Books


**Papers**


P. Hoffman and G. Porter, Cohomology realizations of $\mathbb{Q}[x], \mathbb{O}_x$. *Q.* 24 (1973), 251–255.


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