

Postponed exam 3220/4220, Fall 2022

Problem 1 (Microeconomic Theory)

Part A

Weight 25%

Consider an economy consisting of one firm and one consumer. The firm produces two different products with a single resource. The consumer values both products. The amount of the resource is given.

Discuss assumptions, including on firm production technology and consumer preferences, that are warranted for the existence of a general equilibrium in which both products are traded.

Part B

Weight 25%

Derive the conditions characterising the general equilibrium, including the condition

$$MRS_{12} = \frac{p_1}{p_2} = MRT_{12},$$

where MRS_{12} and MRT_{12} are the marginal rate of substitution and the marginal rate of transformation, respectively, between products 1 and 2, and p_1 and p_2 are the prices of the two products. Interpret the results in economic terms.

The postponed exam in ECON3220/4220, Fall 2022

Problem 2 (Game theory and the economics of information)

This problem relates to experiments made during the lectures of ECON3220/4220. Solving the different parts of the problem does not require that the student has participated in the experiments.

Part A: Bargaining

Weight: 14% (with equal weight = 7% on each subproblem)

- (i) *Ultimatum bargaining.* Consider an ultimatum game where player 1 can demand 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, or 10. If player 2 accepts, then player 1 receives his demand, while player 2 receives 10 minus the demand of player 1. If player 2 rejects, then both players receive 0. Show that it is a subgame-perfect Nash equilibrium outcome that player 1 demands 9 and that player 2 accepts! Are there any other subgame-perfect Nash equilibrium outcomes?
- (ii) *Two-period alternating offer bargaining.* Consider a two-period alternating offer bargaining game where player 1 in the first period can demand 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, or 10. If player 2 accepts player 1's demand, then player 1 receives his demand, while player 2 receives 10 minus the demand of player 1. If player 2 rejects, player 2 in the second period can demand 0, 1, 2, 3, 4, 5, 6, 7, 8, or 9. If player 1 accepts player 2's demand, then player 2 receives his demand, while player 1 receives 9 minus the demand of player 2. If player 1 rejects, then both players receive 0. Show that it is a subgame-perfect Nash equilibrium outcome that player 1 demands 2 and that player 2 accepts! Are there any other subgame-perfect Nash equilibrium outcomes?

Part B: First and second-price sealed-bid auction

Weight: 18% (with equal weight = 6% on each subproblem)

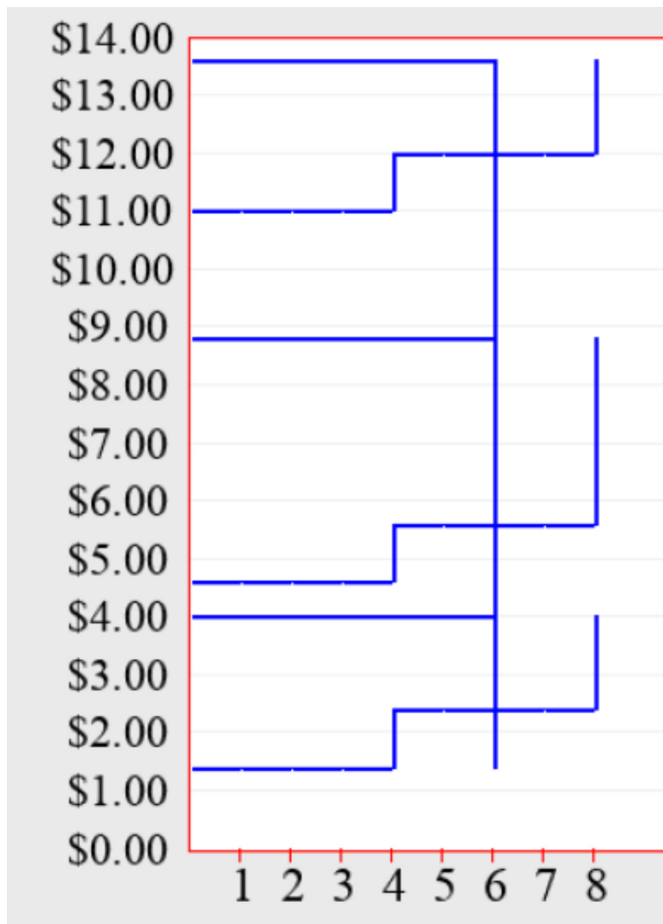
Consider a private value sealed-bid auction with two bidders who both are risk-neutral, have valuations that are independent and uniformly distributed on the interval $[0, 10]$ and can submit bids in the interval $[0, 10]$. The bidders are first informed of their valuations, they then submit their bids, and the item is assigned to the bidder with the highest bid (and with equal probability to each if the two bids are equal). In a first-price auction the winner pays the highest bid (i.e., their own bid), while a second-price auction the winner pays the second-highest bid (i.e., the bid of the other bidder). The utility of the winner equals their valuation minus the payment, while the other bidder has zero utility.

- (i) Argue that it is a Bayesian Nash equilibrium to bid half of the true value in the first-price auction.
- (ii) Argue that it is a Bayesian Nash equilibrium to bid the true value in the second-price auction.
- (ii) Argue that the seller's expected revenue is the same for both types of auctions.

Part C: Market for lemons

Weight: 18% (with equal weight = 6% on each subproblem)

Consider a market with 4 sellers and 6 buyers. The product can be of low, medium or high quality. Each buyer is only willing to pay a positive amount for one single unit of the product: 4.6 if of low quality, 8.8 if of medium quality, and 13.6 if of high quality. Each seller can produce at most two unit of a single quantity, with costs 1.4 for the first unit and 2.4 for the second unit if of low quality, with costs 4.6 for the first unit and 5.6 for the second unit if of medium quality, and with costs 11.0 for the first unit and 12.0 for the second unit if of high quality, This leads to the following demand and supply curves.



Seller first choose quality, then quantity, and finally price for each unit produced. Thereafter buyers decide whether to purchase available units.

- (i) Assume first that the quality choices of sellers are observable for the buyers. Why is the equilibrium outcome that sellers choose medium quality, with two of them producing 2 units and two of them producing 1 units, with all 6 produced units selling at price 5.6?
- (ii) Assume then that the quality choices of sellers are unobservable for the buyers. Why is the equilibrium outcome now that sellers choose low quality, with two of them producing 2 units and two of them producing 1 units, with all 6 produced units selling at price 2.4?
- (iii) When comparing the equilibrium outcomes, what is the efficiency cost of not having complete information?