

# **FYS3410 - Vår 2016 (Kondenserte fasers fysikk)**

**<http://www.uio.no/studier/emner/matnat/fys/FYS3410/v16/index.html>**

**Pensum: Introduction to Solid State Physics  
by Charles Kittel (Chapters 1-9 and 17, 18, 20)**

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# 2016 FYS3410 Lectures (based on C.Kittel's Introduction to SSP, Chapters 1-9, 17,18,20)

## Module I – Periodic Structures and Defects (Chapters 1-3, 20)

M18/1: 9-12 am	Introduction. Crystal bonding. Periodicity and lattices, Brag diffraction and Laue condition, reciprocal space	3h
<i>W20/1 cancelled</i>		
M25/1: 9-12 am	Ewald construction, interpretation of a diffraction experiment , Brag planes, and Brillouin zones	3h
<i>W27/1 cancelled</i>		
M01/2: 10-12 am	Elastic strain and structural defects in crystals	2h
W03/2: 9-10 am	Atomic diffusion in solids	1h
M08/2: 10-12 am	Summary of Module I	2h

## Module II – Phonons (Chapters 4 and 5)

W10/2: 9-10 am	Vibrations in monoatomic and diatomic chains of atoms	1h
M15/2: 10-12am	Periodic boundary conditions, phonons and density of states (DOS)	2h
W17/2: 9-10 am	Planck distribution	1h
M22/2 : 10-12am	Lattice heat capacity: Dulong-Petit, Einstein, and Debye models	2h
<i>W24/2 cancelled</i>		
M29/2: 9-12am	Comparison of different models for lattice heat capacity, thermal conductivity with phonons	3h
W02/3: 9-10 am	Thermal expansion	1h
M07/3: 10-12am	Summary of Module II.	2h

## Module III – Electrons (Chapters 6, 7, 18 - pp.528-530, and Appendix D)

W09/3: 9-10 am	Free electron gas (FEG) versus free electron Fermi gas (FEFG)	1h
M14/3: 10-12am	DOS of FEFG in 3D. Effect of temperature – Fermi-Dirac distribution	2h
W16/3: 9-10 am	Heat capacity of FEFG in 3D	1h
W30/3: 9-10 am	DOS in 2D - quantum wells	1h
M04/4: 10-12am	DOS in 1D and 0D, i.e. quantum wires and quantum dots; transport properties of electrons	2h
W06/4: 9-10 am	Origin of the energy band gap	
M11/4: 10-12am	Nearly free electron model. Kronig-Penney model. Empty lattice approximation.	2h
W13/4: 9-10 am	Number of orbitals in a band	1h
M18/4: 10-12am	Summary of Module III.	2h

## Module IV – Semiconductors and interfaces (Chapters 8, 9-pp 223-231, 17)

W20/4: 9-10 am	Metals versus semiconductors. Surfaces and interfaces.	1h
M25/4: 9-12 am	Effective mass method.	3h
W27/4: 9-10 am	Intrinsic carrier generation – electrons and holes.	1h
M02/5: 9-12 am	Localized levels for hydrogen-like impurities – donors and acceptors. Doping.	3h
W04/5: 9-10 am	Carrier statistics in semiconductors	1h
M09/5: 9-12 am	p-n junctions	3h
W11/5: 9-10 am	Optoelectronic semiconductor properties and devices	1h
M18/5: 9-12 am	Device demonstrations. Summary of Module IV	3h

## Repetition

M23/5 9-12 am	The course in a nutshell	2h
<i>W25/5, M30/5 and W1/6 cancelled</i>		

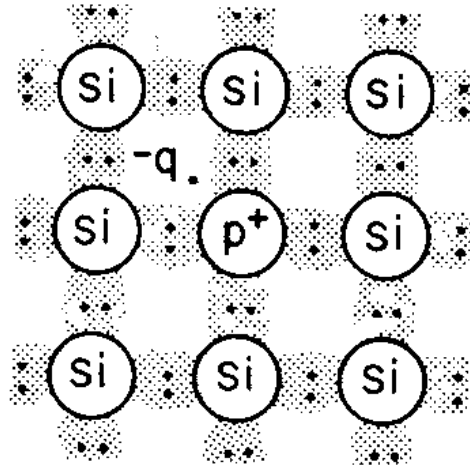
Exam during week 22 (tentatively 30-31/5)

**Lecture 27/4/2016**

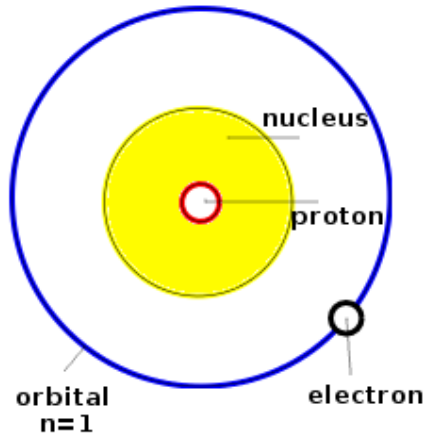
**Effective mass method**

**for hydrogen-like impurities in semiconductors**

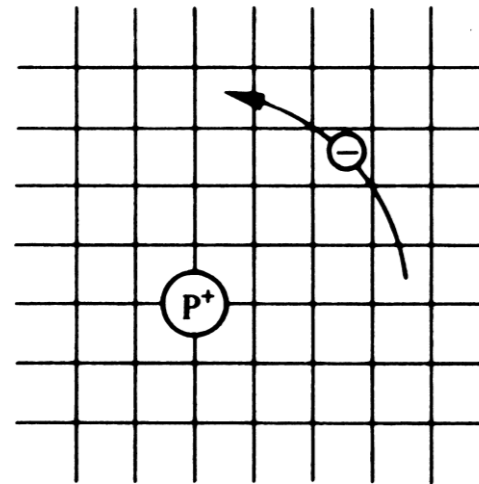
# Hydrogen like impurities in semiconductors



**P donor in Si can be modeled as hydrogen-like atom**



**Hydrogen atom**



**Hydrogen-like donor**

# Hydrogen atom - Bohr model

$$\frac{1}{4\pi\epsilon_0} \frac{Ze^2}{r^2} = m \frac{v^2}{r} \quad \text{for } L = mvr = n\hbar, n = 1, 2, 3, \dots$$

$$\Rightarrow Ze^2 = 4\pi\epsilon_0 mv^2 r = 4\pi\epsilon_0 mr \left(\frac{n\hbar}{mr}\right)^2 = 4\pi\epsilon_0 \frac{n^2 \hbar^2}{mr}$$

$$\Rightarrow r = 4\pi\epsilon_0 \frac{n^2 \hbar^2}{mZe^2}$$

$$\Rightarrow v = \frac{n\hbar}{mr} = \frac{1}{4\pi\epsilon_0} \frac{Ze^2}{n\hbar}$$

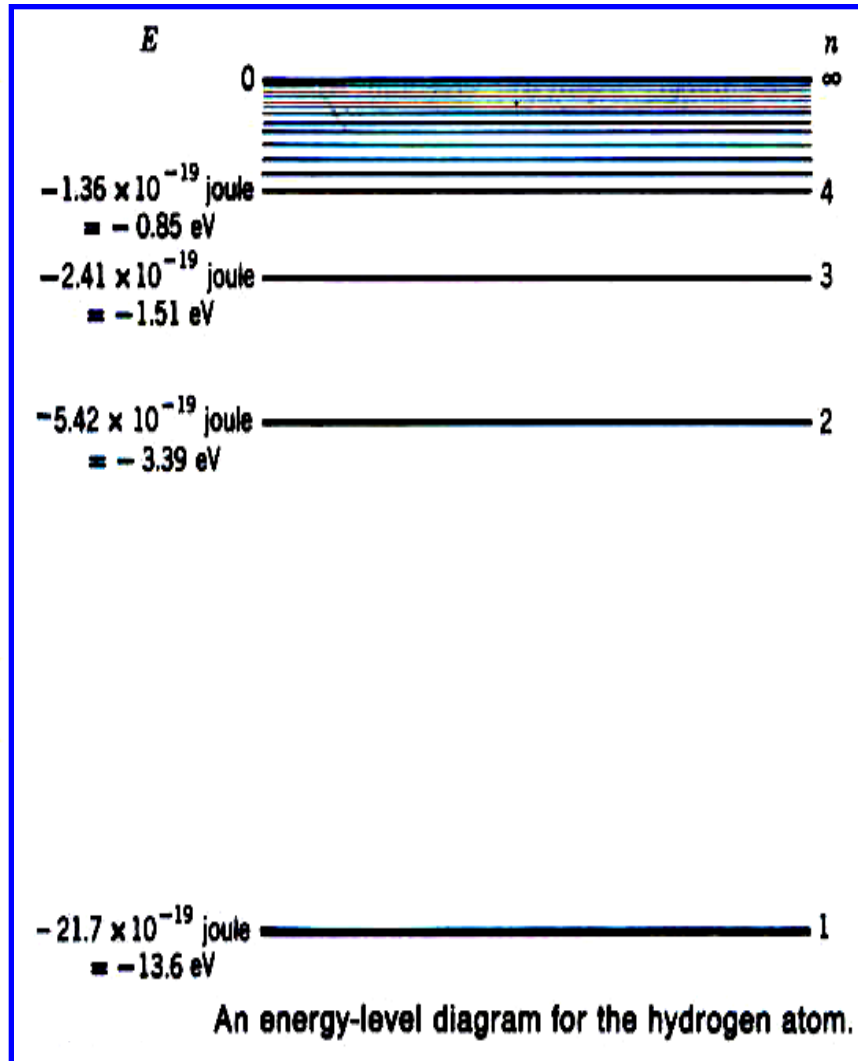
$$\text{Potential energy: } V = -\int_r^\infty \frac{Ze^2}{4\pi\epsilon_0 r^2} dr = -\frac{Ze^2}{4\pi\epsilon_0 r}$$

$$\text{Kinetic energy: } K = \frac{1}{2} mv^2 = \frac{Ze^2}{4\pi\epsilon_0 2r}$$

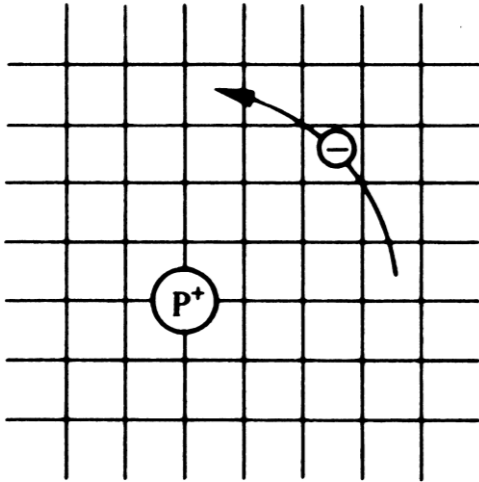
$$\text{Total energy: } E = K + V = -\frac{Ze^2}{(4\pi\epsilon_0)^2 2r} = -K \Rightarrow E = -\frac{mZ^2 e^4}{(4\pi\epsilon_0)^2 2\hbar^2} \frac{1}{n^2}$$

# Hydrogen atom - Bohr model

$$E_H = -\frac{m_0 q^4}{2(4\pi\epsilon_0\hbar)^2} = -13.6 \text{ eV}$$



# Hydrogen like impurities in semiconductors



**Hydrogen-like donor**

Instead of  $m_0$ , we have to use  $m_n^*$ .  
Instead of  $\epsilon_0$ , we have to use  $K_s \epsilon_0$ .

$K_s$  is the relative dielectric constant  
of Si ( $K_{s, Si} = 11.8$ ).

$$E_H = -\frac{m_0 q^4}{2 (4\pi \epsilon_0 \hbar)^2} = -13.6 \text{ eV}$$

$$E_d = -\frac{m_n^* q^4}{2 (4\pi K_s \epsilon_0 \hbar)^2} = -13.6 \text{ eV} \frac{m_n^*}{m_0} \left( \frac{\epsilon_0}{K_s \epsilon_0} \right)^2 \approx -0.05 \text{ eV}$$