

```

μ = {0.06, 0.08, 0.11};
e = {1, 1, 1};
V = {{0.0025, -0.002, 0.003}, {-0.002, 0.01, 0.01}, {0.003, 0.01, 0.04}};

```

```
MatrixForm[V]
```

$$\begin{pmatrix} 0.0025 & -0.002 & 0.003 \\ -0.002 & 0.01 & 0.01 \\ 0.003 & 0.01 & 0.04 \end{pmatrix}$$

```
MatrixForm[vInvers = Inverse[V]]
```

$$\begin{pmatrix} 789.474 & 289.474 & -131.579 \\ 289.474 & 239.474 & -81.5789 \\ -131.579 & -81.5789 & 55.2632 \end{pmatrix}$$

```
(* Vektor for den absolutt variansminimerende portefølje *)
```

$$xMin = \frac{vInvers.e}{e.vInvers.e}$$

```
{0.765957, 0.361702, -0.12766}
```

```
(* Vektor for "korrektions-portefølje" for tilpasning til spesifisert krav om forventet avkastning *)
```

$$zStar = vInvers. \left(\mu - \frac{e.vInvers.\mu}{e.vInvers.e} e \right)$$

```
eRxMin = xMin.μ
```

```
0.0608511
```

```
eRzStar = zStar.μ
```

```
0.0698936
```

$$varxMin = \frac{1}{e.vInvers.e}$$

```
testvarxMin = xMin.V.xMin
```

```
0.000808511
```

```
0.000808511
```

```
(* Her er selve uttrykket for vektene i den effisiente porteføljen *)
```

$$effWeights[r_] := xMin + \frac{(r - eRxMin) zStar}{eRzStar};$$

```
(* Tester at forventet avkastning i den effisiente porteføljen er lik kravet om forventet avkastning *)
```

$$testExStar = Simplify \left[\left(xMin + \frac{(r - eRxMin) zStar}{eRzStar} \right) . \mu \right]$$

```
0. + 1. r
```

```
varzStar = zStar.V.zStar
```

```
0.0698936
```

$$varxStar[r_] = varxMin + \left(\frac{r - eRxMin}{eRzStar} \right)^2 varzStar$$

```
0.000808511 + 14.3075 (-0.0608511 + r)^2
```

```
(* Tester uttrykk for variansen til xStar *)
```

$$Expand \left[varxMin + \left(\frac{r - eRxMin}{eRzStar} \right)^2 varzStar \right]$$

```
0.0537869 - 1.74125 r + 14.3075 r^2
```

(Sammenligner med variansen til den effisiente porteføljen regnet ut rett frem)

```
Expand[ (xMin + (r - eRxMin) zStar / eRzStar) .V. (xMin + (r - eRxMin) zStar / eRzStar) ]
```

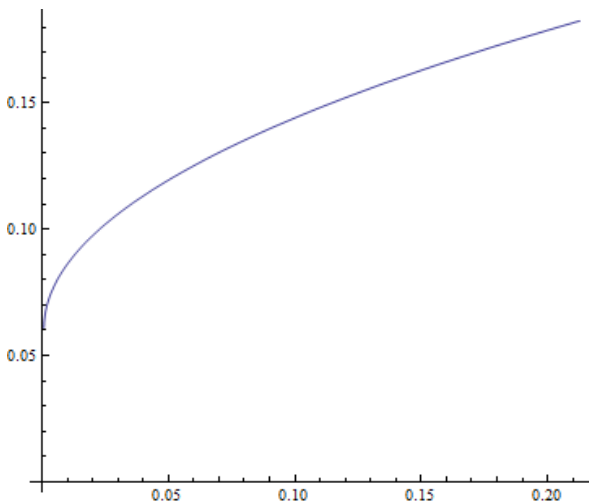
```
0.0537869 - 1.74125 r + 14.3075 r^2
```

(Vester xMin og zStar ulorrolerte)

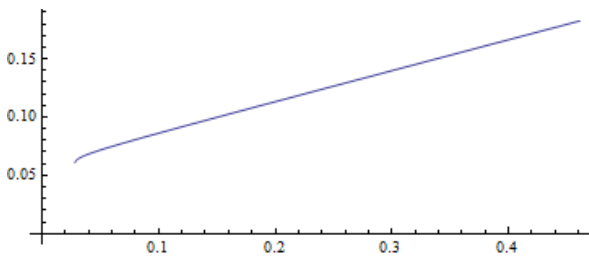
```
xMin.V.zStar
```

```
1.04626 × 10-17
```

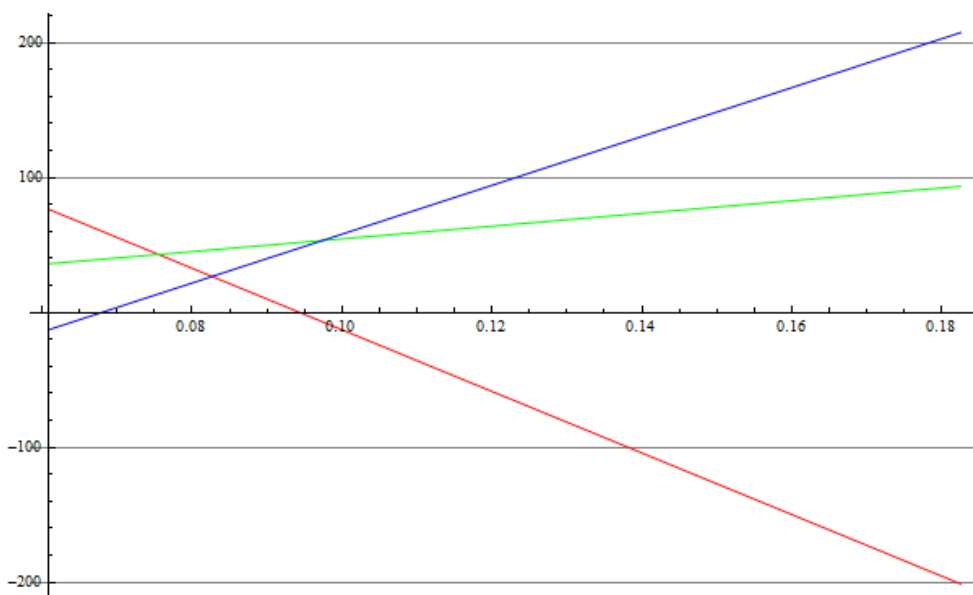
```
ParametricPlot[{varxStar[r], r}, {r, eRxMin, 3 eRxMin}, PlotRange → All, AxesOrigin → {0, 0}]
```



```
ParametricPlot[{sqrt[varxStar[r]], r}, {r, eRxMin, 3 eRxMin}, PlotRange → All, AxesOrigin → {0, 0}]
```



```
effPlots = Table[Plot[100 effWeights[r][[n]], {r, eRxMin, 3 eRxMin}, PlotRange → All, AxesOrigin → {eRxMin, 0},
  DisplayFunction → Identity, PlotStyle → {RGBColor[If[n == 1, 1, 0], If[n == 2, 1, 0], If[n == 3, 1, 0]]}, {n, 1, 3}];
Show[effPlots[[1]], effPlots[[2]], effPlots[[3]], DisplayFunction → $DisplayFunction, GridLines → {None, Automatic},
  ImageSize → 600]
```




Av spesiell interesse er "mulighetsområdet" der alle vektene er positive. Over skjer dette der kravet til forventet avkastning stort sett ligger i området 6,79% til 9,44%.

```
effWeights[.0679]
```

```
effWeights[.0944]
```

```
{0.605023, 0.394962, 0.0000152207}
```

```
{1.4988 × 10-14, 0.52, 0.48}
```

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