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# INF-GEO 4310 Imaging

## Introduction

Sverre Holm



# Short description

- Since time immemorial man has done imaging using his senses. Modern technology now gives us new opportunities for imaging.
- Examples are the human body, the surface of the earth, the sea floor, or oil reservoirs under the sea floor. Imaging is the science of creating images in different media and with different methods.
- This course uses simple laboratory exercises and problem solving to introduce various imaging methods. The emphasis is on explaining basic principles.
- In addition the course will survey the similarities between methods, and show how simple physical principles are used to create various forms of images.



# What will you learn?

The objective is to give an introduction to imaging:

- Get a cross-disciplinary understanding of imaging.
- Know the various physical principles for imaging and how they are used in various applications.
- Get a practical introduction to imaging through laboratory exercises
- Examples of applications that will be covered are:
  - optical imaging (sight, binoculars, telescope, earth observation satellites),
  - radar
  - imaging in medicine with computer tomography (CT), magnetic resonance (MR), positron emission tomography (PET) and ultrasound
  - imaging of the sea floor and fish using sonar
  - seismology for mapping of earthquakes
  - mapping of oil reservoirs with seismics



# The course builds on

- MAT1100 - Calculus
- INF1000 – Basic programming
  - or INF1100 – Basic programming for scientific applications



# Imaging

- <http://www.uio.no/studier/emner/matnat/ifi/INF-GEO4310/>
- Lectures:  
Thursday 09:15 -12:00
- Problem solving:  
Wednesday 10:15-12:15
  - Problems based on e.g. exams from previous years



# Topics per week

- Introduction
- Geometrical optics I
- Geometrical optics II
- Radar
- Remote sensing I
- Remote sensing II
- Sonar
- Medical Ultrasound
- Acoustic Imaging
- Seismics I
- Seismics II
- Seismology
- Medical: CT, MR
- Summing it all up



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# Problem solving

- Some mandatory exercises:
  - Geometrical optics
  - Remote sensing
  - Sonar
  - Ultrasound
  - Seismics/seismology
- Excursions
  - Medical Ultrasound (GE Vingmed Ultrasound)
  - Medical imaging (Interventional Centre)
- Most of the remaining Wednesdays will be used for problem solving





# Orion's Belt

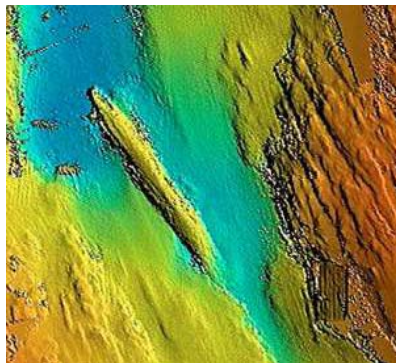
- Den ene av de 4 veggskiverelieffene, "Orions belte", til Bård Breivik som skal monteres i IF12 er fremvist under Beijing Biennale i National Art Museum of China nå under OL. Verket måler omlag 6 x 7 meter og skal etter utstillingen skipes til Norge og lagres i påvente av montering i IF12.
- Vi har fått rapporter fra nordmenn som har sett utstillingen i Beijing at verket fremstår som det mest imponerende og bemerkelsesverdige på hele den internasjonale utstillingen.
- Det blir totalt 4 slike verk på IF12 og flere av dem er utformet i samarbeid med DSB-gruppen – Fritz Albregtsen
- Jeg vedlegger et foto fra Beijing som er tatt av en bekjent av IF12-arkitekten. Det finnes også et lite foto med selveste Sonja foran verket på UDs nettside her:
- <http://www.norway.cn/culture/Exhibitions/The+Queen+of+Norway+enjoys+art+in+Beijing.htm>





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# Kongsberg Multibeam Echosounder



German warship Blücher, Oslofjord



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# Synthetic aperture sonar: Hugin



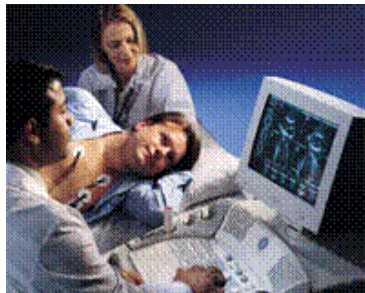
FFI & Kongsberg Maritime



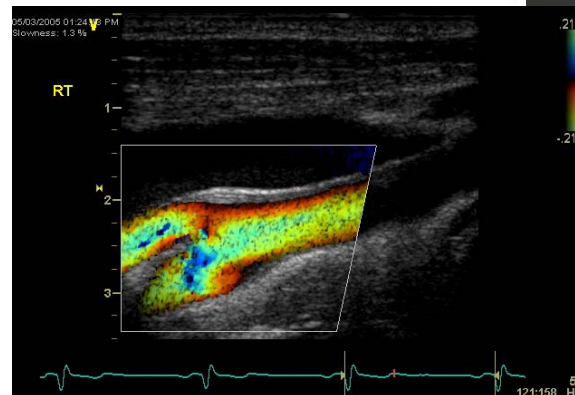
# GE Vingmed Ultrasound



4-chamber cardiac image



DEPARTMENT OF INFORMATICS

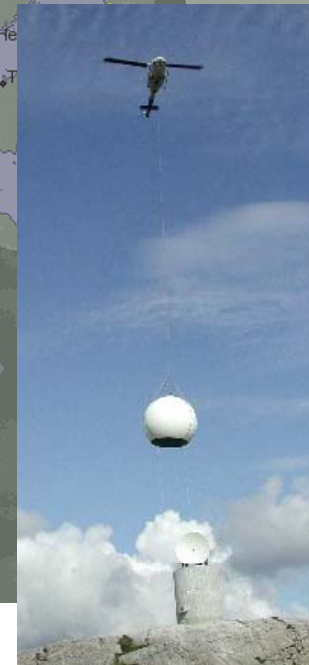
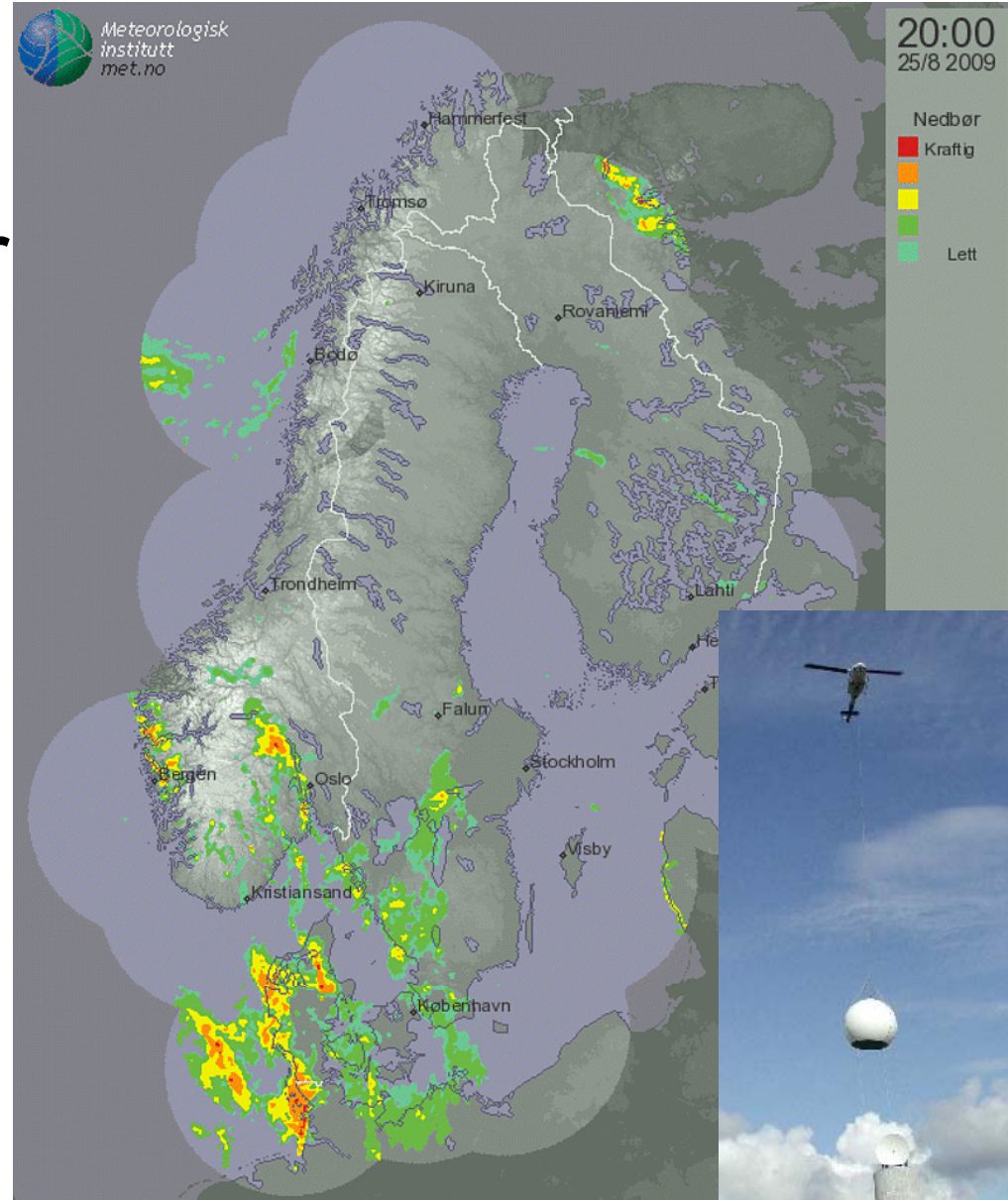


Blood flow in the carotid artery  
(neck) with bifurcation



# Weather radar

- [www.yr.no](http://www.yr.no)
- Nordic network
- Both observation of backscatter (rain) and Doppler shift, i.e. wind speed and direction
- Radius of coverage is 240 km.
- Typically:  $\lambda=10$  cm, S-band (3 GHz)





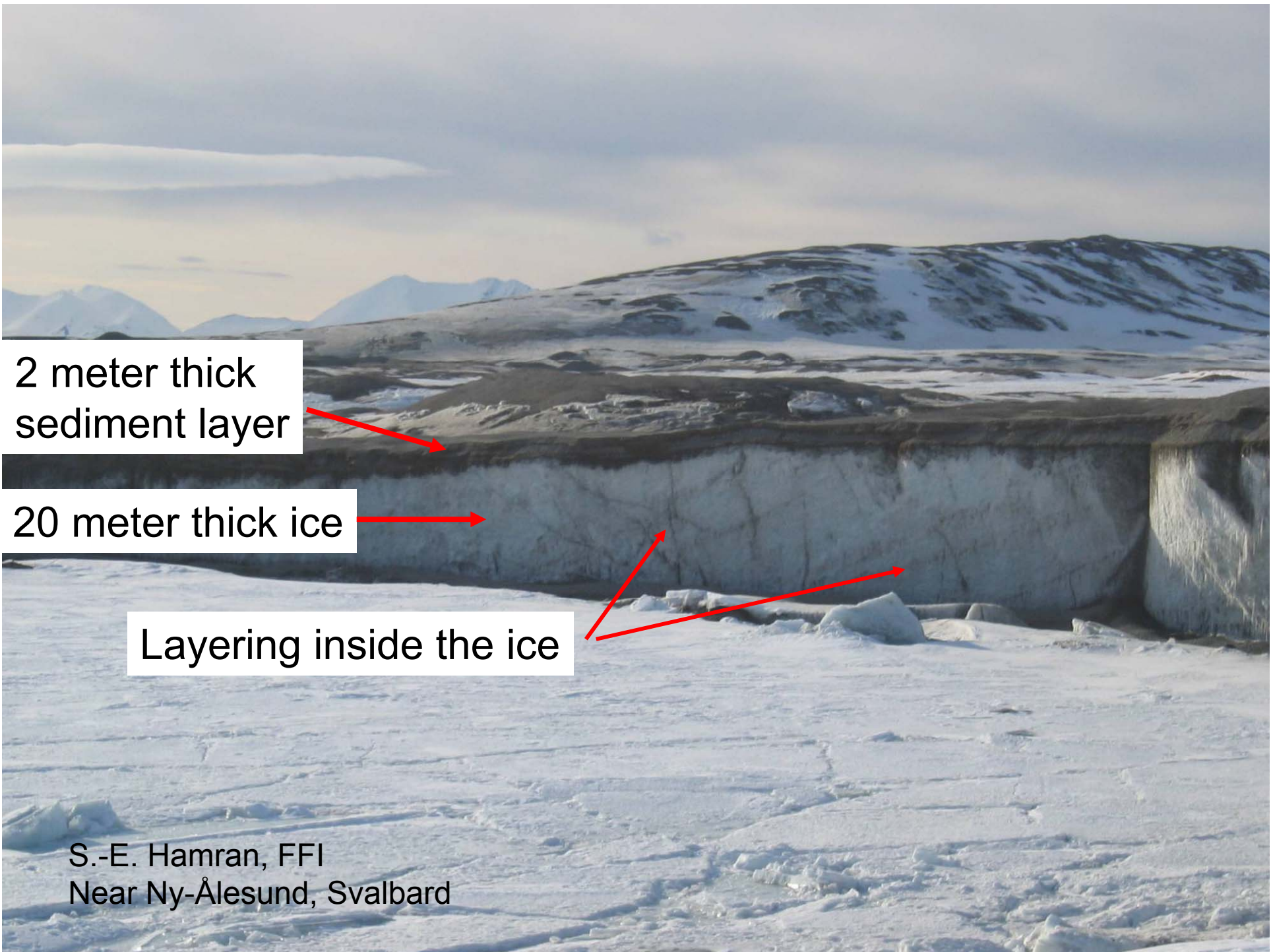
Radar Electronics

PC-Box

Antennas

S.-E. Hamran, FFI

Sampling Wheel



2 meter thick  
sediment layer

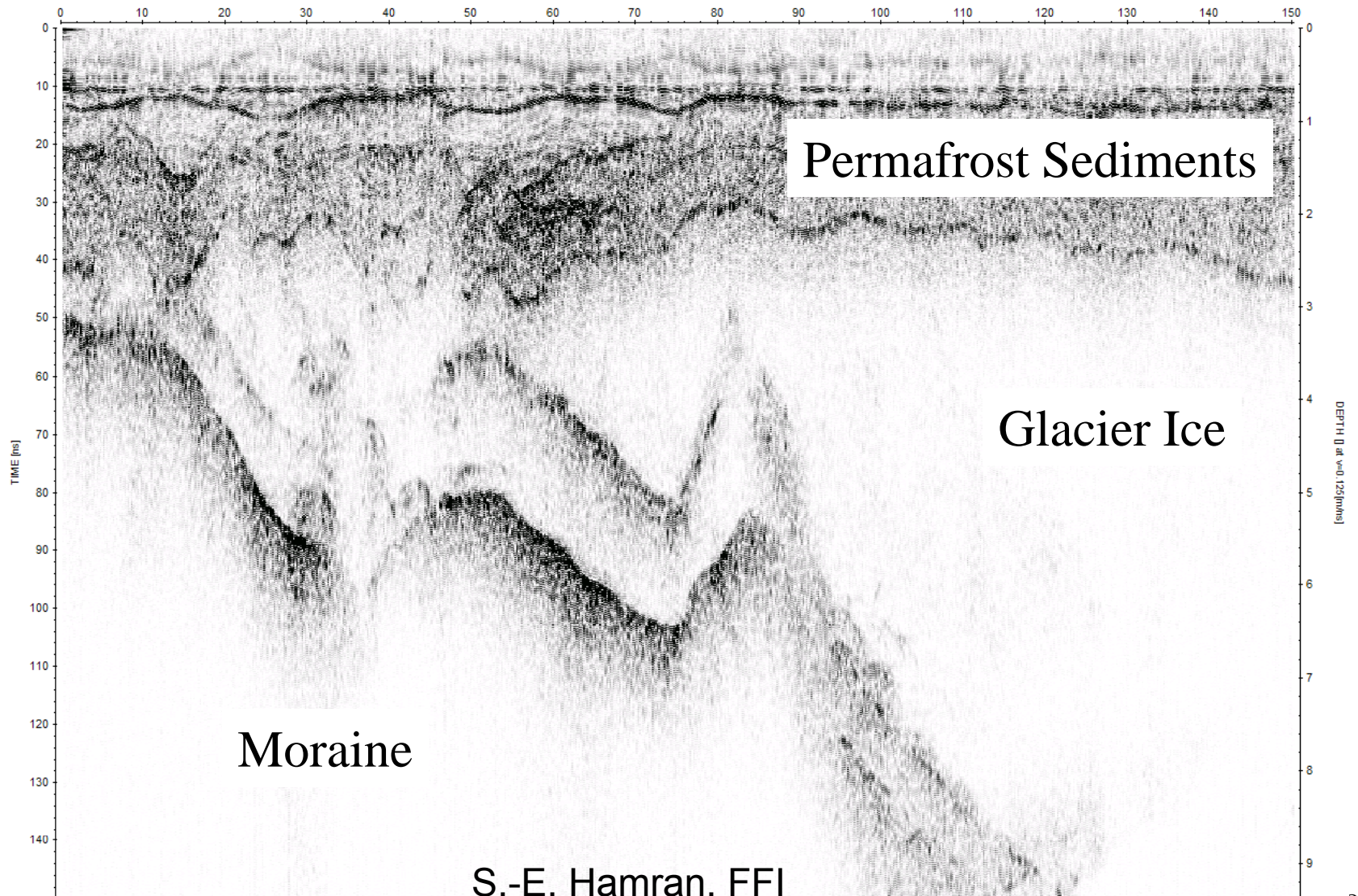
20 meter thick ice

Layering inside the ice

S.-E. Hamran, FFI  
Near Ny-Ålesund, Svalbard



# Subsurface Radar Image

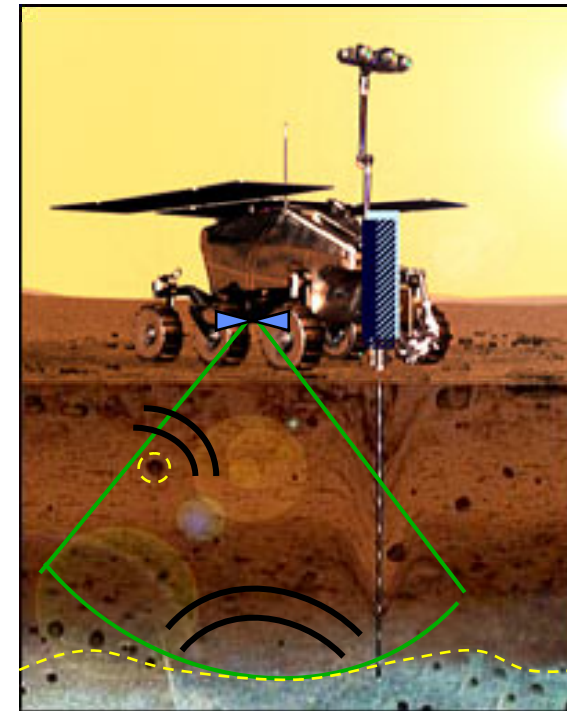






# ExoMars Mission

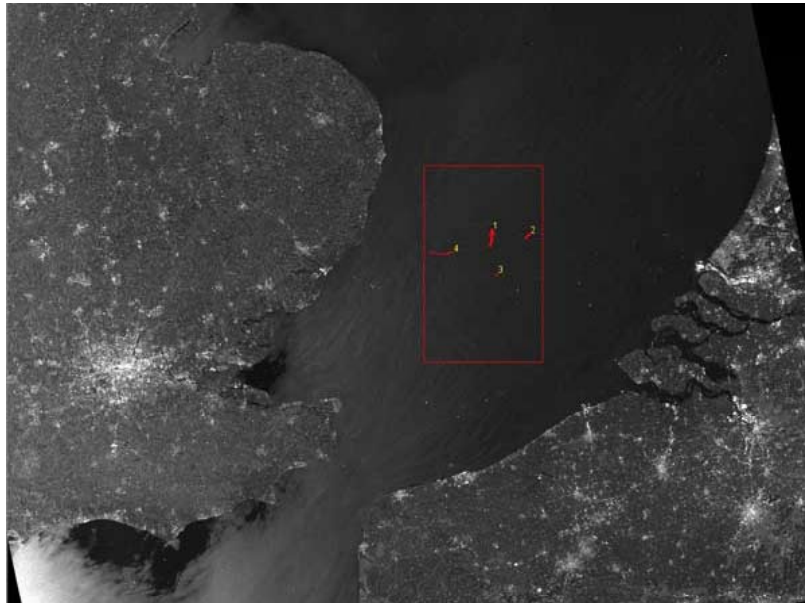
- **Scientific objectives:**
  - Search for signs of life (past/present) on Mars;
  - To characterise the water/geochemical environment as a function of depth in the shallow subsurface;
  - To study the surface environment and identify hazards to future missions;
  - To investigate the planet's subsurface and deep interior to better understand the evolution and habitability of Mars.
- **Pasteur Rover** with instruments: Camera, Organics detector, Mass spectrometer, GPR, Raman/LIBS, Microscope, Drill.
- **GEP:** Met-sensors, Dust, GPR, Electric field
- **WISDOM** = Water Ice and Subsurface Deposit Observations on Mars



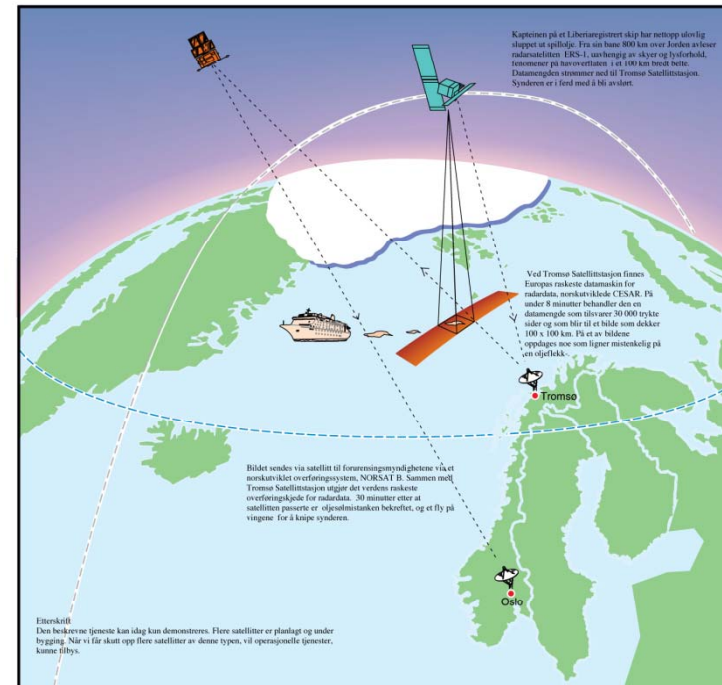
ESA



# Remote sensing - satellite



ENVISAT 16. april 2007 at 2333 Norw. time  
Four oil spills in the English channel  
Copyright: KSAT (Norw. Space Centre)





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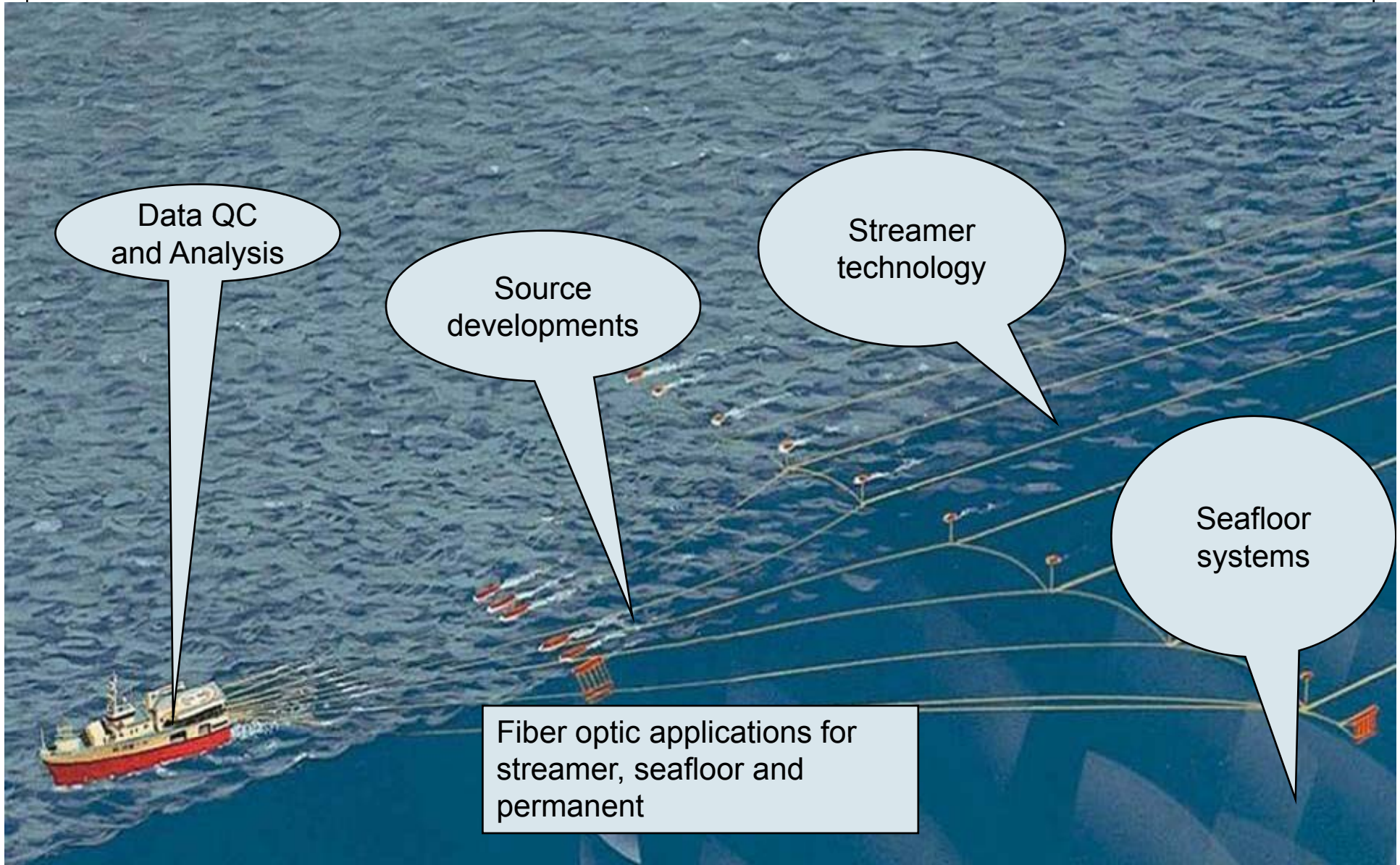
Data QC  
and Analysis

Source  
developments

Streamer  
technology

Seafloor  
systems

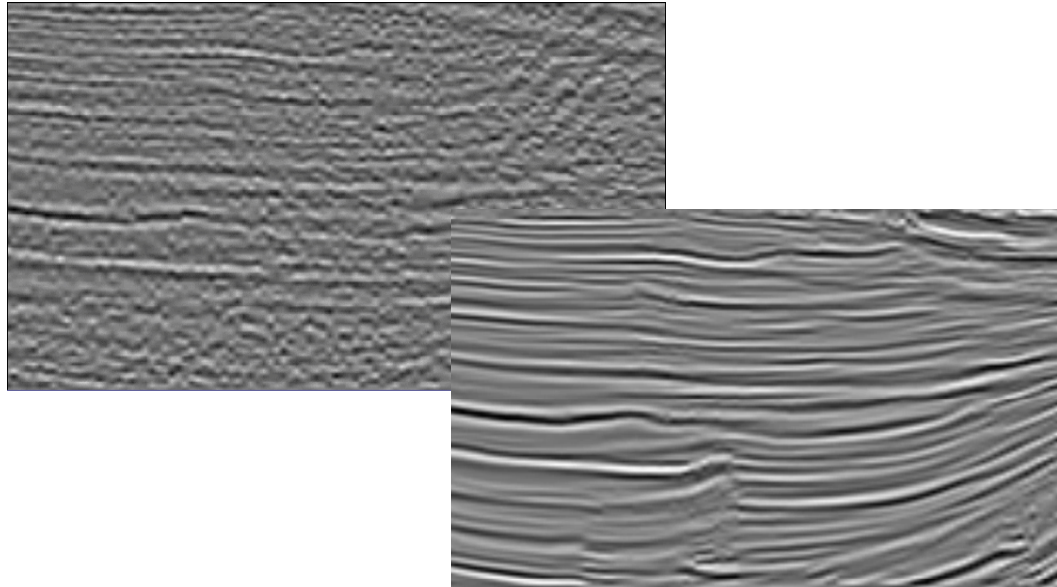
Fiber optic applications for  
streamer, seafloor and  
permanent





# Seismics

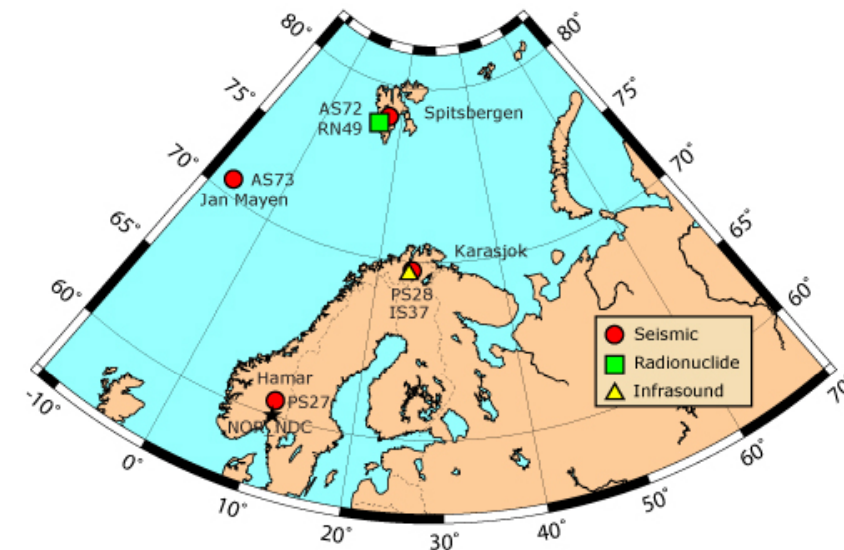
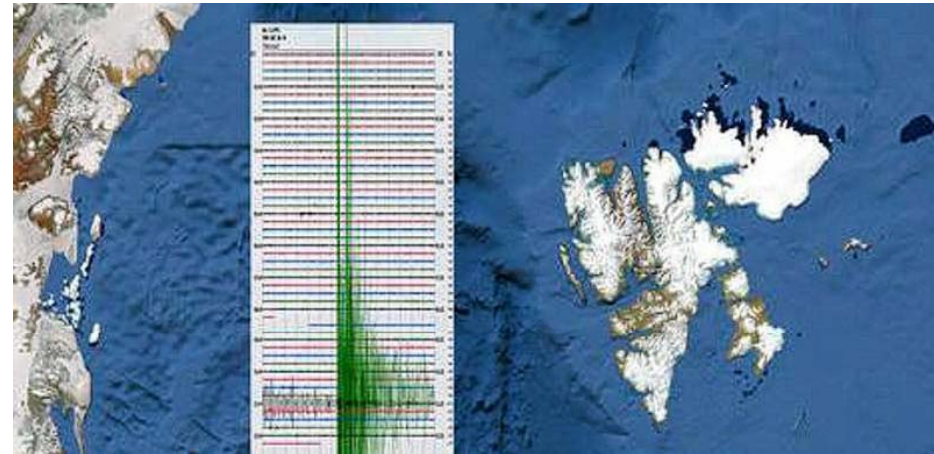
- Improved prestack depth migration
- Data from North Sea





# Seismology

- March 2009: An earthquake of magnitude 6.5 outside Svalbard.
- The strongest ever measured in our part of the world
  - <http://www.aftenposten.no/nyheter/iriks/article2964253.ece>
- Norway: 6 stations (out of 50) in the International Monitoring System (IMS)
  - <http://www.norsar.no/c-71-Station-Network.aspx>



24. august 2011

23



# Centre of Imaging

- Established Jan 2006
- Department of Informatics
  - Digital signal processing and image analysis (DSB)
- Department of Geosciences



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# Imaging principles

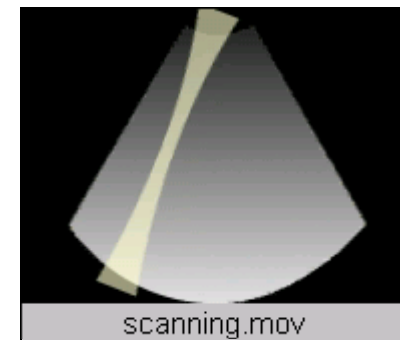
- **Passive:**
  - Reflection
    - » Optics, remote sensing
  - Direct path (one-way):
    - » Passive sonar
    - » Seismology
  - Tomography:
    - » Seismology
- **Active (with transmitter):**
  - Pulse echo:
    - » Active sonar, medical ultrasound, seismics, radar
  - Controlled emission:
    - » X-ray, MR, PET
  - Tomography:
    - » CT, ultrasound





# Echo imaging

- Radar
- Sonar
- Medical Ultrasound
- Non-destructive testing
- Send a 'ping'



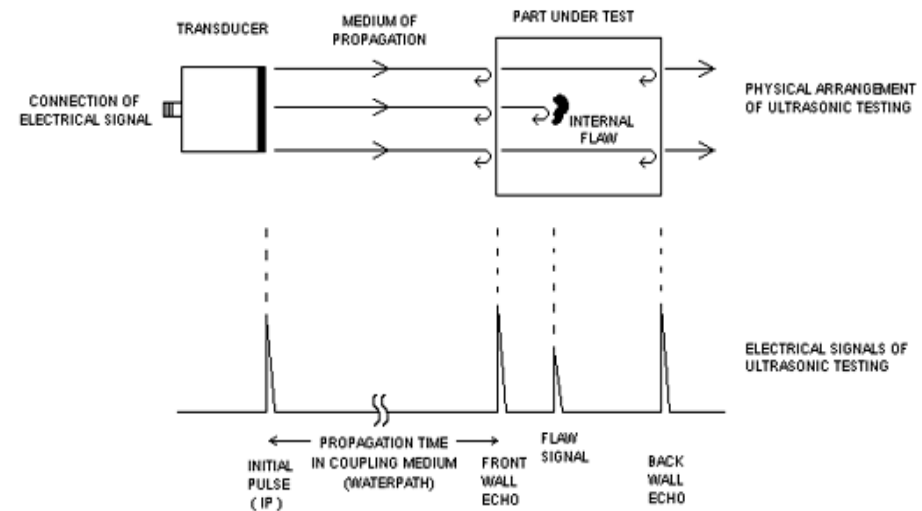


# Radial resolution in echo systems

- Radar, sonar, ultrasound
- Resolution = half the pulse length:

$$\Delta r = c\tau / 2 = c / (2\Delta f)$$

- Also inverse proportional to bandwidth, i.e. usually proportional to centre frequency





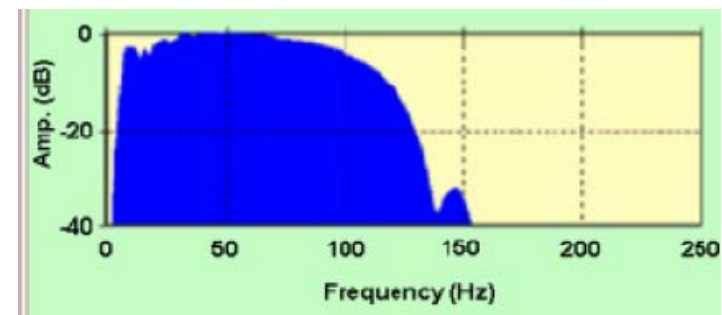
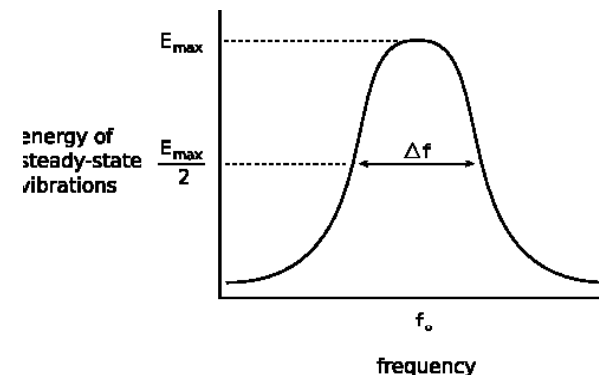
# Bandwidth

- Narrowband (relative bandwidth  $< 10\%$  of center frequency):
  - Optics, remote sensing
  - Radar
  - Sonar (older systems)
  - X-ray
- Wideband:
  - Medical ultrasound
  - Modern sonar
  - Seismics
  - Seismology
- Ultra Wideband (radio)
  - FCC and ITU-R definitions: emitted signal bandwidth exceeds the lesser of 500 MHz or 20% of the center frequency.
  - Frequencies 3.1–10.6 GHz



# Radial, axial, vertical resolution for echo systems (along beam)

- Pulsed continuous wave (PW):  $c\tau/2$
- Broadband pulse:  $c/2\Delta f$ , since  $\tau=1/\Delta f$
- In many systems the transducer/source is the factor which limits bandwidth:
  - $\Delta f = k f_0 \Rightarrow$  where  $k = 50 - 200\%$  = relative bandwidth
  - If  $\Delta f \Leftrightarrow -3\text{dB}$  points, then  $1/k = f_0 / \Delta f = Q\text{-factor}$
- Radial resolution  $c/2\Delta f = c/2k f_0 = Qc/2f_0$ 
  - inverse proportional to center frequency
  - Ex1 (upper fig):  $Q=2$  ( $k=0.5$ )  
 $\Rightarrow$  radial res. =  $c/f_0 = \lambda$ : **typical for medical ultrasound, e.g.  $f_0 = 3.5$  MHz**
  - Ex2 (lower fig):  $Q=0.5$  ( $k=2$ : bandwidth from  $\sim 0$  to  $2f_0$ )  $\Rightarrow$  radial res. =  $\lambda/4$ : **seismics**





## Lateral, horizontal resolution (across beam) for focused beam

- Angular resolution, farfield, focused:  $\theta = k \cdot \lambda / d$ 
  - Definitions: peak-zero, zero-zero, -3dB, -6 dB
  - Constant  $k$  depends on aperture (circular, rectangular):
    - » Circular:
      - -3dB:  $k=1.02$ ; peak-zero:  $k=1.22$ ; -6dB:  $k=1.41$
    - » Rectangular:
      - -3dB:  $k=0.89$ ; peak-zero:  $k=1.0$ ; -6dB:  $k=1.21$
  - Rule-of-thumb: as  $k$  is close to 1:  $\theta \approx \lambda / d$
- $\lambda = c / f \Rightarrow \theta \approx \lambda / d = c / (d \cdot f)$ :
  - lateral resolution improves (= gets smaller) as the center frequency increases



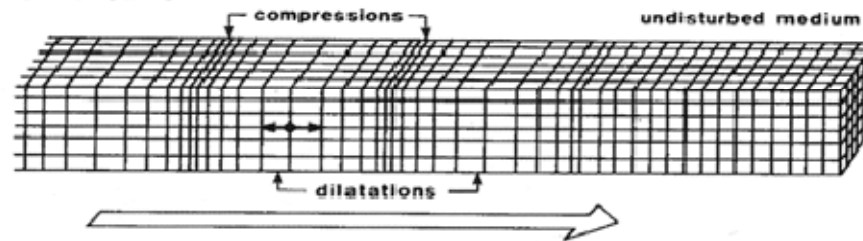
# Wave types

- Electromagnetic waves
  - Optical
  - Infrared, Ultraviolet
  - Radar
  - X-ray (CT – Computer Tomography)
- Mechanical waves
  - Seismics, seismology
  - Audio
  - Ultrasound for sonar and medical ultrasound

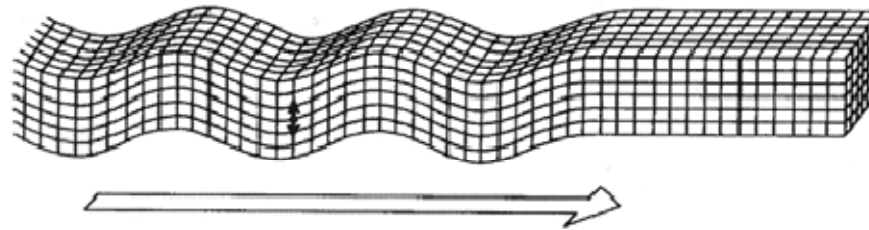


# WAVE PROPAGATION

**P-wave**

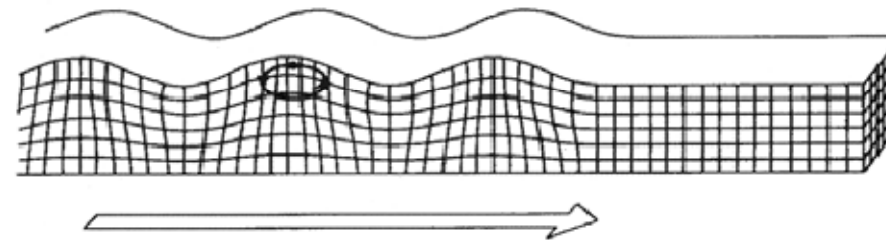


**S-wave**

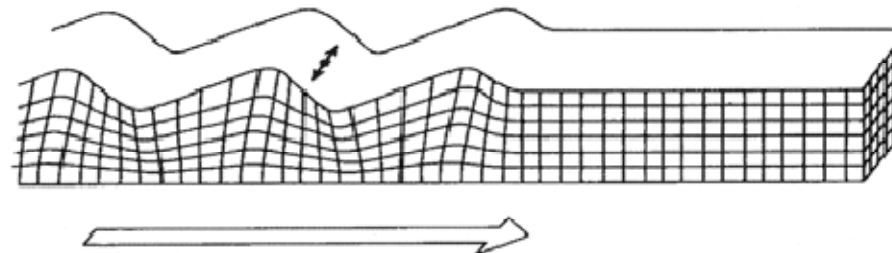


surface waves

**Rayleigh-wave**



**Love-wave**

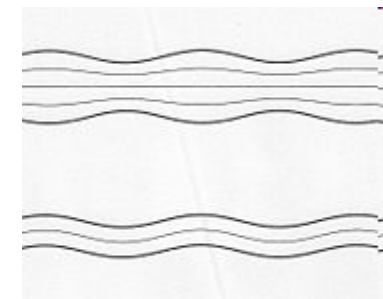




# Wave types

- Longitudinal: pressure wave (P)
  - Acoustics (mechanical wave) in gases and liquids (audio, sonar, medical ultrasound)
  - Mechanical wave in solids (seismics, seismology)
- Transversal: electromagnetic, shear wave (S)
  - Mechanical wave in solids (seismics, seismology)
  - Also a slowly moving shear wave in medical ultrasound
  - Electromagnetic = optics, IR, X-ray, radar
  - polarization
- Surface waves
  - Rayleigh (vertical): ocean waves, seismology
  - Love, component perpendicular to surface (extensional wave), solids only (shear): seismology
- Plate waves
  - Lamb, parallel to plane layer, perpendicular to wave direction (extensional and flexural)
- Modes of Sound Wave Propagation:

<http://www.ndt-ed.org/EducationResources/CommunityCollege/Ultrasonics/Physics/modepropagation.htm>



Extensional mode with  $d / \lambda = 0.6$ .  
Flexural mode with  $d / \lambda = 0.3$ .





# Snell's law

- $\sin\theta_i/v_i = \sin\theta_t/v_t$
- Single-mode: pressure waves or electromagnetic
- Mixed-mode in solids: mode conversion P $\leftrightarrow$ S
- Optics: index of refraction:  
 $n = v_i/v_t$
- Critical angle: transmitted (refracted) wave is parallel to interface -  $\theta_t = 90$  deg
- Non-homogeneous media:  $c(x,y,z)$  - varies in space
  - Varies with depth in seismics/seismology: curved waves
  - Varies with depth, salinity, pressure, ... in underwater acoustics

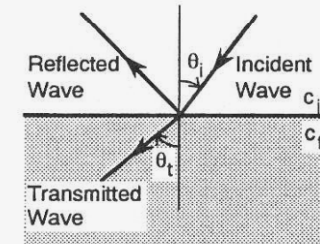
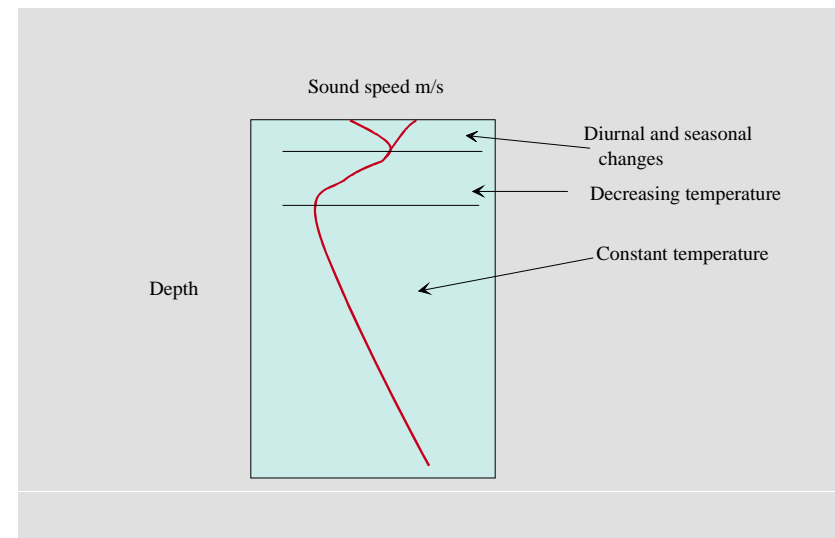


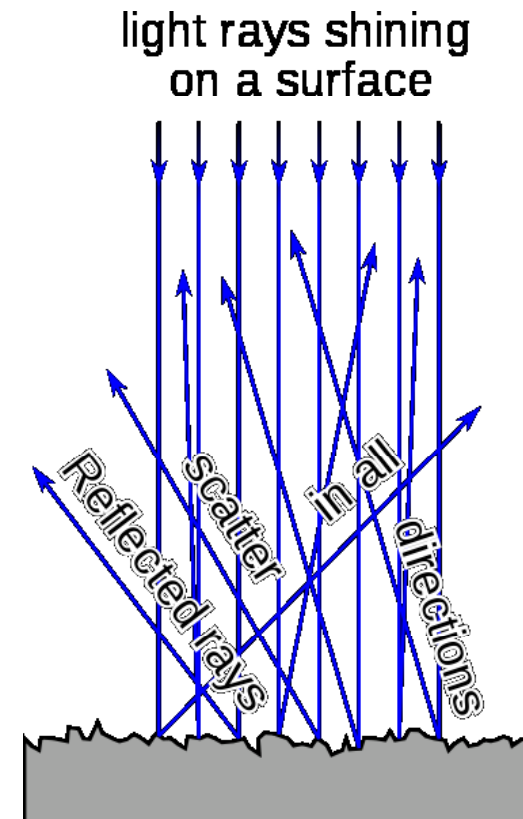
Figure 2.10 An incident wave striking a discontinuity in the medium results in a reflected wave and a transmitted wave. The angle of reflection equals the angle of incidence, and the angle of refraction of the transmitted wave obeys Snell's Law. In this example, the propagation speed in the lower medium is greater than in the upper.





# Diffuse – specular reflection

- Diffuse reflection = scattering
  - When surface irregularities are on the order of the wavelength
  - Illustration: Wikipedia
- Specular reflection = mirror
  - When the surface is smooth compared to a wavelength



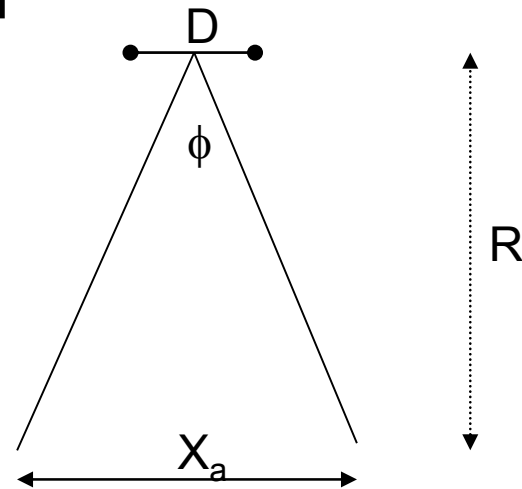


# Near field – farfield

- Aperture:  $D$
- Wavelength:  $\lambda = c/f$
- Distance to target:  $R$

## Independent of type of wave:

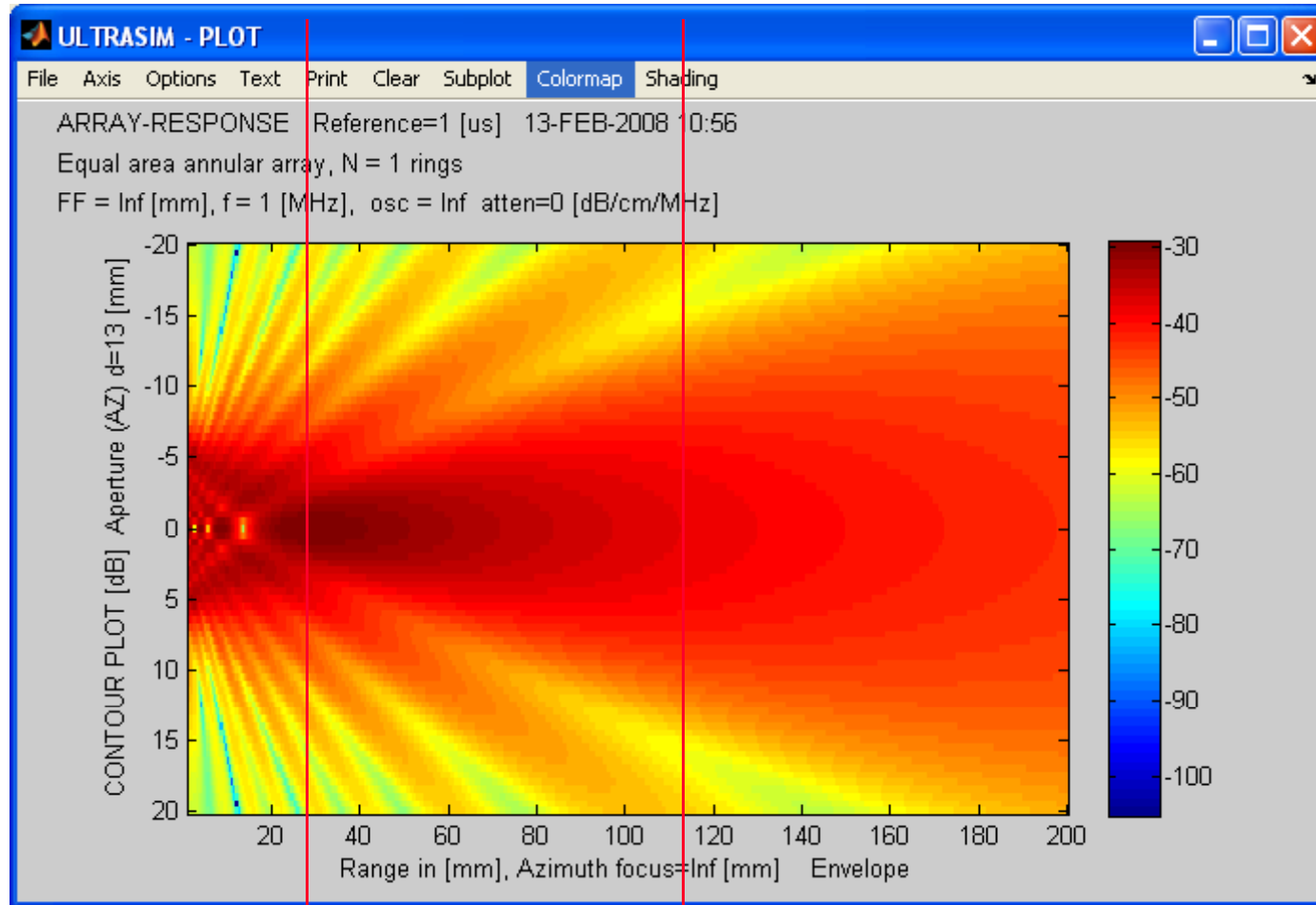
- Angular resolution:  $\phi \approx \lambda/D$
- Resolution at target (azimuth):  
 $X_a \approx R \cdot \phi = \lambda \cdot R/D$
- Near field or far field?  
If the objective is to distinguish something which is smaller than the aperture, i.e.  $X_a < D$ , then it is in the near field and focusing is required



- $X_a = D \Leftrightarrow \lambda \cdot R_{nf}/D = D \Leftrightarrow R_{nf} = D^2/\lambda$
- Nearfield-farfield limit:  
 $D^2/4\lambda \dots D^2/\lambda$  (not a hard limit)



# 1 MHz D=13 mm, unfocused xdcr



Olympus-Panametrics  
A303S  
(in our lab)

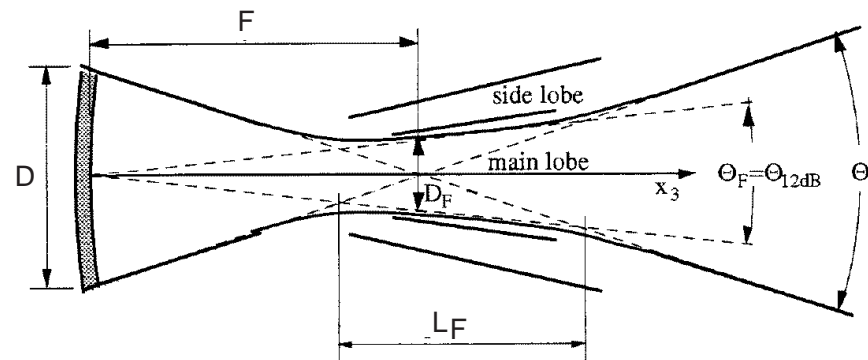
$$D^2/4\lambda$$

$$D^2/\lambda=113 \text{ mm}$$



# Near field – farfield

- Near/far field limit:  $D^2/4\lambda \dots D^2/\lambda$
- Equivalent to hyperfocal distance in optics
  - nearest focus distance at which the far limit of the depth of field,  $L_F$ , extends to infinity
  - i.e. the farthest point to which there is any meaning to focus





# Laser pointer

- Aperture:  $D = 1\text{mm}(?)$ , could be 2
- Wavelength (red):  $\lambda = 650\text{ nm}$
- Near/far-transition:
  - $D^2/4\lambda = (1\text{e-}3)^2/650\text{e-}9 \approx 1.5\text{ m}$
  - $D^2/\lambda \approx 6\text{ m}$





# Nearfield/farfield

- Farfield: remote sensing, radar, sonar
- Important applications in the near field, i.e. Using focusing:
  - Optics
  - Medical ultrasound
  - Seismics
  - Synthetic aperture radar and sonar
- Extreme nearfield: X-ray (CT), laser
  - Collimated beams
  - One reason why ultrasound tomography (nearfield) is so hard compared to X-ray tomography (extreme nearfield)



# Time resolution

- In all pulse-echo systems
- Especially important in medical imaging
  - Pulse Repetition Frequency (PRF) and frame rate must be fast enough to sample the movements of organs in the body
- Also in sonar, radar, seismics



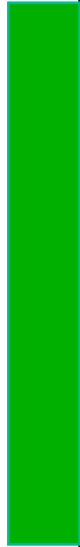


# Medical imaging

- **Ultrasound is best for:**
  - Soft tissues, dynamics of blood flow
  - Fetal, cardiac, liver, kidneys, circulatory system
  - Avoid bone and air (lungs)
- **CT is best for:**
  - Distinguish soft tissue and bone, or tissue and contrast agent
  - Angiography, colon
- **MR is best for:**
  - Detects magnetic dipole of H<sub>2</sub>O molecules
  - Contrast agents, no accumulation of dose as CT
  - Soft tissue: cancer, blood flow (functional MRI)
- **SPECT/PET is best for:**
  - Based on injection of radioactive isotope
  - Brain activity, cancer (large blood flow)



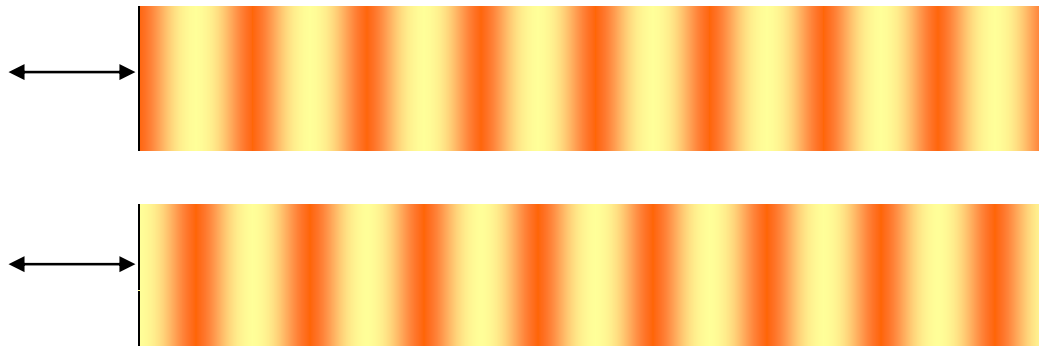
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# Wavelength

- The distance travelled by a wave during one period
- A period:  $T=1/f$ , where  $f$  = frequency [Hz]
- Travelled distance:  $\lambda = Tc = c/f$



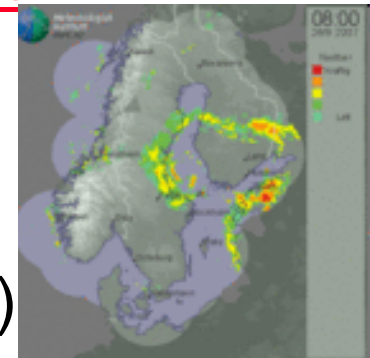
- Shown here: Pressure wave = longitudinal wave
- Transversal waves: electro magnetic waves (optics, radio, ...)
- Other kinds of waves:
  - Shear waves = acoustic waves in solids (e.g. seismics)
  - Surface waves: ocean waves

Figure: J Hovem, TTT4175  
Marine acoustics, NTNU



# Wavelength, electromagnetic waves

- Speed of light:  $c=300,000 \text{ km/sec} = 3 \cdot 10^8 \text{ m/s}$
- Wavelength:  $\lambda = c/f$
- Weather radar <http://met.no/radar/sorost.html>
  - S-band frequencies (2.7 to 3 GHz)
  - $\lambda=3e8/3e9 = 10 \text{ cm}$
- Blue-green light (optical sensor in satellite)
  - $\lambda=500 \text{ nm}$
  - $f = c/\lambda = 3e8/500e-9 = 600 \text{ e}12 = 600 \text{ THz}$





# Wavelength, acoustic waves

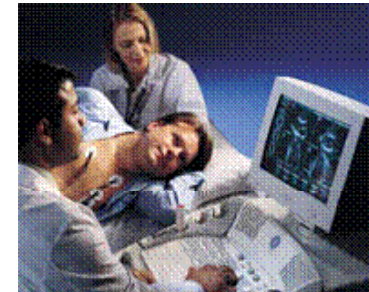
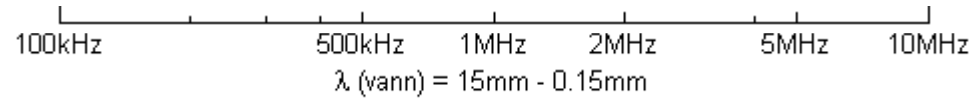
- Speed of sound in ~water:  $c=1500$  m/s
- Wavelength:  $\lambda = c/f$
- Echo sounder for recreational fish-finding
  - $f = 200$  kHz
  - $\lambda=1500/200e3 = 7.5$  mm
- Medical ultrasound scanner
  - $f = 3$  MHz
  - $\lambda=1500/3e6 = 0.5$  mm
- Seismics
  - $f \sim 50$  Hz
  - $\lambda=1500/50 = 30$  m (in water, not in sediment)



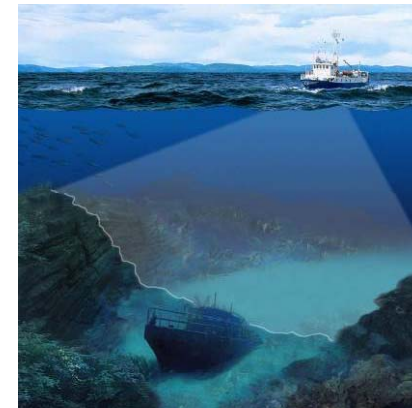
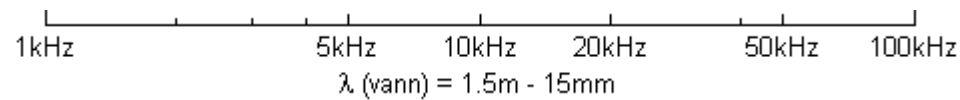


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### Sonars - Non-destructive testing, medical

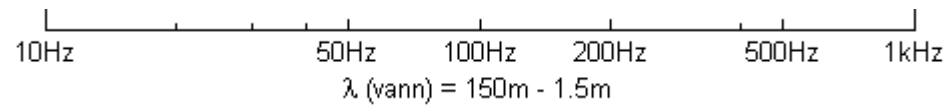


### Sonars, echosounders



### Geophysical

### Geophysics: shallow seismic





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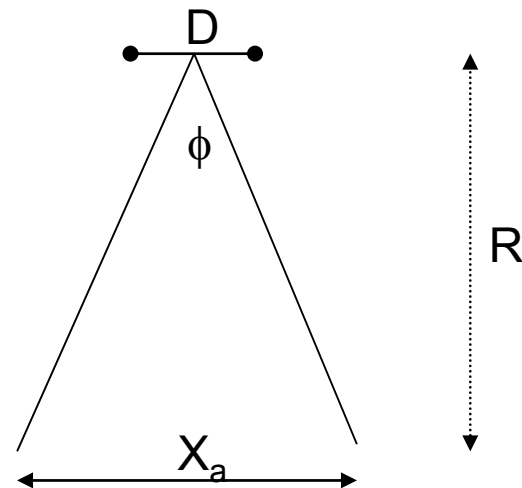


# Resolution

- Aperture:  $D$
- Wavelength:  $\lambda = c/f$
- Distance to target:  $R$

## Independent of type of wave:

- Angular resolution:  $\phi \approx \lambda/D$
- Resolution at target (azimuth):  
 $X_a \approx R \cdot \phi = \lambda \cdot R/D$
- Near field or far field?  
If the objective is to distinguish something which is smaller than the aperture, i.e.  $X_a < D$ , then it is in the near field and focusing is required



- NB! Resolution must always be considered in relation to wave length
- Regardless of whether the wave is acoustic, seismic, electromagnetic, optical, ...





# Satellite: optics, IR, radar

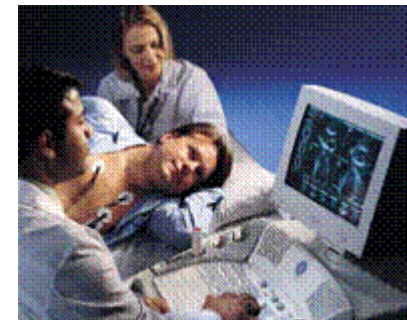
- Polar orbit, height:  $R=800$  km

Sensor	Wave length	Aperture	Ground resolution	Near field?
Light blue-green	$\lambda=500$ nm	$D=40$ mm	$X_a = \lambda \cdot R/D = 0.5 \cdot 10^{-6} \cdot 800 \cdot 10^3 / 0.04 = 10$ m	$X_a > D$ : far field
Thermal IR	$\lambda=10$ $\mu$ m	$D=80$ cm	$X_a = \lambda \cdot R/D = 10 \cdot 10^{-6} \cdot 800 \cdot 10^3 / 0.8 = 10$ m	$X_a > D$ : far field
Radar	$f=3$ GHz, $\lambda=10$ cm	$D=10$ m	$X_a = \lambda \cdot R/D = 0.1 \cdot 800 \cdot 10^3 / 10 = 8$ km	$X_a > D$ : far field
Radar, synthetic aperture		$D=8$ km	$X_a = \lambda \cdot R/D = 0.1 \cdot 800 \cdot 10^3 / 8 \cdot 10^3 = 10$ m	$X_a < D$ : near field



# Medical ultrasound

- Cardiology:
  - Aperture  $D = 19$  mm, Depth  $R = 50$  mm,
  - $f = 3.5$  MHz  $\Rightarrow \lambda = 1540/3.5 \cdot 10^6 = 0.44$  mm
- Resolution:
  - $X_a = \lambda \cdot R/D = 0.44 \cdot 50/19 = 1.1$  mm
  - $X_a < D$ : near field
- Near field/ far field limit:
  - $X_a = D \Leftrightarrow \lambda \cdot R_{nf}/D = D \Leftrightarrow R_{nf} = D^2/\lambda$
  - Often  $D^2/4\lambda$
  - Medical ultrasound: limit  $R_{nf} = 19^2/0.44 = 820$  mm = 0.82 m
  - Always operates in the near field and focusing is always required





# Sonar

- Sonar:
  - $f = 2.5 - 500$  kHz
  - $D = 8$  m – 10 cm
- Typical:
  - $D = 1$  m,  $R = 1$  km
  - $f = 50$  kHz  $\Rightarrow \lambda = 1480/50 \cdot 10^3 \approx 3$  cm
- Resolution:
  - $X_a = \lambda \cdot R/D = 3 \cdot 10^{-2} \cdot 1000/1 = 30$  m
  - $X_a > D$ : far field
  - $R_{nf} = D^2/\lambda \approx 34$  m
  - Sonars usually operate in the far field except for very high frequencies, i.e.  $f >$  approx. 200 kHz



Tx array

Rx array



# Seismics

- Deep seismics:
  - $D = 1$  km (streamer),  $R = 2$  km,
  - $f =$  approx. 50 Hz (broad band)  $\Rightarrow \lambda = 3000/50 = 60$  m
- Resolution:
  - $X_a = \lambda \cdot R/D = 60 \cdot 2/1 = 120$  m
  - $X_a < D$ : near field
  - NB! Inhomogeneous medium,  $c$  varies





# Eyes and ears

## Eyes:

- $D = 1.5 - 8 \text{ mm}$ ,
- $R = 1 \text{ m}$
- $\lambda = 400-700 \text{ nm}$
- Resolution:  $X_a = \lambda \cdot R/D = 500 \cdot 10^{-9} \cdot 1000/8 \approx 0.06 \text{ mm} !$
- $X_a < D$ : near field; therefore we have an adaptive lens
- Presbyopia: stiffer and less flexible lens with age



## Ears:

- Distance:  $D=17.5 \text{ cm}$
- $f = 1000 \text{ Hz}$
- $\lambda = 340/1000 = 34 \text{ cm}$
- Assume  $R = 5 \text{ m}$
- $X_a = \lambda \cdot R/D = 0.34 \cdot 5/0.175 = 9.7 \text{ m}$
- Duplex theory - Rayleigh 1907:
  - IPD Interaural phase difference for  $f < \text{approx. } 1.5 \text{ kHz}$
  - ILD Interaural level difference for higher frequencies
- Head-related transfer function (HRTF) due to shape of outer ear





# Why are antennas for mobile phone base stations tall and narrow?





# På norsk

- (Angular) resolution = (Vinkel)oppløsning
- Bølgelengde, trykkbølger, skjærbølger, overflatebølger, båndbredde, nærfelt, fjernfelt, (syntetisk) aperture,



# Recommended animations

- Acoustics and Vibration Animations
- Dan Russell, Kettering University, Flint, MI
- <http://www.gmi.edu/~drussell/Demos.html>