# INF3580/4580 - Semantic Technologies - Spring 2017

Lecture 6: Introduction to Reasoning with RDF

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20th February 2017



DEPARTMENT OF INFORMATICS



University of Oslo

# Mandatory exercises

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- Exercises mostly from this week's lecture, but one from next week's lecture, Reasoning with Jena.

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# Today's Plan

Inference rules

2 RDFS Basics

Open world semantics

#### Outline

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2 RDFS Basics

Open world semantics

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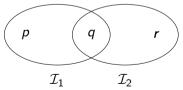
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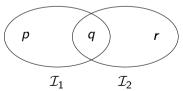
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Syntactic reasoning easier to understand and use than model semantics

• we will show that first.

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Where  $\models$  is the entailment relation,  $\vdash$  is the inference relation. We write  $\Gamma \vdash P$  if we can deduce P from the assumptions  $\Gamma$ .

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# Inference rules in propositional logic

(Part of) Natural dedcution calclulus for propositional logic:

$$\frac{A \qquad (A \to B)}{B} \to E$$

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may be read as an instruction;

• "If  $P_1, \ldots, P_n$  are all in the store, add P to the store."

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- and (for our purposes) a subset of OWL.

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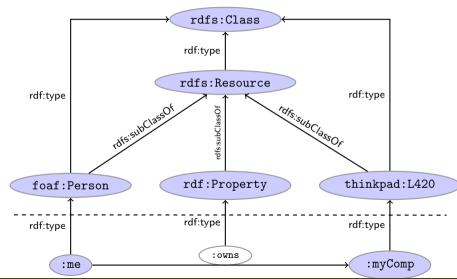
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  - rdfs:subPropertyOf: Property inclusion.

#### Example



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RDFS	Set Theory
A rdf:type rdfs:Class	A is a set of resources
x rdf:type $A$	$x \in A$
A rdfs:subClassOf B	$A\subseteq B$

RDFS supports three principal kinds of reasoning pattern:

I. Type propagation:

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  - "All fathers of people are males. James is the father of Karl, therefore..."

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# Set Theory Analogy

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A rdfs:subClassOf B . x rdf:type A . 
$$x rdf:type B .$$
 
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$$x \in B$$

# Set Theory Analogy

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• Reflexivity of sub-class relation

$$A$$
 is a set  $A \subseteq A$ 

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$$\frac{A \subseteq B \qquad x \in A}{x \in B}$$

Reflexivity of sub-class relation

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A rdfs:subClassOf B . B rdfs:subClassOf C . A rdfs:subClassOf C . 
$$\frac{A \subseteq B \quad B \subseteq C}{A \subset C}$$

### RDFS/RDF knowledge base:

ex:Vertebrate rdf:type rdfs:Class .

```
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ex:Vertebrate rdf:type rdfs:Class .
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(rdfs11)

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    ex:Mammal rdfs:subClassOf ex:Mammal . (rdfs10)
      (... and also for the other classes)
```

# A typical taxonomy

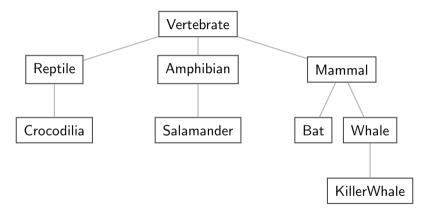


Figure: A typical taxonomy

• A set is a subset of many other sets:

$$\{2,3\} \subseteq \{1,2,3\} \quad \{2,3\} \subseteq \{2,3,4\} \quad \{2,3\} \subseteq \mathbb{N} \quad \{2,3\} \subseteq \mathbb{P}$$

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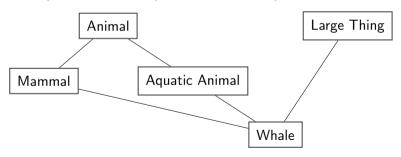
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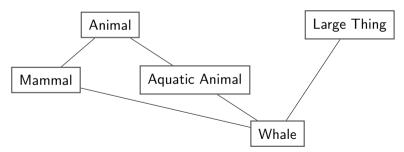


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• This is usually not called a taxonomy, but it's no problem for RDFS.

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p rdfs:subPropertyOf r . rdfs5
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RDFS	Set Theory
r rdf:type rdf:Property	r is a relation on resources
x r y	$\langle x,y \rangle \in r$
<pre>r rdfs:subPropertyOf s</pre>	$r\subseteq s$

# Intuition: Properties as Relations

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for instance Dublin Core.

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```
:writer rdf:type rdf:Property .
:author rdf:type rdf:Property .
:author rdfs:subPropertyOf dcterms:creator .
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```
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And Facts:
   ex:knausgård :writer ex:minKamp .
   ex:hamsun :author ex:sult .
```

Infer:

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#### From Ontology:

```
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- The work of integrating the data is thus done by the reasoning engine,
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- Legacy applications that use e.g. author can operate unmodified.

Large organizations (e.g. universities) offer different kinds of contracts;

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- :recSchol (receives scholarship from).

# Organising the properties

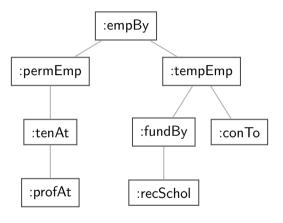


Figure: A hierarchy of employment relations

## Organising the properties

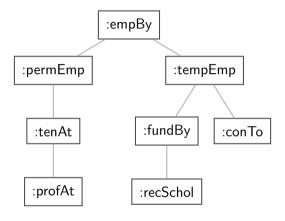


Figure: A hierarchy of employment relations

• Note: doesn't have to be tree-shaped.

# Querying the inferred model

#### Formalising the tree:

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:profAt rdf:type rdfs:Property .
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:profAt rdfs:subPropertyOf :tenAt
..... and so forth.
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#### Given a data set such as:

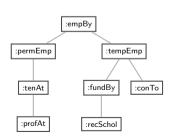
```
:Arild :profAt :UiO .

:Audun :fundBy :UiO .

:Steve :conTo :OLF .

:Trond :recSchol :BI .

:Jenny :tenAt :SSB .
```



#### cont.

### We may now query on different levels of abstraction:

### Temporary employees

```
SELECT ?emp WHERE {?emp :tempEmp \_:x .} \rightarrow Audun, Steve, Trond
```

#### cont.

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→ Audun, Steve, Trond
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```

#### cont.

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```
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Arild, Jenny
```

### All employees

```
SELECT ?emp WHERE {?emp :empBy _{-}:x .} \rightarrow Arild, Jenny, Audun, Steve, Trond
```

Triggered by combinations of

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• rdfs:range

Triggered by combinations of

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Rules for domain and range reasoning:

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  - therefore an application of p suffices to type that resource.

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- The *domain* of R is the set of all x with  $xR \cdots$ :

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• Example:

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  - $R = \{\langle 1, \triangle \rangle, \langle 1, \square \rangle, \langle 2, \lozenge \rangle\}$
  - dom  $R = \{1, 2\}$
  - $\operatorname{rg} R = \{\triangle, \square, \lozenge\}$

### Set intuitions for rdfs:domain and rdfs:range

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RDFS	Set Theory
r rdfs:domain A	$domr\subseteq A$
r rdfs:range B	$\operatorname{rg} r \subseteq B$

Rules:

$$\frac{\operatorname{dom} p \subseteq A \qquad \langle x, y \rangle \in p}{x \in A}$$

$$\frac{\operatorname{rg} p \subseteq B \qquad \langle x, y \rangle \in p}{y \in B}$$

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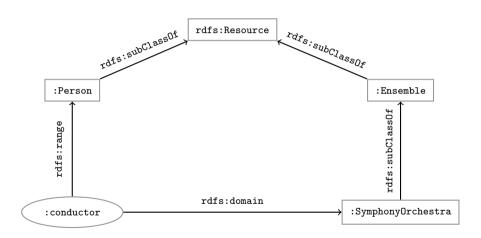
```
:conductor rdfs:domain :SymphonyOrchestra .
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Suppose we have a class hierarchy that includes: :SymphonyOrchestra rdfs:subClassOf :Ensemble . and a property : conductor whose domain and range are: :conductor rdfs:domain :SymphonyOrchestra . :conductor rdfs:range :Person . Now, if we assert :OsloPhilharmonic :conductor :Petrenko . we may infer:

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Now, if we assert
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we may infer:
    :OsloPhilharmonic rdf:type :SymphonyOrchestra .
    :OsloPhilharmonic rdf:type:Ensemble .
    :Petrenko rdf:type :Person .
```

### Conductors and ensembles



#### Consider once more the dataset:

```
:Arild :profAt :UiO .
:Audun :fundBy :UiO .
:Steve :conTo :OLF .
:Trond :recSchol :BI .
:Jenny :tenAt :SSB .
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:Freelancer rdf:type rdfs:Class .
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## Finding the freelancers

The class of freelancers is generated by the rdfs2 rule,

```
:ConTo rdfs:domain :Freelancer . :Steve :conTo :OLF . :Steve rdf:type :Freelancer
```

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The class of freelancers is generated by the rdfs2 rule,

```
:conTo rdfs:domain :Freelancer . :Steve :conTo :OLF . rdfs2
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and may be used as a type in SPARQL (reasoner presupposed):

```
Finding the freelancers

SELECT ?freelancer WHERE {
    ?freelancer rdf:type :Freelancer .
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```

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• ... (another 30 or so)

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- In OWL, there are some simplification which make this superfluous.

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## Outline

1 Inference rules

2 RDFS Basics

Open world semantics

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This is the most important difference between relational DBs and RDF.

## Ramifications

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• (It is not possible to in RDFS to say that ex: Smoker and ex:nonSmoker are disjoint).

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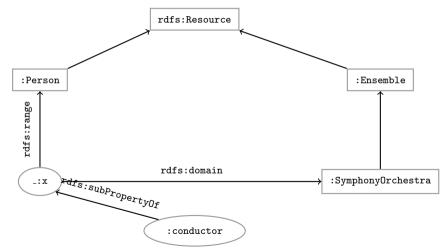
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### Therefore,

- RDFS supports no reasoning services that require consistency-checking.
- If consistency-checks are needed, one must turn to OWL.
- More about that in a few weeks.

## A conspicuous non-pattern

Suppose we elaborate on our music example in the following way:



#### That is:

- We make :conductor a subproperty of \_:x,
- \_:x is a generic relation between people and orchestras,
- to be used whenever we want the associated restrictions.

We would then want to be able to reason as follows (names abbreviated):

■ :Oslo :cond :Abadi . - P

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- 3 :Oslo \_:x :Abadi . rdfs7, 1, 2
- 4 \_:x rdfs:domain :Person . P
- 3 :Abadi rdfs:type :Person . rdfs2, 3, 4

## Contd.

- However, we cannot use rdfs2 and rdfs7 in this way,
- since it requires putting a blank in predicate position,
- which is not legitimate RDF.
- Hence, the conclusion is not derivable.

#### Nevertheless.

- this really is a semantically valid inference,
- ... you are hereby encouraged to check this for yourself,
- whence the RDFS rules are incomplete wrt. RDFS semantics.

## Assessing the situation

RDFS reasoners usually implement only the standardised incomplete rules, so

• they do not guarantee complete reasoning.

#### Better therefore;

- if all you need is the three RDFS reasoning patterns,
- to use OWL and OWL reasoners instead.

#### Unless, of course

- you need to talk about properties and classes as objects,
- that is, you need the meta-modelling facilities of RDFS,
- but people rarely do.

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- It is when we have large knowledge bases and we can apply thousands or millions of derivations that the reasoning becomes really interesting.
- Example of large ontology, SNOMED: http://browser.ihtsdotools.org/?.
- OWL will also allow us to express more complex statements and use more complex types of reasoning.

That's it for today!

Remember the oblig!