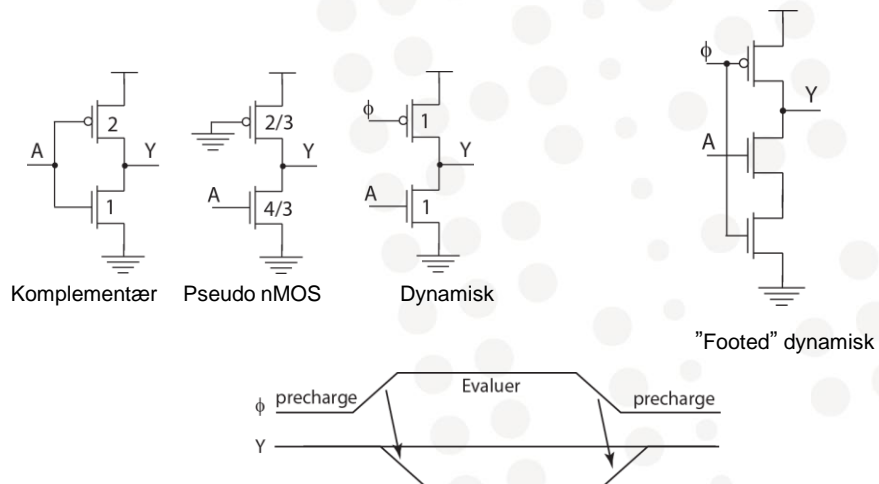
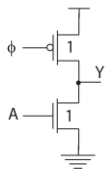




Introduksjon til dynamisk CMOS



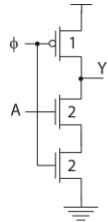
Dynamiske invertere:



$$g_d = 1/3$$

$$P_d = 2/3$$

Ikke-footed inverter:



$$g_d = 2/3$$

$$P_d = 1$$

$$g_d = \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n}\right)^{-1}}$$

$$= \frac{W_n}{3W_n}$$

$$= \frac{1}{3}$$

$$P_d = \frac{1}{W_n} \cdot R \cdot (W_p + W_n) \cdot C$$

$$= 1R \cdot 2C$$

$$= 2RC$$

$$= \frac{2}{3} \tau$$

Footed inverter:

$$g_d = \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n} + \frac{1}{W_n}\right)^{-1}}$$

$$= \frac{W_n}{3\left(\frac{2}{W_n}\right)^{-1}}$$

$$= \frac{2}{3}$$

$$P_d = \left(\frac{1}{W_n} + \frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n) \cdot C$$

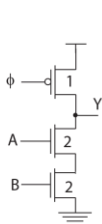
$$= \left(\frac{1}{2} + \frac{1}{2}\right) R \cdot (1 + 2)C$$

$$= 3RC$$

$$= 1\tau$$

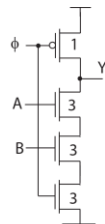
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Dynamiske NAND2:



$$g_d = 2/3$$

$$P_d = 1$$



$$g_d = 1$$

$$P_d = 4/3$$

Ikke-footed NAND2:

$$g_d = \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n} + \frac{1}{W_n}\right)^{-1}}$$

$$= \frac{W_n}{3\left(\frac{2}{W_n}\right)^{-1}}$$

$$= \frac{2}{3}$$

$$P_d = \left(\frac{1}{W_n} + \frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n) \cdot C$$

$$= \left(\frac{1}{2} + \frac{1}{2}\right) R \cdot (1 + 2)C$$

$$= 3RC$$

$$= 1\tau$$

Footed NAND2:

$$g_d = \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n} + \frac{1}{W_n} + \frac{1}{W_n}\right)^{-1}}$$

$$= \frac{W_n}{3\left(\frac{3}{W_n}\right)^{-1}}$$

$$= 1$$

$$P_d = \left(\frac{1}{W_n} + \frac{1}{W_n} + \frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n) \cdot C$$

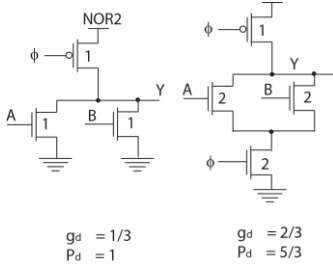
$$= \left(\frac{1}{3} + \frac{1}{3} + \frac{1}{3}\right) R \cdot (1 + 3)C$$

$$= 4RC$$

$$= \frac{4}{3} \tau$$

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Dynamiske NOR2:



$$g_d = 1/3$$

$$P_d = 1$$

$$g_d = 2/3$$

$$P_d = 5/3$$

Ikke-footed NOR2:

$$g_d = \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n}\right)^{-1}}$$

$$= \frac{W_n}{3 \left(\frac{1}{W_n}\right)^{-1}}$$

$$= \frac{1}{3}$$

$$P_d = \left(\frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n + W_n) \cdot C$$

$$= \left(\frac{1}{1}\right) R \cdot (1 + 1 + 1) C$$

$$= 3RC$$

$$= 1\tau$$

Footed NOR2:

$$g_d = \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n} + \frac{1}{W_n}\right)^{-1}}$$

$$= \frac{W_n}{3 \left(\frac{2}{W_n}\right)^{-1}}$$

$$= \frac{2}{3}$$

$$P_d = \left(\frac{1}{W_n} + \frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n + W_n) \cdot C$$

$$= \left(\frac{1}{2} + \frac{1}{2}\right) R \cdot (1 + 2 + 2) C$$

$$= 5RC$$

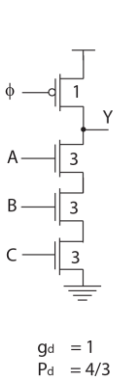
$$= \frac{5}{3}\tau$$



Oppgave 6.27

Tegn transistorskjema for dynamisk footed 3inngangs NAND og NOR porter. Angi bredde på transistorene. Hva blir logisk effort for portene?

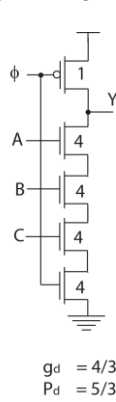
Dynamiske NAND3:



$$g_d = 1$$

$$P_d = 4/3$$

Ikke-footed NAND3:



$$g_d = \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n} + \frac{1}{W_n} + \frac{1}{W_n}\right)^{-1}}$$

$$= \frac{W_n}{3 \left(\frac{3}{W_n}\right)^{-1}}$$

$$= 1$$

$$P_d = \left(\frac{1}{W_n} + \frac{1}{W_n} + \frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n) \cdot C$$

$$= \left(\frac{1}{3} + \frac{1}{3} + \frac{1}{3}\right) R \cdot (1 + 3) C$$

$$= 4RC$$

$$= \frac{4}{3}\tau$$

Footed NAND3:

$$g_d = \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n} + \frac{1}{W_n} + \frac{1}{W_n} + \frac{1}{W_n}\right)^{-1}}$$

$$= \frac{W_n}{3 \left(\frac{4}{W_n}\right)^{-1}}$$

$$= \frac{4}{3}$$

$$P_d = \left(\frac{1}{W_n} + \frac{1}{W_n} + \frac{1}{W_n} + \frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n) \cdot C$$

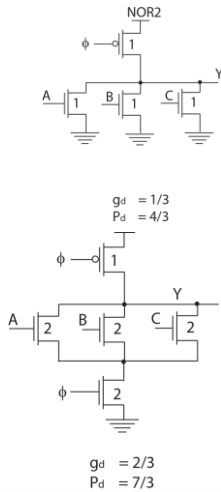
$$= \left(\frac{1}{4} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4}\right) R \cdot (1 + 4) C$$

$$= 5RC$$

$$= \frac{5}{3}\tau$$



Dynamiske NOR3:



Ikke-footed NOR3:

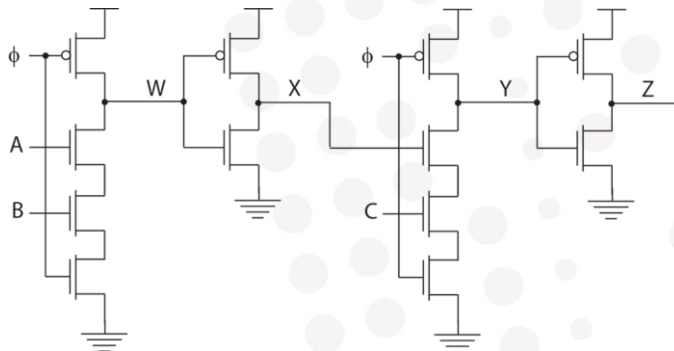
$$\begin{aligned}
 g_d &= \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n}\right)^{-1}} \\
 &= \frac{W_n}{3 \left(\frac{1}{W_n}\right)^{-1}} \\
 &= \frac{1}{3} \\
 P_d &= \left(\frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n + W_n + W_n) \cdot C \\
 &= \left(\frac{1}{1}\right) \cdot R \cdot (1 + 1 + 1 + 1)C \\
 &= 4RC \\
 &= \frac{4}{3} \tau
 \end{aligned}$$

Footed NOR3:

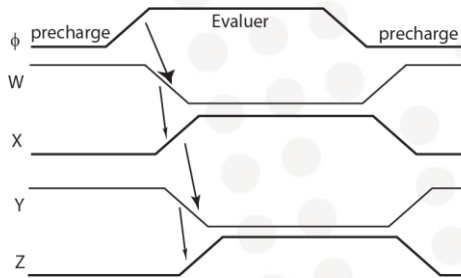
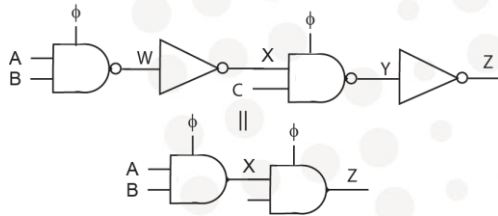
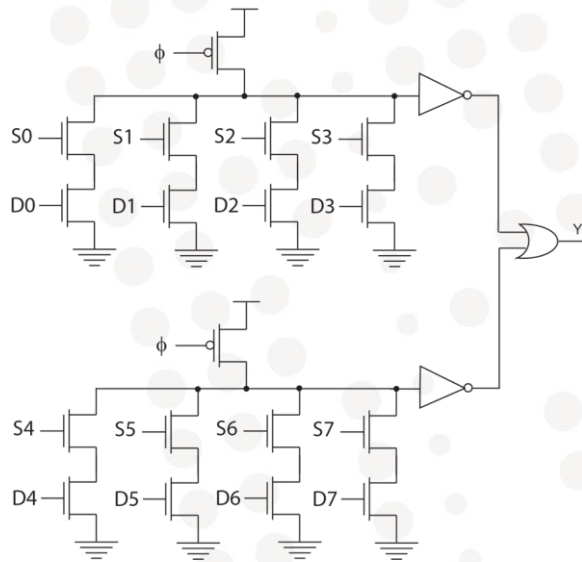
$$\begin{aligned}
 g_d &= \frac{W_n}{\left(1 + \frac{\mu_n}{\mu_p}\right) \cdot \left(\frac{1}{W_n + W_n}\right)^{-1}} \\
 &= \frac{W_n}{3 \left(\frac{2}{W_n}\right)^{-1}} \\
 &= \frac{2}{3} \\
 P_d &= \left(\frac{1}{W_n} + \frac{1}{W_n}\right) \cdot R \cdot (W_p + W_n + W_n + W_n) \cdot C \\
 &= \left(\frac{1}{2} + \frac{1}{2}\right) R \cdot (1 + 2 + 2 + 2)C \\
 &= 7RC \\
 &= \frac{7}{3} \tau
 \end{aligned}$$


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Domino logikk

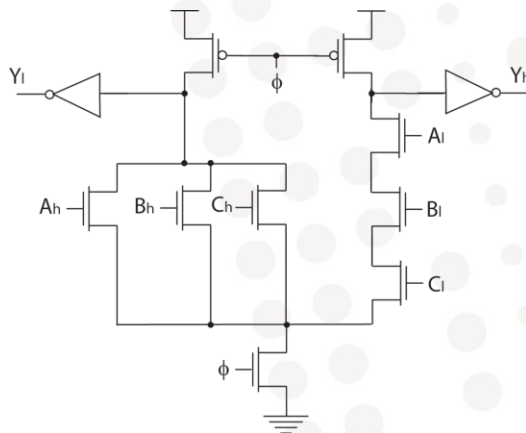

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Domino
multiplexer:

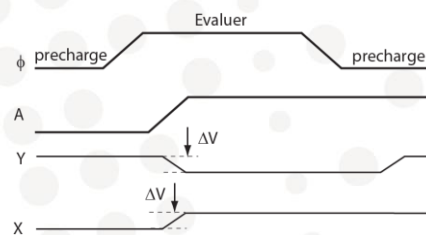
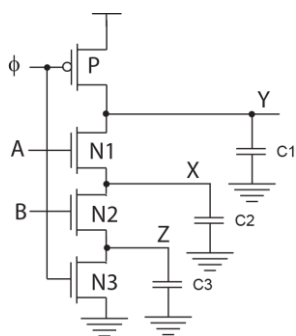


Oppgave 6.28

Tegn transistorskjema for en 3inngangs dual-rail domino OR/NOR port.



Ladningsdeling



Endring pga. ladningsdeling:

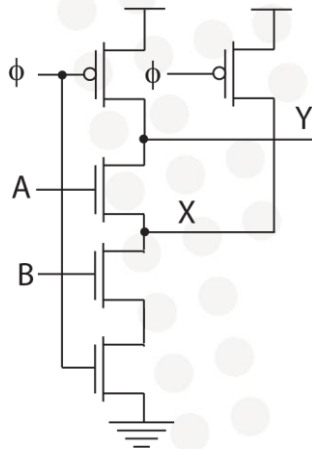
$$\Delta V = \left(1 - \frac{C_1}{C_1 + C_2}\right) \cdot V_{DD}$$

$$V_Y = V_{DD} - \Delta V$$

$$V_X \approx V_Y$$

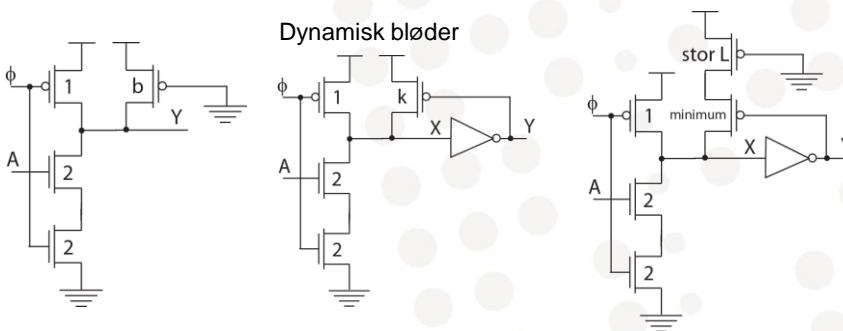


Precharge av interne noder



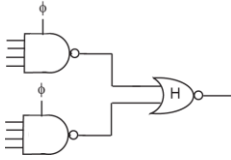
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Blødere (keepers)



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Eksempel:



$$G_u = \frac{5}{3} \cdot \frac{3}{2}$$

$$= \frac{5}{2}$$

$$P_u = (5C + C) \cdot R + \left(4C + 2 \cdot \frac{1}{2}C\right) \cdot R$$

$$= 11RC$$

$$= \frac{11}{3} \tau$$

$$N = 2$$

$$f' = F^{\frac{1}{2}}$$

$$= (G \cdot 1 \cdot H)^{\frac{1}{2}}$$

$$= \sqrt{\frac{5H}{2}}$$

Tidsforsinkelse i kjeden:

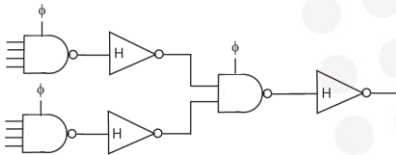
$$D = NF^{\frac{1}{N}} + P_u$$

$$= 2 \sqrt{\frac{5H}{2}} + \frac{11}{3}$$

ifj

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Eksempel:



$$G_u = \frac{5}{3} \cdot \frac{5}{6} \cdot 1 \cdot \frac{5}{6}$$

$$= \frac{125}{108}$$

$$P_u = (5C + C) \cdot R + \left(2 + \frac{1}{2}\right)C \cdot R + (3C + C) \cdot R + \left(2 + \frac{1}{2}\right)C \cdot R$$

$$= 15RC$$

$$= 5\tau$$

$$N = 4$$

$$f' = F^{\frac{1}{4}}$$

$$= (G \cdot 1 \cdot H)^{\frac{1}{4}}$$

$$= \left(\frac{125H}{108}\right)^{\frac{1}{4}}$$

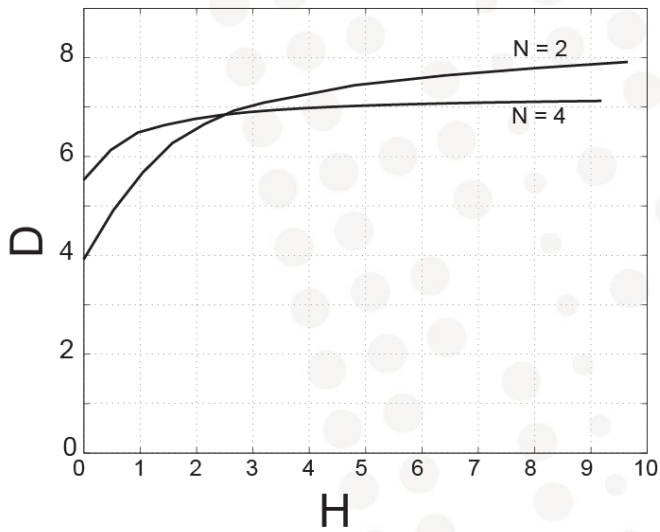
Tidsforsinkelse i kjeden:

$$D = NF^{\frac{1}{N}} + P_u$$

$$= 4 \cdot \left(\frac{125H}{108}\right)^{\frac{1}{4}} + 5$$

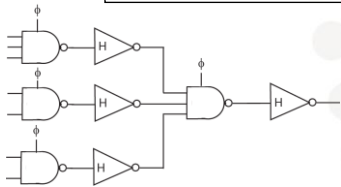
ifj

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Oppgave E

Finn tidsforsinkelse i den dynamiske kjeden som er vist i Figuren.



$$G_u = \frac{4}{3} \cdot \frac{5}{6} \cdot \frac{4}{3} \cdot \frac{5}{6}$$

$$= \frac{100}{81}$$

$$P_u = 5RC + \left(2 + \frac{1}{2}\right)C \cdot R + 5RC + \left(2 + \frac{1}{2}\right)C \cdot R$$

$$= 15RC$$

$$= 5\tau$$

$$N = 4$$

$$f' = F^{\frac{1}{4}}$$

$$= (G \cdot 1 \cdot H)^{\frac{1}{4}}$$

$$= \left(\frac{100H}{81}\right)^{\frac{1}{4}}$$

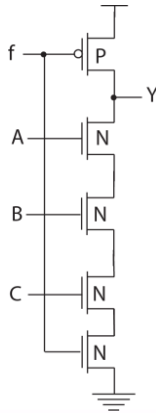
Tidsforsinkelse i kjeden:

$$D = NF^{\frac{1}{N}} + P_u$$

$$= 4 \cdot \left(\frac{100H}{81}\right)^{\frac{1}{4}} + 5$$

Eksamensoppgave 2005

Hva blir parasittisk tidsforsinkelse for nedtrekket for 3inngangsdynamisk footed NAND porten?



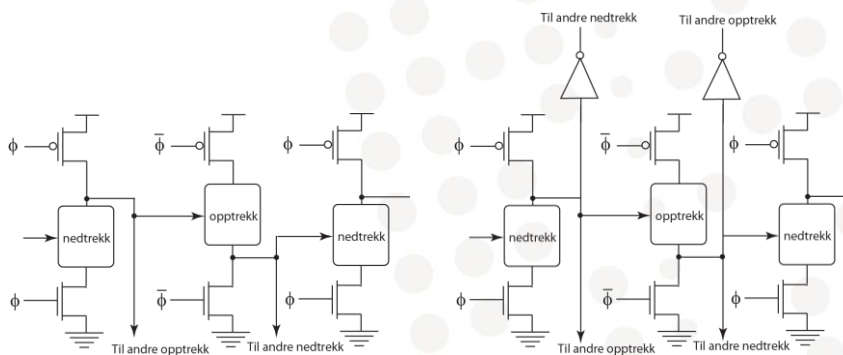
Velger $N=4$ som gir effektiv motstand i nedtrekket lik R :

$$\begin{aligned} P_d &= R(1+4)C \\ &= 5RC \\ &= \frac{5}{3}\tau \end{aligned}$$



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NP (og Zipper domino)



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