— INF4820 — Algorithms for AI and NLP

Classification

Erik Velldal & Stephan Oepen

Language Technology Group (LTG)

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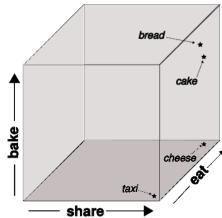
Summing up the previous lecture



- ► Semantic spaces: Vector space models for distributional semantics.
- ▶ Words are represented as points/vectors in a feature space, positioned by their co-occurrence counts for various context features.
- ► For each word, extract context features across a corpus.
- ► Let each feature type correspond to a dimension in the space.

▶ Each word o_i is represented by a (length-normalized) n-dimensional feature vector $\vec{x}_i = \langle x_{i1}, \dots, x_{in} \rangle \in \Re^n$.

- ► We can now measure, say, the Euclidean distance of words in the space, $d(\vec{x}, \vec{y})$.
- ► Semantic relatedness ≈ distributional similarity ≈ spatial proximity



An aside: Term-document spaces for IR



- ► So far we've looked at vector space models for detecting *words* with similar *meanings*.
- ▶ It's important to realize that vector space models are widely used for other purposes as well.
- ► For example, vector space models are commonly used in IR for finding documents with similar content.
- ▶ Each document d_j is represented by a feature vector, with features corresponding to the terms t_1, \ldots, t_n occurring in the documents.
- Spatial distance \approx similarity of content.
- ► Can also represent a search query as a vector:
- ▶ The relevance of a documents given by their distance to the query.

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Today's main topic



- ► Machine learning: Classification
- ► Representing classes and membership
- ► Rocchio classifiers
- ► *k*NN classifiers

Two categorization tasks in machine learning



Clustering

- ► Unsupervised learning from unlabeled data.
- ► Automatically group similar objects together.
- ► No predefined classes or structure, we only specify the similarity measure. Relies on "self-organization".
- ► (The topic for the next lectures.)

Classification

- ► Supervised learning, requiring labeled training data.
- ► Train a classifier to automatically assign *new* instances to *predefined* classes, given some set of examples.
- ► (Topic for today.)

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Classification



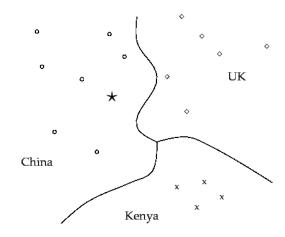
Some examples of classification tasks

- ► Named entity recognition
- ► Document (topic) classification
- ► Authorship attribution
- ► Sentiment analysis
- ► Spam filtering
- ► We'll look at two simple examples of vector space classifiers:
 - ► Rocchio
 - ► kNN

Classes and classification



- ▶ A class can simply be thought of as a collection of objects.
- ▶ In our vector space model, objects are represented as *points*, so a class will correspond to a collection of points; a region.
- ► Vector space classification is based on the the contiguity hypothesis:
- Objects in the same class form a contiguous region, and regions of different classes do not overlap.
- Classification amounts to computing the boundaries in the space that separate the classes; the decision boundaries.
- ► How we draw the boundaries is influenced by how we choose to represent the classes.



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Different ways of representing classes



Exemplar-based

- ► No abstraction. Every stored instance of a group can potentially represent the class.
- ▶ Used in so-called *instance based* or *memory based learning* (MBL).
- ► In its simplest form; the class = the collection of points.
- ► Another variant is to use *medoids*, representing a class by a single member that is considered central, typically the object with maximum average similarity to other objects in the group.

Centroid-based

- ► The average, or the *center of mass* in the region.
- ▶ Given a class c_i , where each object o_j being a member is represented as a feature vector \vec{x}_i , we can compute the class centroid $\vec{\mu}_i$ as

$$\vec{\mu}_i = \frac{1}{|c_i|} \sum_{\vec{x}_i \in c_i} \vec{x}_j$$

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Different ways of representing classes (cont'd)



Some more notes on centroids, medoids and typicality

- ▶ Both *centroids* and *medoids* represent a group by a single prototype.
- ▶ But while a *medoid* is an actual member of the group, a *centroid* is an *abstract* prototype; an average.
- ► *Typicality* can be defined by a member's distance to the prototype.
- ► The centroid could also be distance weighted: Let each member's contribution to the average be determined by its average pairwise similarity to the other members of the group.
- ► There are parallel discussions on how to represent classes and determine typicality within linguistic and psychological prototype theory.

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Representing class membership



Hard classes

- ► Membership considered a Boolean property: a given object is either part of the class or it is not.
- ► A *crisp* membership function.
- ► A variant: disjunctive classes. Objects can be members of more than one class, but the memberships are still crisp.

Soft classes

- ► Class membership is a graded property.
- ► Distance weighted.
- ▶ Probabilistic: The degree of membership for a given object restricted to [0,1], and the sum across classes must be 1.
- ▶ Fuzzy: The membership function is still restricted to [0,1], but without the probabilistic constraint on the sum.

Rocchio classification



- ► AKA nearest centroid classifier or nearest prototype classifier.
- Uses centroids to represent classes.
- ▶ Each class c_i is represented by its centroid $\vec{\mu}_i$, computed as the average of the normalized vectors \vec{x}_i of its members;

$$\vec{\mu}_i = \frac{1}{|c_i|} \sum_{\vec{x}_j \in c_i} \vec{x}_j$$

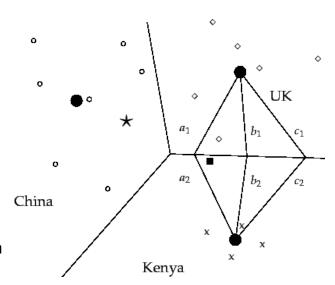
- ▶ To classify a new object o_i (represented by a feature vector $\vec{x_i}$);
 - determine which centroid $\vec{\mu}_i$ that $\vec{x_j}$ is closest to,
 - and assign it to the corresponding class c_i .
- ► The centroids define the boundaries of the class regions.

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The decision boundary of the Rocchio classifier



- ► Defines the boundary between two classes by the set of points equidistant from the centroids.
- ► In two dimensions, this set of points corresponds to a *line*.
- ► In multiple dimensions: A line in 2D corresponds to a *hyperplane* in a higher-dimensional space.



Problems with the Rocchio classifier



- ► The classification decision ignores the distribution of members locally within a class, only based on the centroid distance.
- ▶ Implicitly assumes that classes are spheres with similar radiuses.
- ▶ Does not work well for classes than cannot be accurately represented by a single prototype or center (e.g. disconnected or elongated regions).
- ▶ Because the Rocchio classifier defines a linear decision boundary, it is only suitable for problems involving *linearly separable* classes.

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Ideal



Problematic: Elongated regions



a
a
a
x
b
b
b
b
b
b
b

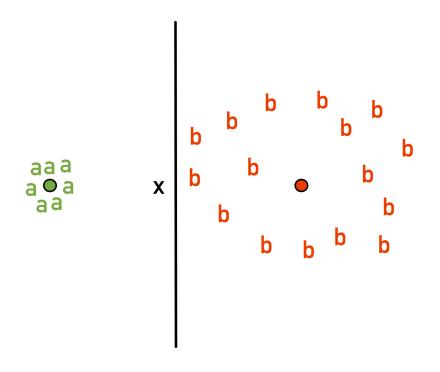
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Problematic: Non-contiguous regions



Problematic: Different sizes





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Problematic: Nonlinear boundary





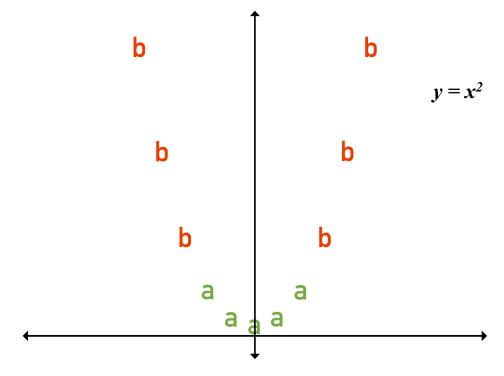


► Before we turn to talk about non-linear classifiers, note that: Classes that are not linearly seperable in a given feature space...

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A side-note on nonlinearity





▶ ... may become linearly separable when the features are mapped to a higher-dimensional space (this is the basis for so-called kernel methods).



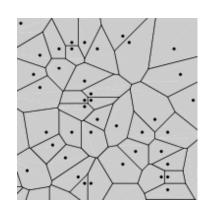
- ▶ *k* Nearest Neighbor classification.
- ► An example of a non-linear classifier.
- ▶ For k = 1: Assign each object to the class of its closest neighbor.
- ▶ For k > 1: Assign each object to the majority class among its k closest neighbors.
- ▶ Rationale: given the contiguity hypothesis, we expect a test object o_i to have the same label as the training objects in the local region of $\vec{x_i}$.
- ightharpoonup The parameter k must be specified in advance.
- \blacktriangleright Unlike Rocchio, the kNN decision boundary is determined locally.
 - ► The decision boundary defined by the Voronoi tessellation.

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Voronoi tessellation

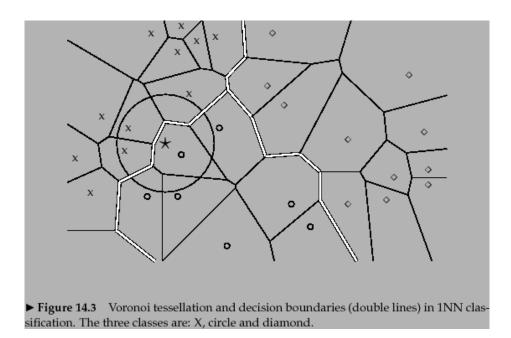


- Assuming k=1: For a given set of objects in the space, let each object define a cell consisting of all points that are closer to that object than to other objects.
- ► Results in a set of convex polygons; so-called Voronoi cells.
- ► Decomposing a space into such cells gives us the so-called Voronoi tessellation.



▶ In the general case of $k \ge 1$, the Voronoi cells are given by the regions in the space for which the set of k nearest neighbors is the same.





Decision boundary for 1NN: defined along the regions of Voronoi cells for the objects in each class. Shows the non-linearity of kNN.

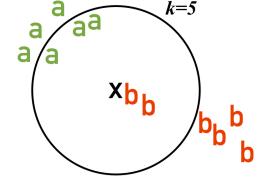
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"Softened" kNN-classification



A probabilistic version

► The probability of membership in a class c given by the proportion of the k nearest neighbors in c.



Distance weighted votes

▶ The score for a given class c_i can be computed as

$$score(c_i, o_j) = \sum_{\vec{x_n} \in knn(\vec{x_j})} I(c_i, \vec{x}_n) sim(\vec{x_n}, \vec{x_j})$$

where $\operatorname{knn}(\vec{x}_j)$ is the set of k nearest neighbors of \vec{x}_j , sim is the similarity measure, and $\mathbf{I}(c_i, \vec{x}_n)$ is 1 if $\vec{x}_n \in c_i$ and 0 otherwise.

► Can give more accurate results, and also help resolve ties.

Some peculiarities of kNN



- ▶ Not really any *learning* or estimation going on at all;
- simply memorizes all training examples.
- ► Generaly with in ML; the more training data the better.
- \blacktriangleright But for kNN, large training sets come with an efficiency penalty.
- ► Test time is linear in the size of the training set,
- but independent of the number of classes.
- ► A potential advantage for problems with many classes.
- ► Notice the similarity to the problem of ad hoc retrieval (e.g., returning relevant documents for a given query);
 - ► Both are instances of finding nearest neighbors.

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Obligatory assignment 2b



- ▶ Builds on oblig 2a: Vector space representation of a set of words based on BoW features extracted from a sample of the Brown corpus.
- ► For 2b we'll provide class labels for most of the words.
- ► Train a Rocchio classifier to predict labels for a set of unlabeled words.

Label	Examples
FOOD	potato, food, bread, fish, eggs
INSTITUTION	embassy, institute, college, government, school
TITLE	president, professor, dr, governor, doctor
PLACE_NAME	italy, dallas, france, america, england
PERSON_NAME	lizzie, david, bill, howard, john
UNKNOWN	department, egypt, robert, butter, senator

Testing a classifier

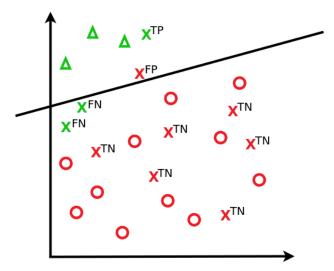


- ► Vector space classification amounts to computing the boundaries in the space that separate the class regions: *the decision boundaries*.
- ► To evaluate the boundary, we measure the number of correct classification predictions on unseeen test items.
 - ► Many ways to do this...
- ▶ We want to test how well a model *generalizes* on a held-out test set.
- ► (Or, if we have little data, by *n*-fold cross-validation.)
- ► Labeled test data is sometimes referred to as the gold standard.
- ► Why can't we test on the training data?

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Example: Evaluating classifier decisions



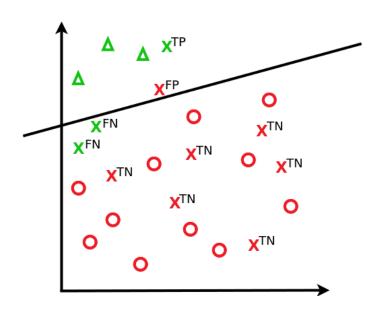


▶ Predictions for a given class can be wrong or correct in two ways:

	gold = positive	gold = negative
prediction = positive	true positive (TP)	false positive (FP)
prediction = negative	false negative (FN)	true negative (TN)

Example: Evaluating classifier decisions





$$\begin{array}{l} accuracy = \frac{TP + TN}{N} \\ = \frac{1+6}{10} = 0.7 \end{array}$$

$$\begin{array}{l} \textit{precision} = \frac{\textit{TP}}{\textit{TP+FP}} \\ = \frac{1}{1+1} = 0.5 \end{array}$$

$$\begin{aligned} & \underline{recall} = \frac{TP}{TP + FN} \\ &= \frac{1}{1+2} = 0.33 \end{aligned}$$

$$\begin{array}{l} {\color{red} F\text{-}score} = \\ {\color{red} \frac{2\times precision \times recall}{precision + recall}} = 0.4 \end{array}$$

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Evaluation measures



- - ► The ratio of correct predictions.
 - ► Not suitable for unbalanced numbers of positive / negative examples.
- $ightharpoonup precision = \frac{TP}{TP+FP}$
 - ► The number of detected class members that were correct.
- $ightharpoonup recall = \frac{TP}{TP + FN}$
 - ► The number of actual class members that were detected.
 - ► Trade-off: Positive predictions for all examples would give 100% recall but (typically) terrible precision.
- $ightharpoonup F\text{-}score = rac{2 imes precision imes recall}{precision + recall}$
 - ► Balanced measure of precision and recall (harmonic mean).

Evaluating multi-class predictions



Macro-averaging

- ► Sum precision and recall for each class, and then compute global averages of these.
- ► The **macro** average will be highly influenced by the small classes.

Micro-averaging

- ► Sum TPs, FPs, and FNs for all points/objects across all classes, and then compute global precision and recall.
- ► The micro average will be highly influenced by the large classes.

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Next lecture



- ► Unsupervised machine learning for class discovery: Clustering
- ► Flat vs. hierarchical clustering.
- ► C-Means Clustering.
- ► Reading: Chapters 16 and 17 in Manning, Raghavan & Schütze (2008) (see course page for the relevant sections).