



Oversampling Data Converters

Tuesday, March 15th, 9:15 - 11:40

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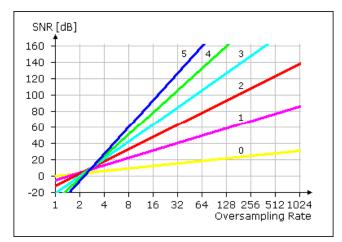
Last time – and today, Tuesday 15th of March: Last time:

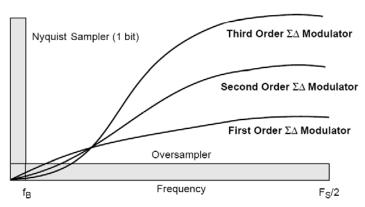


- 12.3 Switched Capacitor Amplifiers
- 12.4 Switched Capacitor Integrator

Today, from chapter 14 in "J. & M.":

- 14.1 Oversampling without noise shaping
- 14.2 Oversampling with noise shaping
- 14.3 System Architectures
- 14.4 Digital Decimation Filters
- 14.5 Higher-Order Modulators
- (14.6 Bandpass Oversampling Converters)
- 14.7 Practical Considerations
- 14.8 Multi-bit oversampling converters2nd order sigma delta design example





Note: Higher order Noise Shaper has less baseband noise

Oversampling converters (chapter 14 in 19

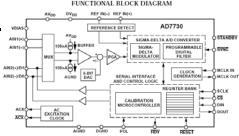


 For high resolution, low-to-medium-speed applications like for example digital audio



- Relaxes requirements placed on analog circuitry, including matching tolerances and amplifier gains
- Simplify requirements placed on the analog antialiasing filters for A/D converters and smoothing
 filters for D/A converters.
- Sample-and-Hold is usually not required on the input
- Extra bits of resolution can be extracted from converters that samples much faster than the Nyquist-rate. Extra resolution can be obtained with lower oversampling rates by exploiting noise shaping

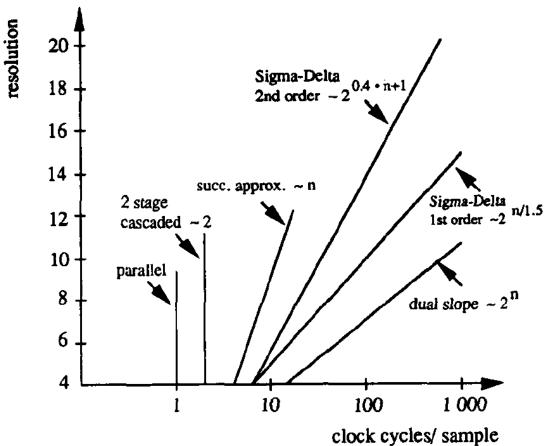








Resolution and clock cycles per same



. Dependence of achievable resolution and required clock cycles per sample for various ADC systems.

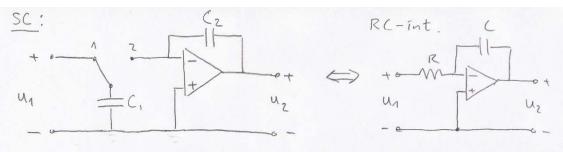
IEEE JOURNAL OF SOLID-STATE CIRCUITS, VOL. 27, NO. 10, OCTOBER

A Gigasample/Second 5-b ADC with On-Chip Track and Hold Based on an Industrial 1-μm GaAs MESFET E/D Process

Transfer function for simple discrete time integrator







Svitsjen er ved tidspunkt t = (n-1)TT posisjon 1, og det blin tatt en punktprove ("et sampel") au u, (t) da C. blir ladet til:

$$q_1 \left[\left(n-1 \right) T \right] = \left(1 \cdot u_1 \left[\left(n-1 \right) T \right] \right]$$

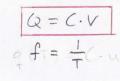
Ladningen på (z er (samtidig):

$$q_2[(n-1)T] = (2 \cdot u_2[(n-1)T]$$

Ved tidspunkt t= n.T blir ladningen på C, overfort til C, ved at suitsjen er i posisjon 2.

tlete ladningen på (, blir ført over til Cz fordi operasjonsforst.

tvinger spenningen over (, til å bli null. H(z)= - (1) = - (1) = - (1) = - (1)



Ladn, pa C1 dermed fra lada. Nils Haaheim: Analog (MOS Universitetet i Trandheim -NTH , 1994

Ladn. på (z ved t=nT blir dermed:

$$q_{2}[nT] = q_{2}[(n-1)T] - q_{1}[(n-1)T]$$

 $C_2 \cdot u_z[nT] = C_z \cdot u_z[(n-1)T] - C_1u_1[(n-1)T]$

$$u_2[nT] = u_2[(n-1)T] - \frac{C_1}{C_2} \cdot u_1[(n-1)T]$$

Kan benytte Z-transform

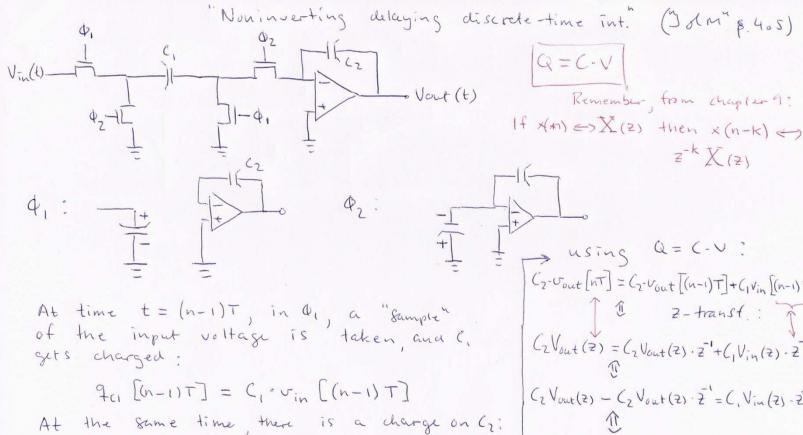
 $\Leftrightarrow z^k X(z)$

$$U_{z}(z) = U_{z}(z) \cdot z^{-1} - \frac{c_{1}}{c_{2}}U_{1}(z) z^{-1}$$

$$|z| = \frac{C_2}{C_1} = \frac{C_2}{C_1} = \frac{C_2}{C_2} = \frac{C_2}{C_1}$$

Transfer function not dependent on Cp1: (Circuit in Fig. 10.9)





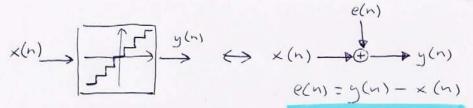
9cz [(n-1) T] = Cz. Vout [(n-1) T]

9cz [nT] = 9cz [(n-1)T] + 9cz [(n-1)T] -

Z-K X (2) (2-Vout [nT] = (2-Vout [(n-1)T]+(1Vin [(n-1)T] (2 Vout(2) - (2 Vout(2) - 2 = (Vin(2) - 2 (2 Vout(2) (1-2) = (,Vin(2).2) At time t= nT the charge on (, is transmitted H(z) = Vout(z) = C, Z

QUANTIZATION

The quantization voise is the difference between the input and output values.



This model is exact under the assumption that the quantization armor is strongly related to the input signal (") d m" p. 532) The model becomes approximate when consumptions are made about the statistical properties of e(n), such as e(n) being an independent white-noise signal. This model leads to a simpler undertunding of ZD and with some exceptions is usually reasonably accurate,

- If x(n) is very active, e(n) can be approximated as an incependent random number uniformly distributed between ± 2, where A equals the difference between two adjacent

quantization levels. Thus the quantization noise power equals (Sec. 11.3) and is independent of the Sampling frequency fs

The spectral density of e(n) S. (f) is white (constant over freq.) and all its power within + fs/2, as shown in the figure?

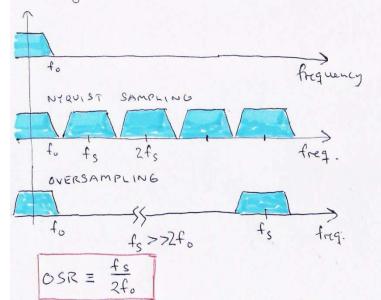
$$\frac{-\frac{fs}{2}}{-\frac{fs}{2}}$$

$$\int_{-\frac{fs}{2}}^{\frac{fs}{2}} S_e^2(f) df = \int_{-\frac{fs}{2}}^{\frac{fs}{2}} K_x^2 df = (K_x)^2 f_s = \frac{\Delta}{12}$$

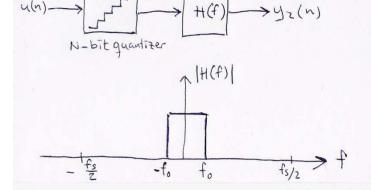
$$K_z = \frac{\Delta}{\sqrt{n}} \sqrt{\frac{fs}{fs}}$$

The spectral density height is calculated by noting that the total noise power is 62/12 and with a two - sided det of power equals the area under Se(f) within +/- fs/2

signal of interest is bandlimited to to



After quantization, y, (n) is filtered by H(f) to create yz (n) that eliminates quantization norse (together with any other signals) greater than fo.



If the input is sinusoidal, its maximum peak value without clipping is $2^{N}(\Delta/2)$ For this wave the signal power, P_{s} , has a power equal to $P_{s} = \left(\frac{\Delta 2^{N} + 1}{2}\right)^{2} = \frac{\Delta^{2} 2^{N}}{8}$

The power of the input signal within yz(n) remains the same as before since we assumed the signal's frequency content is below to.

HOWEVER, THE QUANTIZATION NOISE POWER IS
REDUCED TO

for

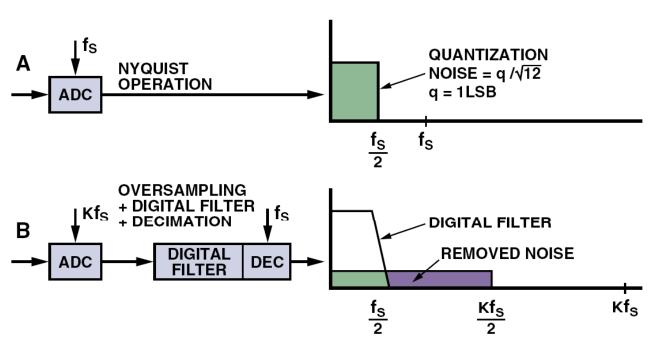
$$P_{e} = \int_{0}^{4s/2} S_{e}^{2}(f) |H(f)|^{2} df = \int_{0}^{2s} k_{x}^{2s} df$$

$$= \frac{2f_{0}}{f_{0}} \cdot \frac{\Delta^{2}}{12} = \frac{\Delta^{2}}{12} \left[\frac{1}{0SR} \right]$$

THEREFORE, DOUBLING OSR DECREASES
THE QUANTIZATION NOISE POWER BY ONEHALF, OR EQUIVALENTLY, 3 dB (or equiv. OSbits)

SNR_{max} = 10 log
$$\left(\frac{Ps}{Pe}\right)$$
 = 10 log $\left(\frac{3}{2}2^{2N}\right)$ + 10 log (65R)
= 6.02N + 1.76 + 10 log (05R) [dB]
due to N-vit quantiter due to oversampling

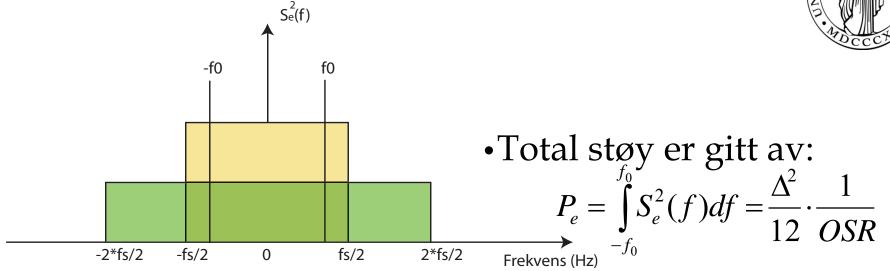
Nyquist Sampling and Oversampling



- Figure from [Kest05]
- Straight oversampling gives an SNR improvement of 3 dB / octave
- $fs > 2f_0 (2f_0 = Nyquist Rate)$
- OSR = $f_s/2f_0$
- SNRmax = 6.02N+1.76+ 10log (OSR)

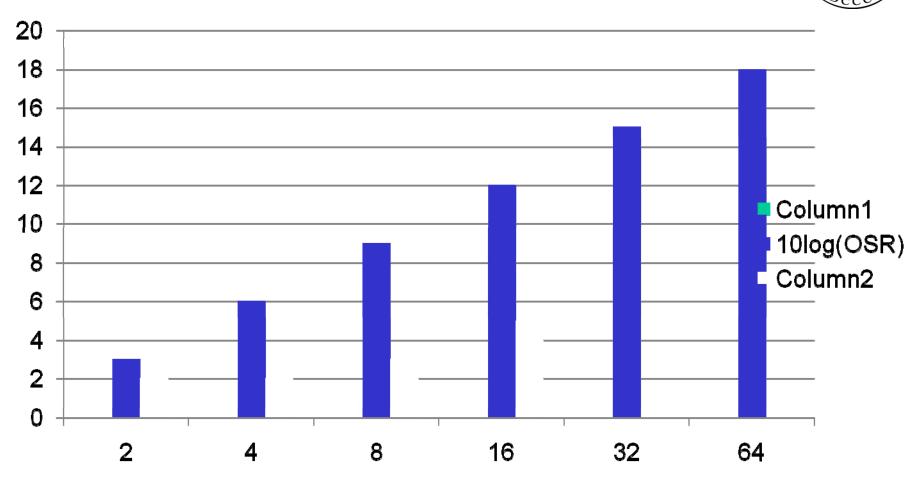
Oversampling (without noise shaping)





- Doubling of the sampling frequency increases the dynamic range by 3 dB = 0.5 bit.
- To get a high SNR a very high fs is needed → high power consumption.
- Oversampling usually combined with noise shaping and higher order modulators, for higher increase in dynamic range per octave ("OSR")

SNRmax = 6.02N+1.76+10log(OSR) [dB] SNR improvement 0.5 bits / octave



EXAMPLE 14.3

Given that a 1-bit A/D converter has a 6-dB SNR, what sample rate is required using oversampling (no noise shaping) to obtain a 96-dB SNR (i.e., 16 bits) if $f_0 = 25$ kHz? (Note that the input into the A/D converter has to be very active for the white-noise quantization model to be valid—a difficult arrangement when using a 1-bit quantizer with oversampling without noise shaping).

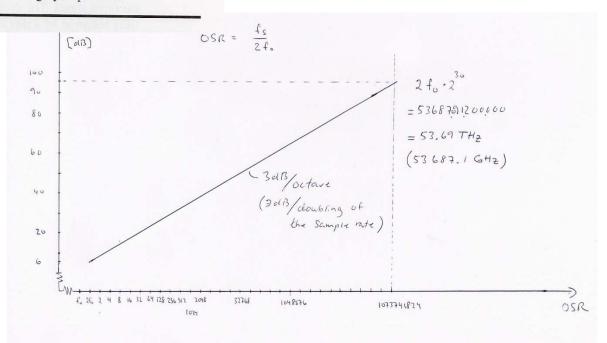
Solution

Oversampling (without noise shaping) gives 3 dB/octave where 1 octave implies doubling the sampling rate. We require 90 dB divided by 3 dB/octave, or 30 octaves. Thus, the required sampling rate, $f_{\rm s}$, is

$$f_s = 2^{30} \times 2f_0 \cong 54,000 \text{ GHz}!$$

This example shows why noise shaping is needed to improve the SNR faster than 3 dB/octave, since 54,000 GHz is highly impractical.



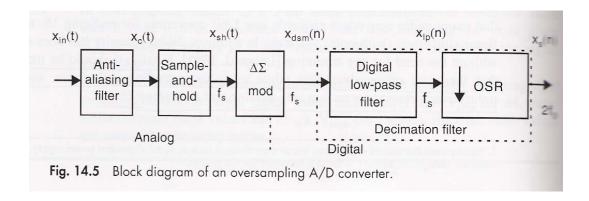


Advantages of 1-bit A/D converters (p.537 in "J&M"

- Oversampling improves signal-to-noise ratio, but not linearity
- Ex.: 12-bit converter with oversampling needs component accuracy to match better than 16-bit accuracy if a 16-bit linear converter is desired
- Advantage of 1-bit D/A is that it is inherently linear. Two points define a straight line, so no laser trimming or calibration is required
- Many audio converters presently use 1-bit converters for realizing 16- to 18-bit linear converters (with noise shaping).

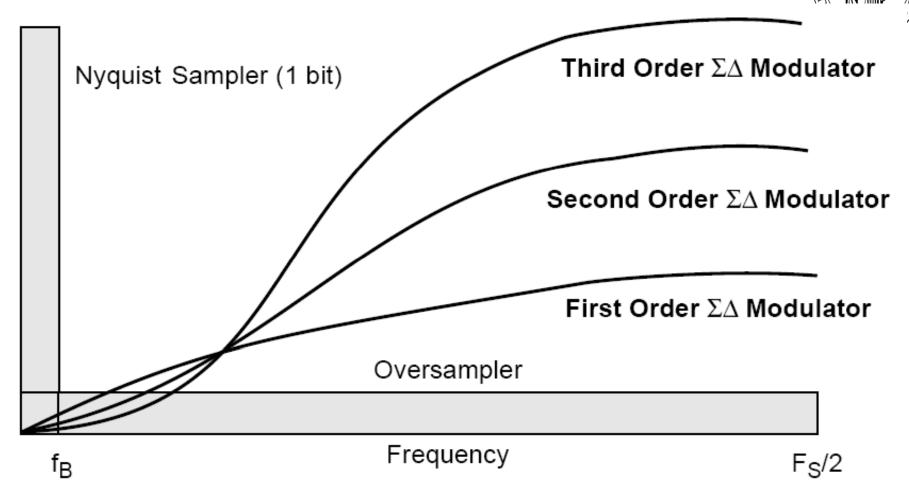
Oversampling with noise shaping

- Oversampling combined with noise shaping can give much more dramatic improvement in dynamic range each time the sampling frequency is doubled.
- The sigma delta modulator converts the analog signal into a noise-shaped low-resolution digital signal.
- The decimator converts to a high resolution digital signal



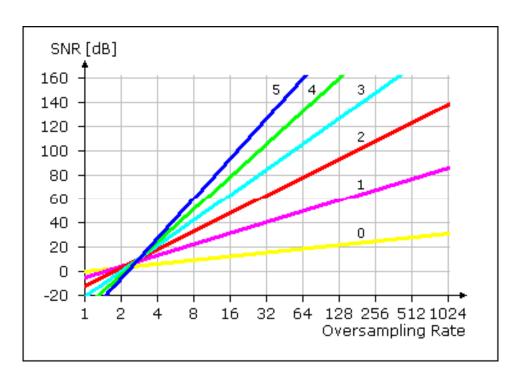
Multi-order sigma delta noise shapers

Park, Motorola)



Note: Higher order Noise Shaper has less baseband noise

Ex. 14.5 "point":



- 2 X increase in M→
 (6L+3)dB or (L+0.5) bit increase in DR.
- L: sigma-delta order
- 6 db Quantizer, for 96 dB SNR:
- Plain oversampling: f_s=54
 GHz
- 1st order : f_s=75.48 MHz
- 2nd order: $f_s = 5.81 \text{ MHz}$

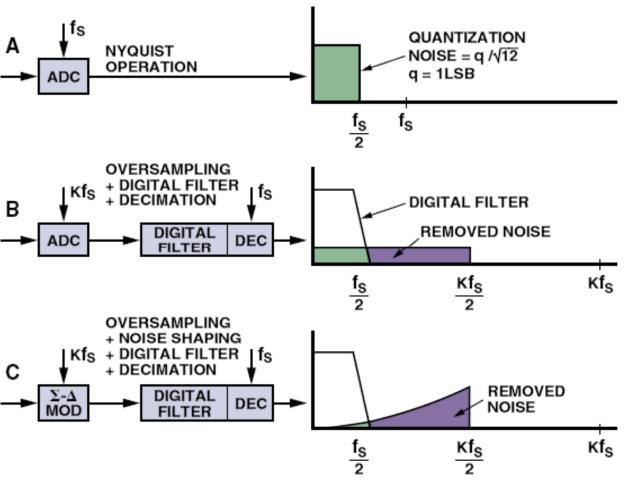
3 a) (Weight 10 %)

A sampled signal is bandlimited to $f_0 = 22$ kHz. What is the sampling frequency, f_s , for an oversampling ratio ("OSR") of 128?

A 1-bit analog-to-digital converter ("ADC") has an inherent 6-dB SNR. Which maximum SNR is acquired by combining it with strict oversampling and an OSR of 128, if no noise shaping is used? What is the maximum SNR in the similar case exploiting 2nd order noise shaping?

If a 1-bit ADC using 3rd order noise shaping has a maximum SNR of 125 dB for an OSR of 128, what is the expected maximum SNR if the OSR is reduced to 32?

Nyquist Sampling, Oversampling, Noise Shaping



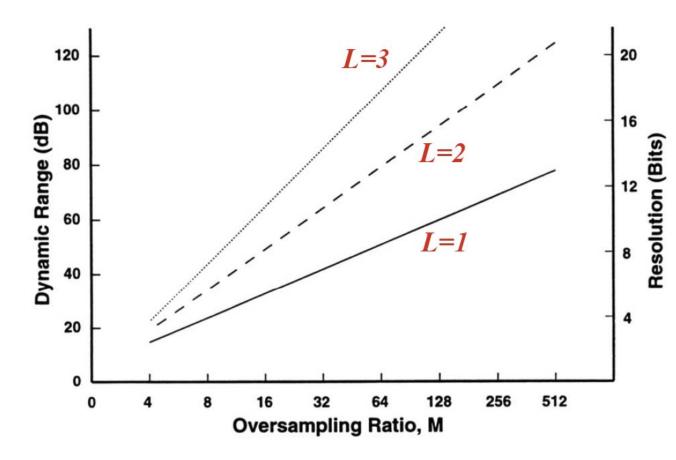
- Figure from [Kest05]
- Straight oversampling gives an SNR improvement of 3 dB / octave

nano

- $fs > 2f_0 (2f_0 =$ Nyquist Rate
- $OSR = f_s/2f_0$
- SNRmax = 6.02N+1.76+ 10log (OSR)

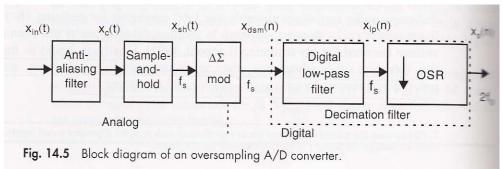
OSR, modulator order and Dynamic Range





- 2 X increase in M → (6L+3)dB or (L+0.5) bit increase in DR.
- L: sigma-delta order
- Oversampling and noise shaping

14.2 Oversampling with noise shaping



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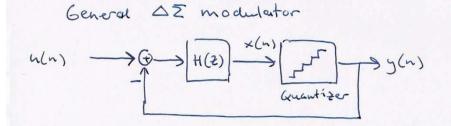


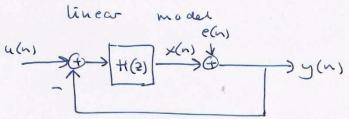
- The continous time signal x_c(t) is sampled by a S/H (not necessary with separate S/H in Switched Capacitor impl.)
- The Delta Sigma modulator converts the analog signal to a noise shaped low resolution digital signal
- The decimator converts the oversampled low resolution digital signal into a high resolution digital signal at a lower sampling rate usually equal to twice the desired bandwidth of the desired input signal (conceptually a low-pass filter followed by a downsampler).

Noise shaped Delta Sigma Modulator









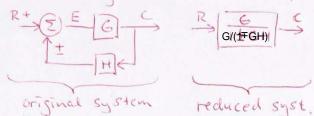
The linear model can be treated as having two independent inputs (which is an approximation).

Signal:

$$u(n) \xrightarrow{+} \bigoplus H(z) \longrightarrow y(n)$$

Noise:

BLUCK DIAGRAM ALGEBRA, Cathey & Nasar P. 292; eliminating a terdback loop:



Signal transfer function, STF (2):

$$S_{TF}(z) = \frac{V(z)}{V(z)} = \frac{H(z)}{1 + H(z)}$$

Noise transfer function, NTF (2):

$$N_{TF}(z) \equiv \frac{F(z)}{F(z)} = \frac{1}{1+H(z)}$$

The output is the combination of the input and noise: Y(z)=S_F(z)U(z)+N_F(z)E(z)

First-Order Noise Shaping (Figures from Schreier & Temes '05)

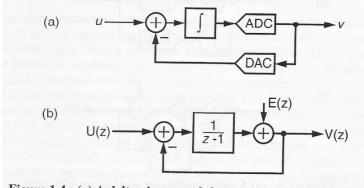


Figure 1.4: (a) A delta-sigma modulator used as an ADC and (b) its linear z-domain model.

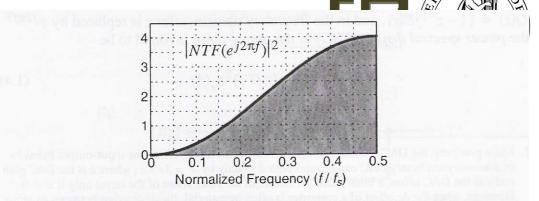
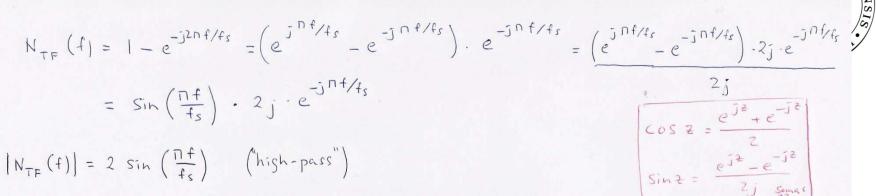


Figure 1.5: Noise-shaping function for the $\Delta\Sigma$ modulator shown in Fig. 1.4.

- $S_{TF}(z) = [H(z)/1+H(z)]$ (eq. 14.15) $N_{TF}(z) = [1/1+H(z)]$
- $Y(z) = S_{TF}(z) U(z) + N_{TF}(z) E(z)$
- H(z) = 1/z-1 (discrete time integrator) gives 1st order noise shaping
- $S_{TF}(z) = [H(z)/1+H(z)] = 1/(z-1)/[1+1/(z-1)] = z^{-1}$
- $N_{TF}(z) = [1/1+H(z)] = 1/[1+1/(z-1)] = (1-z^{-1})$
- The signal transfer function is simply a delay, while the noise transfer function is a discrete-time differentiator (i.e. a high-pass filter)

14.2 Oversampling with noise shaping 📙 🚝





Quantization noise power over the frequency band 0 to fo is now given by $P_{e} = \int_{0}^{\infty} S^{2}e(f) \cdot |N_{TF}|^{2} df = \int_{0}^{\infty} \left(\frac{\Delta^{2}}{12}\right) \frac{1}{f_{s}} \left[2 \sin\left(\frac{\pi f}{f_{s}}\right)\right] df \qquad (14.23)$

Making the approximation that $f_0 < \zeta f_s$ (OSR >> 1) so that $\sin\left(\frac{\Pi f}{f_s}\right) \approx \frac{\Pi f}{f_s}$: $P_{e} = \left(\frac{\Delta^{2}}{12}\right)\left(\frac{\Pi^{2}}{3}\right)\left(\frac{2f_{0}}{f_{0}}\right)^{3} = \frac{\Delta^{2}\Pi^{2}}{36}\left(\frac{1}{0SR}\right)^{8}, \quad OSR = \frac{f_{S}}{2f_{0}}$

It is assumed that the maximum signal power is the same as obtained before, in equation 14.11 ($P_s = \Delta^2 2^{2N}/8$), making maximum SNR:

$$SNR_{max} = 10 log \left(\frac{P_s}{P_e}\right) = 10 log \left(\frac{3}{2} \cdot 2^{2N}\right) + 10 log \left(\frac{3}{D^2} \left(0 SR\right)^3\right), or$$

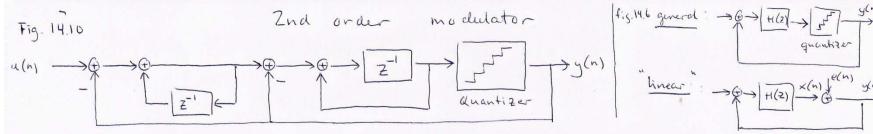
SNRmax = 6.02 N + 1.76 - 5.17 + 30 log (OSR)

Doubling the OSR gives an SNR improvement for a 1st order modulator of 9 01B/octave or equiv. 1.5 bits/octave.

Quantization noise power for linearized model of a general $\Delta \Sigma$ modulator

15. mars 2011

Second-order noise shaping LC:



The above modulator realizes 2nd order noise shaping. fig. 14.11:
The signal transfer function is given by

The noise transfer function is given by $N_{TF}(f) = (1 - z')^{2}$

Magnitude:
$$|N_{TF}(f)| = \left[2 \sin\left(\frac{\pi f}{fs}\right)\right]^2$$

The quantitation noise power over the frequency band of interest: $Pe = \frac{\Delta^2 \Pi^4}{60} \left(\frac{1}{05R} \right)^5$

Max Sur:
SNR_{max} = 10 log
$$\left(\frac{P_S}{P_E}\right)$$
 = 10 log $\left(\frac{3}{2}2^{2N}\right)$ + 10 log $\left(\frac{5}{11}4\left(0SR\right)^{\frac{1}{2}}\right)$

Ex. 14.5 p. 545: 1-bit A/D, 6-bit SUR. fo = 25 kHz 96 dB SUR is the good. Sample rated needed? -oversampling: 54 THz -1st order n.s.: 75 MHz -2nd order n.s.: 58 MHz

Ast order noise

/ noise shaping

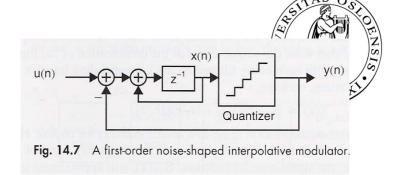
INTE (f)

Given that a 1-bit A/D converter has a 6 dB SNR, which sample rate is required to obtain a 96-dB SNR (or 16 bits) if f₀ = 25 kHz for straight oversampling as well as first-and second-order noise shaping?

- Oversampling with noise shaping: From ex. 14.3 we know that straight oversampling requires a sampling rate of 54 THz.
- (6.02N+1.76+10 log
 (OSR) = 96
 <->
 6 + 10 log OSR = 96)
 <-> 10 log OSR = 90

$$SNR_{max} = 6.02N + 1.76 - 5.17 + 30 \log(OSR)$$
 (14.26)

We see here that doubling the OSR gives an SNR improvement for a first-order modulator of 9 dB or, equivalently, a gain of 1.5 bits/octave. This result should be compared to the 0.5 bits/octave when oversampling with no noise shaping.



- Oversampling with 1st order noise shaping:
- 6 5.17 + 30 $\log(OSR) = 96$ $OSR = f_s / 2f_0$
- $30\log(OSR) = 96 6 + 5.17 = 95.17$

A doubling of the OSR gives an SNR improvement of 9 dB / octave for a 1st order modulator;

95.17 / 9 = 10.57
$$2^{10.56}$$
 x 2^*25 kHz = 75.48 MHz

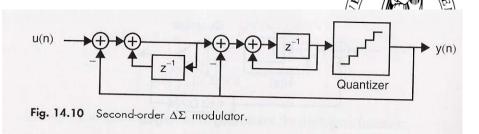
OR: $log(OSR) = 95.17/30 = 3.17 \rightarrow OSR = 1509.6$

1509.6 * (2*25kHz) = 75.48 MHz

$$SNR_{max} = 6.02N + 1.76 - 12.9 + 50 \log(OSR)$$
 (14.)

We see here that doubling the OSR improves the SNR for a second-order mod lator by 15 dB or, equivalently, a gain of 2.5 bits/octave.

The realization of the second-order modulator using switched-capacitor ter niques is straightforward and is left as an exercise for the interested reader.



- Oversampling with 2nd order noise shaping:
- $6 12.9 + 50 \log(OSR) = 96$

$$OSR = fs / 2f_0$$

 $50 \log (OSR) = 96 - 6 + 12.9 = 102.9$

A doubling of the OSR gives an SNR improvement of 15 dB / octave for a 2nd order modulator;

$$102.9 / 15 = 6.86$$
 $2^{6.86} \times 2^*25 \text{ kHz} = 5.81 \text{ MHz}$

2nd order sigma delta modulator



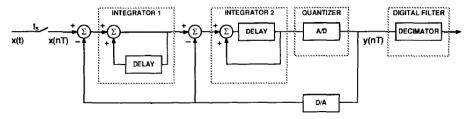


Fig. 1. Block diagram of second-order $\Sigma\Delta$ modulator with decimator.

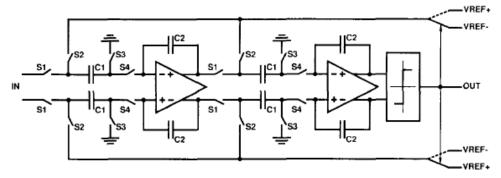


Fig. 10. Second-order $\Sigma\Delta$ modulator implementation.

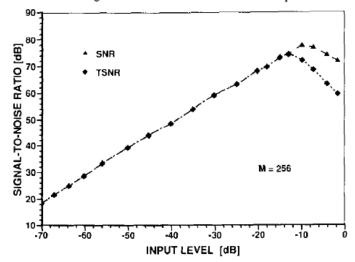


Fig. 13. Measured SNR for a sampling frequency of 4 MHz and a signal frequency of 1.02 kHz.

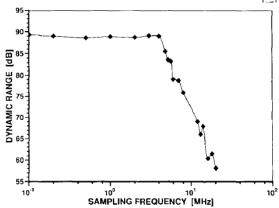
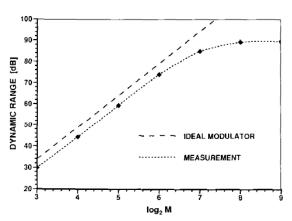


Fig. 14. Maximum operating frequency.



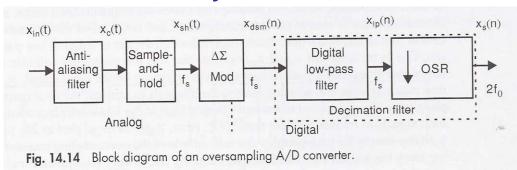
 Dynamic range as a function of the oversampling ratio for a sampling frequency of 4 MHz.

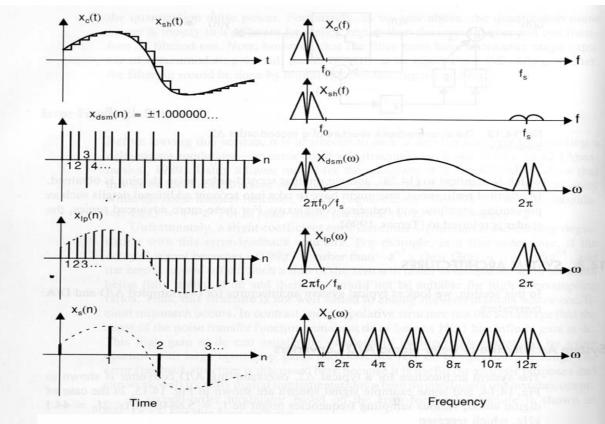
IEEE JOURNAL OF SOLID-STATE CIRCUITS, VOL. 23, NO. 6, DECEMBER 1988

The Design of Sigma-Delta Modulation Analog-to-Digital Converters

BERNHARD E. BOSER, STUDENT MEMBER, IEEE, AND BRUCE A. WOOLEY, FELLOW, IEEE

14.3 System Architectures (A/D)

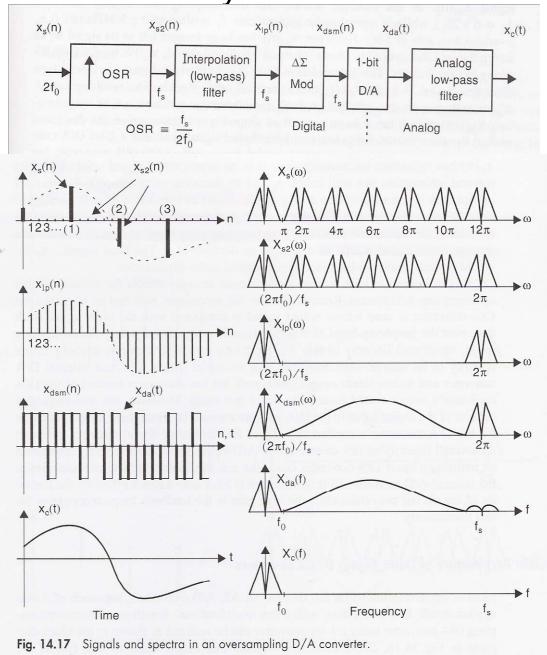






- X_c(t) is sampled and held; resulting in x_{sh}(t).
- x_{sh}(t) is applied to an A/D Sigma Delta modulator which has a 1-bit output, x_{dsm}(n). The 1-bit signal is assumed to be linearly related to the input X_c(t) (accurate to many orders of resolution), although it includes a large amount of out-of-band quantization noise (seen to the right).
- A digital LP filter removes any high frequency content, including out of band quantization noise, resulting in X_{Ip}(n)
- Next, X_{lp}(n) is resampled at 2f₀ to obtain X_s(n) by keeping samples at a submultiple of the OSR

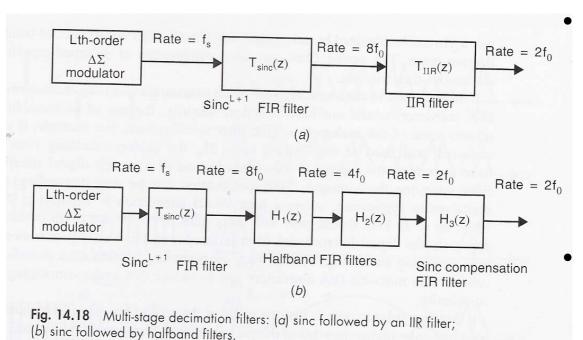
System Architectures (D/A)





- The digital input, X_s(n) is a multi-bit signal and has an equivalent sample rate of 2f₀, where f₀ ,is slightly higher than the highest input signal frequency.
- Since X_s(n) is just a series of numbers the frequency spectrum has normalized the sample rate to 2π.
- The signal is upsampled to an equivalent higher sampling rate, f_s, resulting in the signal x_{s2}(n)
- $x_{s2}(n)$ has images left that are filtered out by the interpolation filter (brick-wall type) to create the multi-bit signal $X_{lp}(n)$, by digitally filtering out the images.
- X_{Ip}(n) is applied to a fully digital sigma delta modulator producing the 1-bit signal, X_{dsm}(n), containing shaped quantization noise.
- X_{dsm}(n) is fed to a 1-bit D/A producing X_{da}(t), which has excellent linearity properties but still quantization noise.
- The desired signal, X_c(t) can be obtained by using an analog filter to filter out the out-of-band quantization noise. (filter should be at least one order higher than the modulator.)

14.4 Digital decimation filters



Many techniques

- a) FIR filter removes much of the quantization noise, so that the output can be downsampled by a 2nd stage filter which may be either IIR type (as in a), uppermost) or a cascade of FIR filters (as in b), below)
- In b) a few halfband FIR filters in combination with a sinc compensation FIR-filter are used.

In some applications, these halfband and sinc compensation filters can be realized using no general multi-bit multipliers [Saramaki, 1990]

14.5 Higher-Order Modulators Interpolative structure

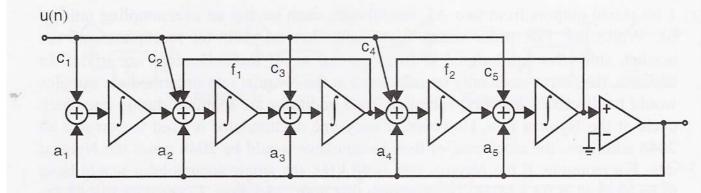
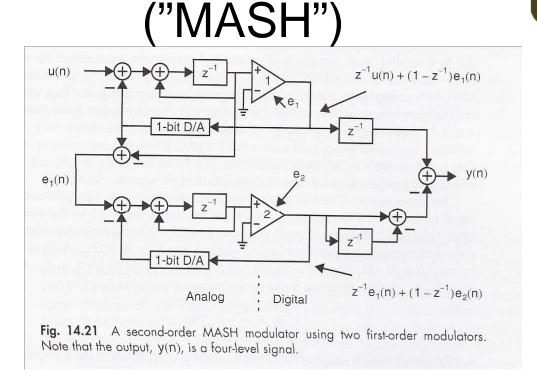


Fig. 14.20 A block diagram of a fifth-order modulator.

- Lth order noise shaping modulators improve SNR by 6L+3dB/octave.
- Typically a single high-order structure with feedback from the quantized signal.
- In figure 14.20 a single-bit D/A is used for feedback, providing excellent linearity.
- Unfortunately, modulators of order two or more can go unstable, especially when large input signals are present (and may not return to stability) Guaranteed stability for an interpolative modulator is nontrivial.

Multi-Stage Noise Shaping architecture



- Overall higher order modulators are constructed using lower-order, more stable, ones → more stable overall system.
- Fig. 14.21: 2nd order using two first-order modulators.
- Higher order noise filtering can be achieved using lower-order modulators.
- Unfortunately sensitive to finite opamp gain and mismatch

14.7 Practical considerations



- Stability
- Linearity of two-level converters

 tor. For this case, the output segments because the same modula-
- Idle tones
- Dithering
- Opamp gain

tor. For this case, the output sequence becomes

$$y(n) = \{1, 1, -1, 1, 1, 1, -1, 1, 1, 1, -1, 1, 1, 1, -1, 1, 1, 1, -1, 1, 1, 1, 1, -1, 1, 1, 1,$$

The period of this output pattern is now 16 cycles long and has some power at $f_s/16$. With an oversampling ratio of eight (i.e., $f_0 = f_s/16$), the post low-pass filter will not attenuate the signal power at f_s/16 since that frequency is just within the frequency band of interest. In other words, a dc level of 3/8 into this modulator will

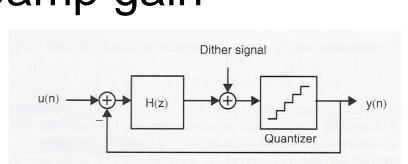


Fig. 14.26 Adding dithering to a delta-sigma modulator. Note that the dithered signal is also noise shaped.



Design example, 14b 2nd order Sigma-Delta mod

Second-Order Sigma Delta
Modulator

Snore Aunet
Email: as Browlein to
Nerdic VLSI
Norreay
May 4, 1994

BOSER AND WOOLEY: SIGMA-DELTA MODULATION ANALOG-TO-DIGITAL CONVERTERS

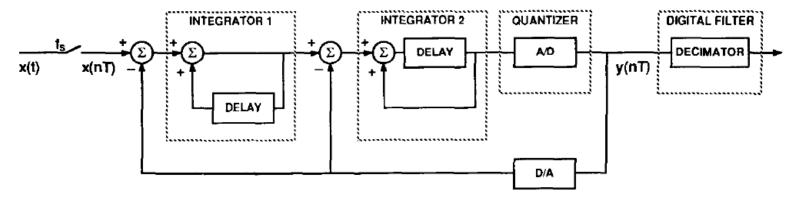


Fig. 1. Block diagram of second-order $\Sigma \Delta$ modulator with decimator.

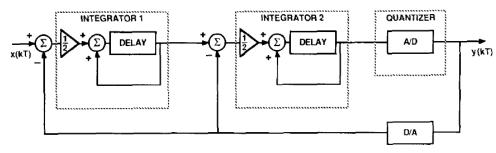


Fig. 2. Modified architecture of second-order $\Sigma\Delta$ modulator.

 16 bit, 24 kHz, OSR as powers of two, and allowing for increased baseband noise due to nonidealities: OSR 512 was chosen

Design example, 14b 2nd order Sigma-Delta mod

- Among most relevant nonidealities:
- Finite DC gain
- Bandwidth,
- Slew rate
- Swing limitation
- Offset voltage
- Gain nonlinearity
- Flicker noise
- Sampling jitter
- Voltage dependent capacitors
- Switch on-resistance
- Offset voltage and settling time for comparators

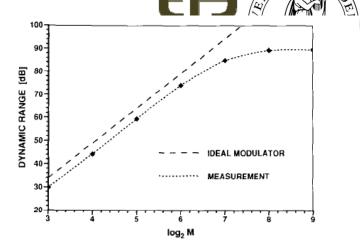
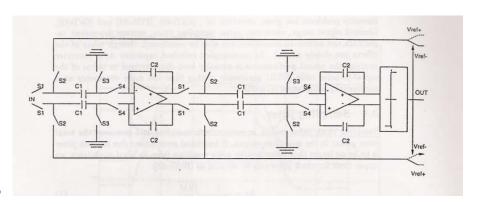
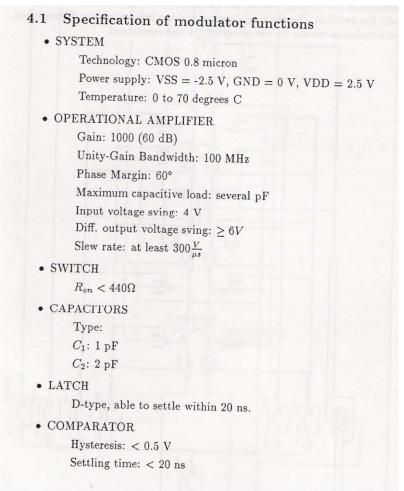
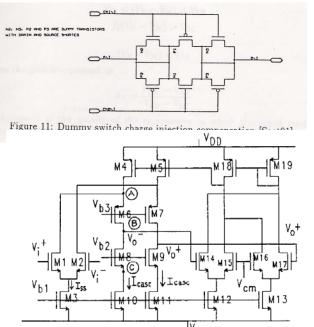


Fig. 15. Dynamic range as a function of the oversampling ratio for a sampling frequency of 4 MHz.



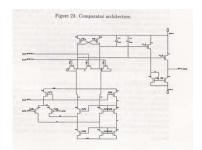
Design example, 14b 2nd order Sigma-Delta mod





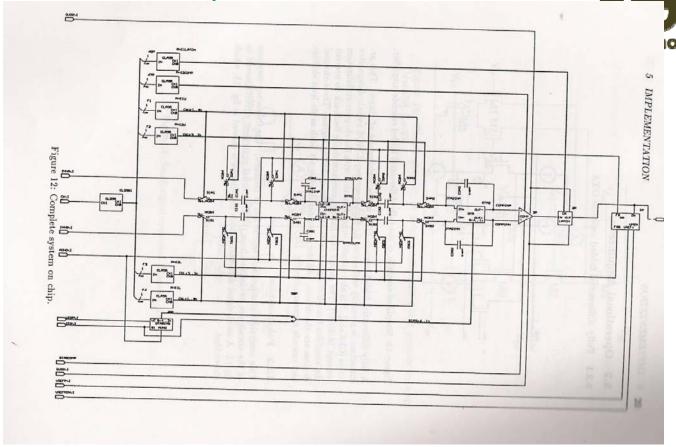
Second-Order Sigma Delta Modulator Snorre Aunet Email: sa@nvlsi.no Nordic VLSI

Fig. 1. Fully differential folded-cascode amplifier (after [4]).



Noninverting parasitic insensitive integrator (fig 10.9) was used (fully differential implementation)

2nd order modulator; top level schematics



• Two-phase clock generator, switches, chopper stabilized OTA (1st int.), OTA (2nd int.- fully differential folded cascode), comparator, latch, two-level DAC. Biasing circuit.

Functional after test.

Sigma Delta converters, ISSCC 2011



SESSION 27

Session Chair:

Associate Chair:

Wednesday February 23rd, 1:30 PM

ISSCC-

OVERSAMPLING CONVERTERS

Foremost global forum

Kong-Pang Pun, Chinese University of Hong Kong, Hong Kong, China Lucien Breems. NXP. Eindhoven. The Netherlands

27.1 A 4GHz CT ΔΣ ADC with 70dB DR and -74dBFS THD in 125MHz BW

M. Bolatkale¹, L. Breems¹, R. Rutten¹, K. Makinwa²

¹NXP Semiconductors, Eindhoven, The Netherlands

²Delft University of Technology, Delft, The Netherlands

"CT": continous time

A 4GHz CT ΣΔ ADC is presented with a loop filter topology that absorbs the pole caused by the input capacitance of its 4b quantizer and compensates for the excess delay caused by the quantizer's latency. Implemented in 45nm CMOS, the ADC achieves 70dB DR and -74dBFS THD in a 125MHz BW, while dissipating 256mW and occupying only 0.9mm².

27.2 An 8mW 50MS/s CT ΔΣ Modulator with 81dB SFDR and Digital 2:00 PM Background DAC Linearization

J. G. Kauffman, P. Witte, J. Becker, M. Ortmanns Ulm University, Ulm, Germany

A 3rd-order single-loop CT $\Delta\Sigma$ modulator with a 4b quantizer is sampled at 500MHz with an OSR of 10. It achieves 63.5dB SNDR and -81dB SFDR in a 25MHz bandwidth without DEM. The DAC nonlinearity is digitally estimated and corrected. All feedback amplifiers are compensated for finite GBW influence. The modulator occupies 0.15mm² in 90nm CMOS and achieves an FOM of 125fJ/conversion-step.

27.3 A Third-Order DT $\Delta\Sigma$ Modulator Using Noise-Shaped Bidirectional Single-Slope Quantizer

N. Maghari, U-K. Moon
Oregon State University, Corvallis, OR

A single-slope quantizer using modified bidirectional discharging is proposed. This quantizer provides first-order shaping of quantization noise and is used as the quantizer of a second-order delta-sigma loop. The fabricated prototype ADC achieves 78.2dB SNDR at 50MHz sampling speed at OSR of 24 with 2.9mW power consumption.

Break 3:00 PM

2:30 PM

1:30 PM

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SESSION 27

Wednesday February 23rd, 1:30 PM

27.4 A 250mV 7.5μW 61dB SNDR CMOS SC ΔΣ Modulator Using a Near-Threshold-Voltage-Biased CMOS Inverter Technique

3:15 PM

F. Michel, M. Steyaert KU Leuven, Leuven, Belgium

An ultra-low-voltage SC $\Delta\Sigma$ converter using a near-threshold-voltage-biasing technique is reported. This guarantees reliable operation of inverter-based integrators over temperature while running at a supply voltage of 250mV. An SNDR of 61dB is achieved for a BW of 10 kHz with a total power consumption of only 7.5 LW.

27.5 A 84dB SNDR 100kHz Bandwidth Low-Power Single Op-Amp Third-Order $\Delta\Sigma$ Modulator Consuming 140 μ W

3:45 PM

A. Pena Perez, E. Bonizzoni, F. Maloberti University of Pavia. Pavia. Italy

A third-order $\Delta\Sigma$ modulator with single operational amplifier achieves 13.6 bits with 100kHz signal bandwidth and consumes 140µW. The time-interleaved two-integrators scheme is a modification of a second-order prototype. A slew-rate boost enables minimum power in a two stages op-amp. The SFDR is 96dB with an FoM of 54fJ/conversion-step.

27.6 A 1.7mW 11b 1-1-1 MASH ΔΣ Time-to-Digital Converter

4:15 PM

4:45 PM

Y. Cao¹², P. Leroux¹³, W. De Cock², M. Steyaert¹

¹KU Leuven, Leuven, Belgium

²SCK-CEN, Mol, Belgium

³KH Kempen, Geel, Belgium

The first radiation tolerant third-order $\Delta\Sigma$ TDC is presented. The converter, implemented in 0.13 μ m CMOS, employs a 1-1-1 MASH architecture. It achieves an ENOB of 11b and a time resolution of 5.6ps, when the OSR is 250. A radiation assessment up to 5MGy proves the TDC's robustness. The TDC core consumes 1.7mW and occupies 0.11mm².

27.7 A 120dB-SNR 100dB-THD+N 21.5mW/Channel Multibit CT ΔΣ DAC

A. Bandyopadhyay, M. Determan, S. Kim, K. Nguyen Analog Devices, Wilmington, MA

A continuous-time 8b oversampling DAC architecture is presented, which measures 120dB of SNR and 100dB of ThD+N while consuming 21.5mW/channel. This performance is achieved by using a 3-level rotational data-shuffling scheme along with analog low-power techniques. The 1.35mm²/channel chip is fabricated in 0.35µm DPQM CMOS process.

27.8 A 108dB-DR 120dB-THD and 0.5V_{rms} Output Audio DAC with Inter-Symbol-Interference-Shaping Algorithm in 45nm CMOS

5:15 PM

L. Risbo¹, R. Hezar², B. Kelleci², H. Kiper², M. Fares²

¹Texas Instruments, Copenhagen, Denmark

²Texas Instruments, Dallas, TX

An oversampled audio multi-bit DAC using a mismatch-shaping algorithm designed to shape element mismatch errors concurrently with inter-symbol-interference is presented. It can achieve THD powers better than -120dBFs with spurious tone free operation at low signal levels. It is implemented in 45nm CMOS with 0.16mm² area, 0.875mW power, and 0.5V_{rms} output.

litterature



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A MICRO POWER SIGMA-DELTA A/D CONVERTER IN 0.35-μM CMOS FOR LOW FREQUENCY APPLICATIONS

Adnan Gundel^{1,2}, William N. Carr¹
Email: adnangundel@icee.org; william.carr@njit.edu



- Ch. 13; Nonlinearity and Mismatch plus beginning of chapter 14; Oscillators (?)
- Messages are given on the INF4420 homepage.

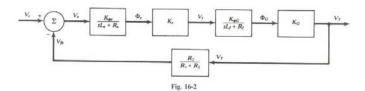
sa@ifi.uio.no
 , 22852703 / 90013264

$$\frac{V_T(s)}{\Phi_G(s)} = K_G$$
(6)

Voltage divider. If the series combination of the exciter field resistance and the reference-command potentiometer resistance is much larger than R_2 , then voltage division is valid and the transfer function relating v_T to v_{th} is

$$\frac{V_{\rho,l}(s)}{V_T(s)} = \frac{R_2}{R_1 + R_2}$$
(7)

The above transfer functions and summer signal have been used to form the (mathematical) block diagram of Fig. 16-2.



16.2 BLOCK DIAGRAM ALGEBRA

For a control system of any complexity, the block diagram will contain many transfer functions in series and parallel arrangements. It is expedient to reduce the block diagram to more tractable form by applying the rules of block diagram algebra, as summarized in Table 16-1.

Table 16-1

Rule	Original System	Reduced System
1. Cascaded blocks	R G_1 A G_2 C	$R \longrightarrow G_1G_2$
2. Parallel paths	G_1 C	R $G_1 \pm G_2$ C
3. Moving a pickoff point	R G C	R G C

292

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BLOCK DIAGRAMS AND SIGNAL FLOW GRAPHS

[CHAP. 16

CASO

Table 16-1 (cont.)

Rule	Original System	Reduced System
4. Moving a summer	$\begin{array}{c} R \\ \hline G \\ \hline \end{array} \begin{array}{c} C \\ \end{array} \end{array} \begin{array}{c} C \\ \end{array} \begin{array}{c$	$\begin{array}{c} R + \sum G \xrightarrow{C} G \xrightarrow{A} \\ \downarrow $
5. Eliminating a feedback loop	R + \(\S\) E \(\G\)	R G C 1 = GH

The original system of Rule 5 exhibits the canonical form into which any control system with feedback can be transformed.

Example 16.2 Reduce the block diagram of Fig. 16-3(a) to a single block.

Move the pickup point for feedback signal W(s) from the left to the right of block C(s), using Rule 3. The result is shown in Fig. 16-3(b).

Combine cascaded (series-connected) blocks in the forward and feedback paths by Rule 1, giving the reduced block diagram of Fig. 16-3(c).

Finally, the simple negative feedback loop is eliminated by Rule 5, to yield the diagram of Fig. 16-3(d).

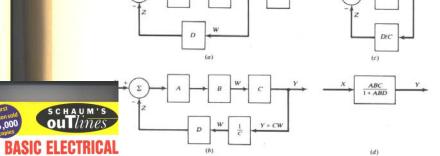


Fig. 16-3

15. mars 2011