

Last time

1. We defined convergence in measure: $\{f_n\}$ converges in measure to f if for all $\varepsilon > 0$

$$\lim_n \mu(\{x \in \Omega \mid |f_n(x) - f(x)| > \varepsilon\}) = 0$$

2. We compared the notions pointwise convergence almost everywhere and convergence in measure.
3. Looked more examples of how to compute with the Lebesgue integral.
4. Useful techniques:
 - 4.1 If f is positive or integrable then

$$\int_{\mathbb{R}} f \, d\lambda = \lim_n \int_{[-n,n]} f \, d\lambda.$$

- 4.2 If f is continuous then

$$\int_{[a,b]} f \, d\lambda = \int_a^b f(x) \, dx.$$

Last time

1. We defined convergence in measure: $\{f_n\}$ converges in measure to f if for all $\varepsilon > 0$

$$\lim_n \mu(\{x \in \Omega \mid |f_n(x) - f(x)| > \varepsilon\}) = 0$$

2. We compared the notions pointwise convergence almost everywhere and convergence in measure.
3. Looked more examples of how to compute with the Lebesgue integral.
4. Useful techniques:
 - 4.1 If f is positive or integrable then

$$\int_{\mathbb{R}} f \, d\lambda = \lim_n \int_{[-n,n]} f \, d\lambda.$$

- 4.2 If f is continuous then

$$\int_{[a,b]} f \, d\lambda = \int_a^b f(x) \, dx.$$

Last time

1. We defined convergence in measure: $\{f_n\}$ converges in measure to f if for all $\varepsilon > 0$

$$\lim_n \mu(\{x \in \Omega \mid |f_n(x) - f(x)| > \varepsilon\}) = 0$$

2. We compared the notions pointwise convergence almost everywhere and convergence in measure.
3. Looked more examples of how to compute with the Lebesgue integral.
4. Useful techniques:

4.1 If f is positive or integrable then

$$\int_{\mathbb{R}} f \, d\lambda = \lim_n \int_{[-n,n]} f \, d\lambda.$$

4.2 If f is continuous then

$$\int_{[a,b]} f \, d\lambda = \int_a^b f(x) \, dx.$$

Last time

1. We defined convergence in measure: $\{f_n\}$ converges in measure to f if for all $\varepsilon > 0$

$$\lim_n \mu(\{x \in \Omega \mid |f_n(x) - f(x)| > \varepsilon\}) = 0$$

2. We compared the notions pointwise convergence almost everywhere and convergence in measure.
3. Looked more examples of how to compute with the Lebesgue integral.
4. Useful techniques:
 - 4.1 If f is positive or integrable then

$$\int_{\mathbb{R}} f \, d\lambda = \lim_n \int_{[-n,n]} f \, d\lambda.$$

- 4.2 If f is continuous then

$$\int_{[a,b]} f \, d\lambda = \int_a^b f(x) \, dx.$$

Today

1. We will shift our focus to normed spaces and Banach spaces.
2. We will define:
 - 2.1 normed spaces,
 - 2.2 linear operators,
 - 2.3 the norm of a linear operator, and
 - 2.4 Banach spaces.
3. We will prove some basic properties about these and give examples.

Today

1. We will shift our focus to normed spaces and Banach spaces.
2. We will define:
 - 2.1 normed spaces,
 - 2.2 linear operators,
 - 2.3 the norm of a linear operator, and
 - 2.4 Banach spaces.
3. We will prove some basic properties about these and give examples.

Today

1. We will shift our focus to normed spaces and Banach spaces.
2. We will define:
 - 2.1 normed spaces,
 - 2.2 linear operators,
 - 2.3 the norm of a linear operator, and
 - 2.4 Banach spaces.
3. We will prove some basic properties about these and give examples.