

## Tutorial on Frequency Response

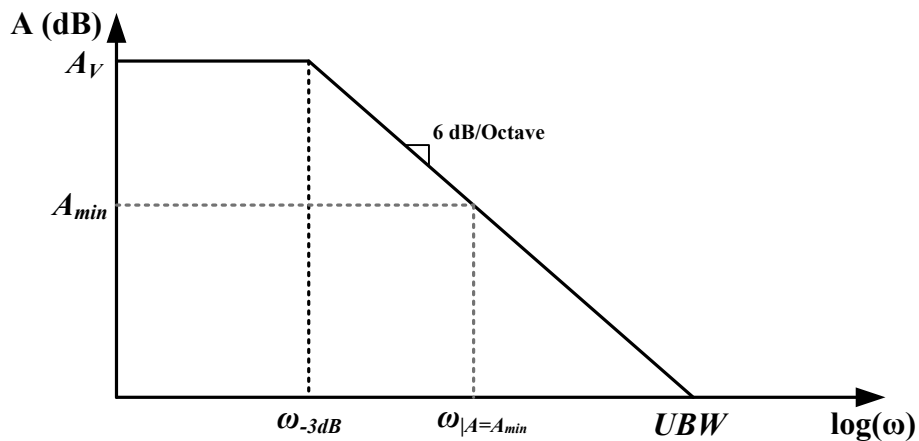
$$A_V = g_m R_o$$

$$\omega_{-3dB} = \frac{1}{C_o R_o}$$

At  $A = A_V$ ,

$$\text{Gain Bandwidth Product (GBW)} = A_V \cdot \omega_{-3dB} = \frac{g_m}{C_o}$$

We can also draw the Bode plot,



For a single-pole system, when  $\omega > \omega_{-3dB}$ , it is defined that A decreases 6dB/octave (which is not 100% true, see the appendix). This means A decreases by two when  $\omega$  increases by two and GBW is a constant when  $\omega > \omega_{-3dB}$ .

At  $A = A_{min}$ ,

$$\text{GBW} = A_{min} \cdot \omega_{|A=A_{min}} = \frac{g_m}{C_o}$$

$$\rightarrow \omega_{|A=A_{min}} = \frac{g_m}{C_o \cdot A_{min}}$$

At  $A = 1$  (i.e. 0dB),

$$\text{GBW} = 1 \times \text{Unity Gain Bandwidth (UBW)} = \frac{g_m}{C_o}$$

With the information above, you should be able to design the comparators.

## Appendix

For a single-pole system,

$$A(s) = \frac{A_V}{\sqrt{1 + \frac{s}{\omega_{-3dB}}}}$$

The magnitude is given by:

$$|A(j\omega)| = \frac{A_V}{\sqrt{1 + \left(\frac{\omega}{\omega_{-3dB}}\right)^2}}$$

$$\log |A(j\omega)| = \log A_V - \frac{1}{2} \log \left( 1 + \left(\frac{\omega}{\omega_{-3dB}}\right)^2 \right)$$

$$20 \cdot \log |A(j\omega)| = 20 \cdot \log A_V - 10 \cdot \log \left( 1 + \left(\frac{\omega}{\omega_{-3dB}}\right)^2 \right)$$

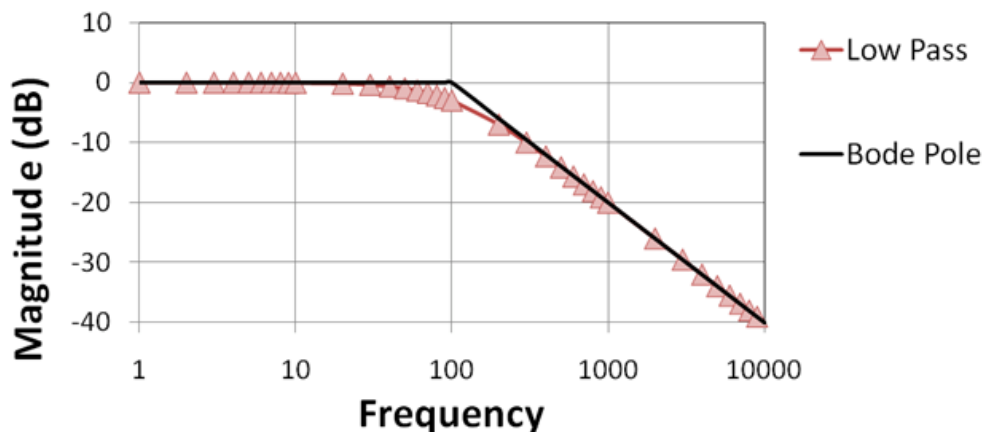
At  $\omega = \omega_{-3dB}$ ,  $20 \cdot \log |A(j\omega)| = 20 \cdot \log A_V - 3\text{dB}$

When  $\omega \gg \omega_{-3dB}$ ,  $20 \cdot \log |A(j\omega)| = 20 \cdot \log A_V - 10 \cdot \log \left(\frac{\omega}{\omega_{-3dB}}\right)^2$

$$20 \cdot \log |A(j\omega)| = 20 \cdot \log A_V - 20 \cdot \log \left(\frac{\omega}{\omega_{-3dB}}\right)$$

which means when  $\omega$  increases by 2, the gain decreases by 6dB.

The gain decreases by 6dB when  $\omega \gg \omega_{-3dB}$ .



(From Wikipedia, [http://upload.wikimedia.org/wikipedia/commons/c/cc/Bode\\_Low-Pass.PNG](http://upload.wikimedia.org/wikipedia/commons/c/cc/Bode_Low-Pass.PNG))

Should be Bode Plot, not Bode Pole)