

## SECTION 37

1. a. The conjugate classes are  $\{\rho_0\}$ ,  $\{\rho_2\}$ ,  $\{\rho_1, \rho_3\}$ ,  $\{\mu_1, \mu_2\}$ ,  $\{\delta_1, \delta_2\}$ .  
 b.  $8 = 2 + 2 + 2 + 2$   
 3. a.  $T$       c.  $F$       e.  $T$       g.  $T$       i.  $F$   
 e. This is somewhat a matter of opinion.  
 9.  $24 = 1 + 6 + 3 + 8 + 6$

## SECTION 38

1.  $\{(1, 1, 1), (1, 2, 1), (1, 1, 2)\}$   
 3. No.  $n(2, 1) + m(4, 1)$  can never yield an odd number for first coordinate.  
 7.  $2\mathbb{Z} < \mathbb{Z}$ , rank  $r = 1$

## SECTION 39

1. a.  $a^2b^2a^3c^3b^{-2}, b^2c^{-3}a^{-3}b^{-2}a^{-2}$       b.  $a^{-1}b^3a^4c^6a^{-1}, ac^{-6}a^{-4}b^{-3}a$   
 3. a. 16      b. 36      c. 36  
 5. a. 16      b. 36      c. 18  
 11. a. Partial answer:  $\{1\}$  is a basis for  $\mathbb{Z}_4$ .      c. Yes  
 13. c. A blob group on  $S$  is isomorphic to the free group  $F[S]$  on  $S$ .

## SECTION 40

1.  $(a : a^4 = 1); (a, b : a^4 = 1, b = a^2); (a, b, c : a = 1, b^4 = 1, c = 1)$ . (Other answers are possible.)  
 3. Octic group:

	1	$a$	$a^2$	$a^3$	$b$	$ab$	$a^2b$	$a^3b$
1	1	$a$	$a^2$	$a^3$	$b$	$ab$	$a^2b$	$a^3b$
$a$	$a$	$a^2$	$a^3$	1	$ab$	$a^2b$	$a^3b$	$b$
$a^2$	$a^2$	$a^3$	1	$a$	$a^2b$	$a^3b$	$b$	$ab$
$a^3$	$a^3$	1	$a$	$a^2$	$a^3b$	$b$	$ab$	$a^2b$
$b$	$b$	$a^3b$	$a^2b$	$ab$	1	$a^3$	$a^2$	$a$
$ab$	$ab$	$b$	$a^3b$	$a^2b$	$a$	1	$a^3$	$a^2$
$a^2b$	$a^2b$	$ab$	$b$	$a^3b$	$a^2$	$a$	1	$a^3$
$a^3b$	$a^3b$	$a^2b$	$ab$	$b$	$a^3$	$a^2$	$a$	1

Quaternion group: The same as the table for the octic group except that the 16 entries in the lower right corner are