deformation tensor  $\epsilon_{ik}$  through the displacement vector  $\vec{u}(\vec{r})$ . Why does only the symmetric component enter? What is the physical meaning of  $(\delta u_i / \delta x_k - \delta u_k / \delta x_i)$ ?

### D. Problem 3.4

-Recall the general relationship between the strain tensor  $\epsilon_{ik}$ , and the stress tensor,  $\sigma_{ik}$ .

-How does this relation look for an elastic medium? How many elastic constants enter this relationship?

-Explain the meaning of the Young's modulus  $E$ , the shear modulus,  $G$ , and the Poisson ratio,  $\nu$ . How can these quantities be measured experimentally?