

Exercise 3: Alternative presentation of the Lorenz curve

- (i) Explain how the information content of the Lorenz curve can be given an alternative presentation and interpretation which is consistent with the notion of inequality captured by the Lorenz curve.
- (ii) The alternative representation of the Lorenz curve, called the scaled conditional mean curve (the M-curve), shows to possess several attractive properties. Explain these properties.

Exercise 4: Choosing measures of inequality for empirical applications

- (i) Provide a justification for why the moments of the M-curve can be considered to form a family of inequality measures that uniquely determines the M-curve and the Lorenz curve.
- (ii) The standard approach in empirical work is to employ the Gini coefficient in combination with measures from the Atkinson family and/or the Theil family. Explain why it is hard to justify such an approach.
- (iii) Provide arguments for why it might be attractive to employ the three first moments of the M-curve to summarize inequality exhibited by an income distribution.
- (iv) Let C_1 , C_2 and C_3 denote the three first moments of the M-curve. Show that these three measures can be given the following expressions in terms of the distribution function F :

$$C_1 = \frac{1}{\mu_0} \int_0^{\infty} F(x) \log F(x) dx, \quad C_2 = G = \frac{1}{\mu_0} \int_0^{\infty} F(x)(1 - F(x)) dx, \quad C_3 = \frac{1}{2\mu_0} \int_0^{\infty} F(x)(1 - F^2(x)) dx.$$

- (v) Show that C_1 , C_2 and C_3 can be given explicit expressions in terms of social welfare and that the associated social welfare functions can be decomposed with regard to the mean and (in)equality.