

# Environmental Economics – Lecture 2

## Emission control: Targets

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Perman et al (2011) ch 5



# Review last lecture

1. Overview and Organisation
2. Environment  $\leftrightarrow$  Economy
3. Efficient and optimal allocation of goods
4. Public goods and the Free-rider problem
5. Externalities and the Coase theorem



## Key concepts last lecture

- ▶ Markets allocate goods efficiently under ideal conditions but need not be optimal from a social point of view
- ▶ Efficiency for private goods:  $MRUS^A = MRUS^B = MRT$
- ▶ Public goods are goods that are both non-excludable and non-rivalrous
- ▶ Efficiency for public goods:  $MRUS^A + MRUS^B = MRT$
- ▶ Public good implies presence of externality
- ▶ Externality does **not** imply existence of public good
- ▶ Uncorrected externalities lead to inefficiencies



# Preview this lecture

1. The efficient level of emissions
2. Benefits and damages from emissions
3. Different types of pollution problems



# The efficient level of emissions

Trade-off between benefit and damages from emission.

Standard solution:  $M^*$  defined by  $B'(M) = D'(M)$



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- ▶ Marginal benefits from emission are decreasing (linked to marginal utility of consumption)
- ▶ Marginal damage from emission is increasing (gradually reduced ecosystem services or increased valuation of unspoiled nature)



# Benefits from emissions

- ▶ Consumers have preferences for a private good  $y$  and a public good  $E$  (environmental quality).
- ▶ Firms competitively produce the private good  $y$ . Production causes emissions  $M$  that reduce  $E$ .
- ▶ Firms can exercise (costly) effort to reduce emissions:
  - ▶ End-of-the-pipe cleaning
  - ▶ Changed technology, cleaner inputs, increased diligence
  - ▶ Reduced production



# Benefits from emissions



Figure: The solution to pollution is dilution?



# Benefits from emissions

[Notation: Aggregate emissions  $M$  are sum of emissions  $m_j$  from all firms  $j = 1, 2, \dots$ ]

- ▶ For each firm  $j$ , suppose that inputs can be separated into those that are used for producing  $y$  and those that are used for reducing  $m$ .
- ▶ Production and emissions linked by a function  $y_j = f(m_j)$ .
- ▶ As if emissions are an input to production:
  - ▶ For a given  $y$ ,  $m$  can only be reduced at the cost of increasing other inputs
  - ▶ If all other inputs are fixed,  $y$  can only be increased by increasing  $m$ .
- ▶ Let  $\hat{m}_j$  be  $j$ 's emissions when no effort to reduce emissions. Furthermore:  $f(m_j) \geq 0$ ,  $f'(m_j) \geq 0$ ,  $f''(m) \leq 0$  and  $f(0) = 0$ ,  $f'(\hat{m}) = 0$ .



# Benefits from emissions and costs of abatement

Firm's benefits from emission are the avoided costs of abatement.

- ▶ Abatement is the emission reduction compared to the baseline scenario:  $a_j = \hat{m}_j - m_j$
- ▶ Abatement cost loss due to reduced output (keeping the other inputs fixed):  $c_j(a_j) = f(\hat{m}_j) - f(m_j)$
- ▶ Marg. abatement cost equals marg. productivity of emissions:

$$\frac{\partial c_j(a_j)}{\partial a_j} = \frac{\partial [f(\hat{m}_j) - f(m_j)]}{\partial m_j} \frac{\partial m_j}{\partial a_j} = -f'(m_j)(-1) = f'(m_j)$$

- ▶  $c$  is increasing and convex, defined on  $[0, \hat{m}_j]$  with  $c(0) = 0$  and  $c(\hat{m}_j) = f(\hat{m}_j)$ .



# Benefits from emissions

The firm's objective is to maximize profits:

$$\pi(m_j) = f(m_j) - b_j - \tau m_j$$

where:

- ▶ the price of the (numeraire) good is normalized to 1
- ▶  $b$  are the (fixed) costs of the other inputs to production
- ▶  $\tau$  is the price per unit of emission that the firm has to pay

Without regulation,  $\tau = 0$  and  $m_j^* = \arg \max \pi = \hat{m}_j$



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- ▶ How much would consumer pay for marg improvement of  $E$ ?
  - ▶ Differentiate  $U_i = u(y_i, E)$  keeping  $U_i$  fixed:

$$dU_i = \frac{\partial u}{\partial y_i} dy_i + \frac{\partial u}{\partial E} dE = 0 \quad \Leftrightarrow \quad -dy_i = \frac{u'_E}{u'_{y_i}} dE$$



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- ▶ However, interested in emissions  $M$ : substitute  $dE = -z'(M)dM$
- ▶ Let  $dM = 1$  so that our measure for  $MWTP_i$  is  $z'(M) \frac{u'_E}{u'_{y_i}}$



# Damages from emissions

From individual  $MWTP$  to aggregate  $D(M)$ :

- ▶ Is measurement possible?  
(discussed in Lecture 5)
- ▶ Is aggregation possible?  
( $MWTP_i > MWTP_j$  could be caused by differences in the valuation of  $y$ )
- ▶ Here focus on efficiency and suppose zero income / distribution effects.
- ▶  $D'(M) = z'(M) \sum_i \frac{u'_E}{u'_y_i}$





We know that efficiency requires  $B'(M) = D'(M)$ :

- ▶  $B'(M) = \frac{\partial \sum_j f(m_j)}{\partial m_j} = f'(m_j)$

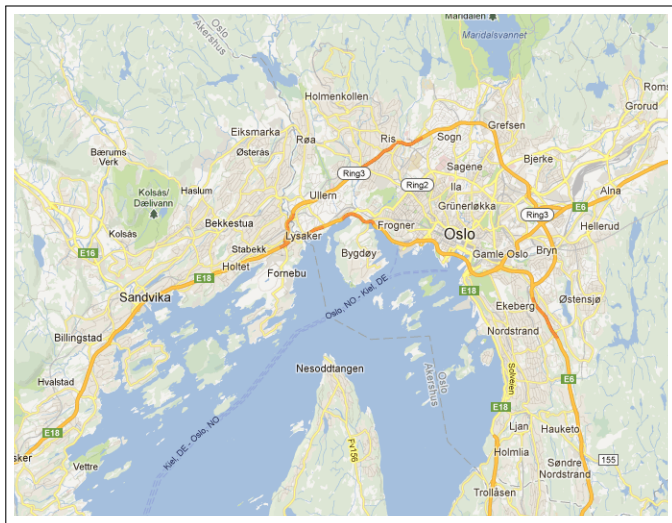
- ▶  $D'(M) = z'(M) \sum_i \frac{u'_E}{u'_{y_i}}$

The market solution is  $f'(m_j) = \tau$

- ▶ Task of regulation:  $\tau = z'(M) \sum_i \frac{u'_E}{u'_{y_i}}$



# Discussion: Where to put a waste treatment plant?



## Different types of pollution problems

- ▶ In the model so far, environmental quality was impacted directly by emissions and there was no time dimension: The "static flow pollution" model
- ▶ Often, emissions accumulate to form a stock of some stock  $A$  of a harmful substance. Damages are then a function of  $A$ .
  - (a) If the stock dissolves quickly, no need to take time into account: "short-lived stock pollutant"
  - (b) If the stock dissolves slowly: explicit dynamic modeling necessary: "long-lived stock pollutant" (Lecture 9)
- ▶ Even in case (a), the distinction between stock and flow may matter when:
  - ▶ space matters
  - ▶ there are non-convexities in the damage function



## Different types of pollution problems

Short-lived stock pollutants: Are emissions “uniformly mixing”?

- ▶ If yes, model stock as  $A = kM$
- ▶ If not, damages depend on relative position of the  $I$  “sources” and  $J$  “receptors”. Model stock as  $\mathbf{A}_{I \times 1} = \mathbf{T}_{I \times J} \mathbf{M}_{J \times 1}$
- ▶ Objective is now:  $\max NB = \sum_i B_i(m_i) - \sum_j D_j(A_j)$



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- ▶ Substitute:  $\max NB = \sum_i B_i(m_i) - \sum_j D_j(\sum_i t_{ji} m_i)$



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- ▶ Substitute:  $\max NB = \sum_i B_i(m_i) - \sum_j D_j(\sum_i t_{ji} m_i)$
- ▶ Efficiency condition is:  $B'_i(m_i) = \sum_j D'_j(A_j) t_{ji}$



## Key concepts this lecture

- ▶ The emission target should be set such that the aggregate marginal benefit from emission equals the aggregate marginal damage from emission.
- ▶ Equivalently, the marginal abatement costs should equal the total willingness to pay for a marginal improvement of environmental quality
- ▶ Pollution can be classified as flow- or stock pollution. The latter can be short-lived or long-lived, uniformly mixing or non-uniformly mixing.



# Preview next lecture

## **Emission control: Instruments**

Perman et al (2011) ch 6

- ▶ Criteria for choosing emission control instruments
- ▶ Voluntary approaches
- ▶ Command-and-control measures
- ▶ Incentive-based instruments

