## Environmental Economics - 4910

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- Overusing/exploiting renewable and exhaustible resources
- Land use changes (e.g. tropical deforestation)
- Waste (e.g. hazardous, or plastic)
- Water (over-usage, or contamination)
- Air (particles, NO<sub>x</sub>, acid rain; ozone layer)
- Greenhouse gases (e.g., CO<sub>2</sub>)

- National vs. international
- Political vs. marked-based
- Number of sources and number of affected parties
- Tangible vs. nonverifiable pollutants
- Affecting producers vs consumers
- Flow pollutants vs. accumulated stocks
- Contemporary vs. long-term effects

## Outline

- Welfare theorems and market failures (micro)
- Policy instruments (Pigou, Coase, Weitzman) (public ec.)
- Trade and the environment (int. trade)
- Self-enforcing vs. binding agreements (game theory)
- S Architectures for agreements (economic systems)
- Free-riding and participation (contract theory)
- Supply-side environmental policy (resource ec.)
- Oeforestation and REDD contracts (development ec.)
- Interpretation of the Future: Discounting (behavioral ec.)
- Integrated Assessment Models (Traeger) (macro)

## Consumption and Production: "ECON 101"

• Consumers *i*'s utility and good *j*'s production function:

$$u^i\left(x_1^i,...,x_J^i
ight)$$
 and  $\sum\limits_i x_j^i \leq f^j\left(y_j^1,...,y_j^K
ight)$  ,

- ...where i ∈ {1, ..., I} consumes x<sub>j</sub><sup>i</sup> of good j ∈ {1, ..., J}, and y<sub>j</sub><sup>k</sup> is the quantity of input k ∈ {1, ..., K} used in the production of good j.
- Pareto optimality (PO) requires that

$$\max_{\{x_j^i\}, \{y_j^k\}} u^1 \left(x_1^1, ..., x_J^1\right) \text{ s.t.}$$

$$u^i \left(x_1^i, ..., x_J^i\right) \geq \overline{u}^i, \forall i \qquad (\text{shadow value: } \lambda_i),$$

$$\sum_i x_j^i \leq f^j \left(y_j^1, ..., y_j^K\right) \quad \forall j \quad (\text{shadow value: } \mu_j),$$

$$\sum_j y_j^k \leq \overline{y}^k \quad \forall k \qquad (\text{shadow value: } \eta_k).$$

for some default levels (ū<sup>i</sup>'s) and input quantities (y<sup>k</sup>'s).
Do we need to include labor/leisure in the model?

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Lecture Notes 1

## Consumption and Production: Pareto Optimality

• Lagrange (/Kuhn-Tucker) problem with foc for  $x_i^i$  and  $y_i^k$  (if  $\lambda_1 \equiv 1$ ):

$$\begin{aligned} \lambda_i u_j^i &= \mu_j, \\ \mu_j f_k^j &= \eta_k. \end{aligned}$$

- The shadow values depend on the default levels; the  $\overline{u}_i$ 's.
- For PO, it is sufficient that the foc's hold for *some* shadow values.
- When the foc's are combined:

$$\begin{array}{ll} \frac{u_{j}^{i}}{u_{j'}^{i}} & = & \frac{\mu_{j}}{\mu_{j'}} = \frac{u_{k}^{i'}}{u_{l}^{j'}} \,\,\forall \left(i,i'\right), \left(j,j'\right) \quad (\text{efficiency in consumption}), \\ \frac{f_{k}^{j}}{f_{k'}^{j}} & = & \frac{\eta_{k}}{\eta_{k'}} = \frac{f_{k}^{j'}}{f_{k'}^{j'}} \,\,\forall \left(k,k'\right), \left(j,j'\right) \quad (\text{efficiency in production}), \\ \frac{u_{j}^{i}}{u_{j'}^{i}} & = & \frac{f_{k}^{j'}}{f_{k}^{j}} \,\,\forall \left(j,j'\right), i,k \qquad (\text{efficiency in exchange}). \end{array}$$

### Consumption and Production: Market Equilibrium

- Consumers' choice, given endowment  $E^i$  (with shadow-value  $\nu_i$ ):  $\max_{\{x_j^i\}_j} u^i \left(x_1^i, ..., x_j^i\right) \text{ s.t. } \sum_j p_j x_j^i \leq E^i \quad (\nu_i) \Rightarrow u_j^i = \nu_i p_j.$
- Producers:

$$\max p_j f^j \left( y_j^1, ..., y_j^K \right) - \sum_k w^k y_j^k \Rightarrow p_j f_k^j = w^k.$$

Combined:

$$\begin{array}{ll} \frac{u_{j}^{i}}{u_{j'}^{i}} & = & \frac{\mu_{j}}{\mu_{j'}} = \frac{u_{j}^{j'}}{u_{j'}^{j'}} \text{ if just } \mu_{j} = p_{j}, \\ \frac{f_{k}^{j}}{f_{k'}^{j}} & = & \frac{\eta_{k}}{\eta_{k'}} = \frac{f_{k}^{j'}}{f_{k'}^{j'}} \text{ if just } \eta_{k} = w^{k}, \\ \frac{u_{j}^{i}}{u_{j'}^{i}} & = & \frac{f_{k}^{j'}}{f_{k}^{j}} = \frac{p_{j}}{p_{j'}} \ \forall \ (j,j') \ , i, k. \end{array}$$

## Consumption and Production: Welfare Theorems

#### Theorem

- Every market equilibrium  $\Rightarrow$  Pareto optimal.
- ② Every Pareto optimal outcome ⇒ market equilibrium given some allocation of endowments.
  - Where is the environment?

## Consumption and Production: With Externalities

• Externalities from inputs/productions to consumers:

$$u^i\left(x_1^j,...,x_J^i,\sum_j g_j
ight)$$
 and  $\sum_i x_j^i \leq f^j\left(y_j^1,...,y_j^K,g_j
ight)$ .

• Pareto Optimality is given by the same conditions as above, plus:

$$\mu_j f_g^j = \sum_i \lambda_i \left( -u_g^i \right) \Rightarrow u_j^1 f_g^j = \sum_i u_j^1 \frac{-u_g^i}{u_j^i} \Rightarrow f_g^j = \sum_i \frac{-u_g^i}{u_j^i}$$

- Equilibrium with no regulation: j emits until  $f_g^j = 0$ .
- With regulation or tax  $t_g^j$  on j's emission:  $p_j f_g^j = t_g^j$
- This coincides with the PO outcome if

$$f_g^j = rac{t_g^j}{p_j} = \sum_i rac{-u_g^i}{u_j^i} = \sum_i rac{-u_g^i}{p_j u_1^i / p_1} \Rightarrow t_g^j = \sum_i rac{-u_g^i}{u_1^i} p_1.$$

 So, the emission tax should be the same for all firms, no matter how valuable/dirty they are.

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# Consumption and Production: With Externalities (cont.)

- If good 1 is a numeraire good (i.e., if  $u_1^i = 1 = p_1$ ), then  $t_g^j = \sum_i u_g^i$ .
- Alternatively, the regulator may decide on the  $g_j$ 's directly.
- For each such policy, there will be equilibrium prices and quantities such that payoffs are functions  $u_i(\mathbf{g})$  and profits  $\pi_j(\mathbf{g})$ .
- Larger g<sub>j</sub>'s is likely to benefit producer j (B<sub>j</sub> (g<sub>j</sub>)) but be costly for consumers (C<sub>i</sub> (g<sub>j</sub>)).

## Externalities and Public Goods

Let g<sub>i</sub> be emission by agent i ∈ N ≡ {1, ..., n}, and g = {g<sub>1</sub>, ..., g<sub>n</sub>}.
Externalities:

$$u_{i}\left(\mathbf{g}\right)$$
, if  $\partial u_{i}/\partial g_{j}\neq 0$  for some  $j\neq i$ .

• Public good/bad:

$$u_{i}\left(\mathbf{g}
ight)=u_{i}\left(g_{i},\,G
ight)=B_{i}\left(g_{i}
ight)-C_{i}\left(G
ight)$$
 , where  $G=\sum_{j\in\mathcal{N}}g_{j}$  .

- To get a unique solution, assume u<sub>i</sub> is concave in g<sub>i</sub>
  - For example: Every  $B_i$  is concave while  $C_i$  is convex.
- Business as usual (interior) equilibrium:

$$B_{i}^{\prime}\left(g_{i}\right)=C_{i}^{\prime}\left(G
ight).$$

- Suppose transfers enter linearly and additively in *u<sub>i</sub>*.
- The first-best (FB; the unique PO outcome with transfers):

$$B_i'(g_i^*) = \sum_{j \in N} C_j'(G^*).$$

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## Pigou Taxes (The "Incorrect Prices" Approach)

- Suppose *i* pays  $t_i g_i$  and receives  $T_i(\mathbf{g})$ .
- Then, in equilibrium:

$$rac{\partial B_{i}\left(g_{i}
ight)}{\partial g_{i}}=C_{i}^{\prime}\left(G
ight)+t_{i}-rac{\partial T_{i}\left(\mathbf{g}
ight)}{\partial g_{i}}.$$

• Equivalent: A subsidy  $T_i(\mathbf{g}) - t_i g_i$ , f.ex.  $t_i \cdot (\overline{g}_i - g_i)$ .

• This coincides with the first-best if e.g.:

$$t_{i}=\sum_{j\in N\setminus i}C_{j}^{\prime}\left( G
ight) ext{ and }rac{\partial \mathcal{T}_{i}\left( \mathbf{g}
ight) }{\partial g_{i}}=0.$$

• In principle, it is (almost) irrelevant how tax revenues are spent.

- For example:  $T_i(\mathbf{g}) = \sum_{j \in N \setminus i} t_j g_j / (n-1)$ .
- If  $C'_i \approx 0$  for each emitter, the linear tax is the same for all:

$$t = \sum_{j \in \mathbb{N}} C'_{j}(G^{*}) \Rightarrow B'_{i}(g_{i}) = \sum_{j \in \mathbb{N}} C'_{j}(G^{*}).$$

### Pigou Taxes - Uncertainty

• Facing the same tax, we get:

$$B_{i}'(g_{i},\epsilon_{i})=t=B_{j}'(g_{j},\epsilon_{j})\,\forall\,(i,j)\in N^{2}$$

even if individual shocks  $(\epsilon_i)$  are private information.

• Then, define  $\boldsymbol{\epsilon}=(\epsilon_1,...,\epsilon_n)$  and

$$B(t,\epsilon) \equiv \sum_{i\in N} B_i \left( B_i^{\prime-1}(t,\epsilon_i),\epsilon_i \right).$$

The optimal tax is given by:

$$\max_{t} \mathsf{E}\left[B\left(t, \epsilon\right) - C\left(\sum_{i \in N} B_{i}^{\prime-1}\left(t, \epsilon_{i}\right)\right)\right]$$

## Pigou Taxes - Uncertainty - Example Q

• Consider the quadratic approximation (Y=exp. "bliss" point):

$$B\left( {\left( {G,\epsilon } 
ight)} = -rac{b}{2}\left( {Y - G - \epsilon } 
ight)^2$$
 and  $C\left( {G} 
ight) = rac{c}{2}G^2$ 

where the aggregate shock is  $\epsilon \in \mathbb{R}$ ,  $E\epsilon = 0$ , and variance  $E\epsilon^2 = \sigma_{\epsilon}^2$ . • The equilibrium, given t:

$$\max_{G} -\frac{b}{2} \left(Y - G - \epsilon\right)^{2} - tG \Rightarrow b \left(Y - G - \epsilon\right) = t.$$

The tax pins down B' and B, leaving the uncertainty to G and C(G).
The optimal t:

$$\max_{t} - \frac{t^{2}}{2b} - \mathsf{E}\frac{c}{2}\left(Y - \epsilon - t/b\right)^{2} \Rightarrow t^{*} = c\left(Y - t^{*}/b\right) = \frac{cbY}{b+c}.$$

• The uncertainty does not influence the optimal level of t. (Why?)

• Welfare loss relative to no uncertainty increases in c:

$$L_t^{\epsilon} = \frac{c\sigma_{\epsilon}^2}{2}.$$

#### Pigou Taxes and Tax Revenues

• Tax revenues (at the above optimal  $t^*$ ):

$$\mathsf{E}tG = \mathsf{E}rac{cbY}{b+c}\left(Y-\epsilon-rac{cY}{b+c}
ight) = rac{cb^2Y^2}{b+c}.$$

• Tax revenues (at general t):

$$t(Y-\epsilon-t/b)$$

- Normally, revenues necessitate distortionary taxes.
- With the social value  $\lambda$ , the optimal t is thus:

$$\max_{t} - \frac{t^{2}}{2b} - \mathsf{E}\frac{c}{2} \left(Y - \epsilon - t/b\right)^{2} + \mathsf{E}\lambda t \left(Y - \epsilon - t/b\right) \Rightarrow$$
$$t = c \left(Y - t/b\right) + \lambda b \left(Y - 2t/b\right) = \frac{cb + \lambda b^{2}}{b + c + 2\lambda b} Y.$$

- which can be increasing or decreasing in  $\lambda$ ...
- RQ: (When) is there a "double dividend"?

#### Proposition

- Weak form: The regulation with Pigou tax revenues raises social efficiency relatively to regulation without tax revenues.
  - Holds trivially
- **2** Strong form: The optimal tax is larger than the Pigovian level.
  - The strong form may or may not hold.

## Coase (The "Property Rights" Approach)

- Suppose disagreement leads to the "default" payoffs  $u_i^D$ . For example,  $u_i^D$  may equal  $u_i$  ( $\mathbf{g}^{BAU}$ ).
- To negotiate a better outcome, a "proposer", *i*, would prefer to:

$$\max_{\mathbf{g},\mathbf{t}} u_{i} = B_{i}\left(g_{i}\right) - C_{i}\left(G\right) - t_{i} \text{ s.t.}$$
$$u_{j} = B_{j}\left(g_{j}\right) - C_{j}\left(G\right) - t_{j} \geq u_{j}^{D}\left(\mathsf{IR}_{j}\right).$$

- With budget balance,  $t_i = -\sum_{j \in N \setminus i} t_j$ , so *i* prefers the largest  $t_j$ 's satisfying IR<sub>j</sub>.
- $IR_j$  can be substituted into  $u_i$ , so that *i* maximizes:

$$\begin{aligned} \max_{\mathbf{g},\mathbf{t}} u_i &= B_i\left(g_i\right) - C_i\left(G\right) + \sum_{j \in N \setminus i} \left[B_j\left(g_j\right) - C_j\left(G\right) - u_j^D\right] \\ &= \sum_{j \in N} \left[B_j\left(g_j\right) - C_j\left(G\right)\right] - \sum_{j \in N \setminus i} u_j^D = \sum_{j \in N} u_j\left(\mathbf{g}^*\right) - \sum_{j \in N \setminus i} u_j^D. \end{aligned}$$

In other words: *i* maximizes the sum of payoffs (minus a constant).
Consequently, the proposed g<sub>j</sub>'s coincides with the first best.

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#### Theorem

- The parties negotiate the efficient outcome, regardless of the initial allocation of property rights (i.e., the default outcome,  $u_j^D$ ) as long as there are no 'transaction costs.'
- For example,  $u_j^D$  may reflect BAU (i.e., everyone has the "right" to emit as much as they want), or  $u_j^D$  could be  $u_j$  (**0**), i.e., no-one has the right to emit anything.
- "Transaction costs" (*tc<sub>i</sub>*) must be sufficiently small:

$$tc_i \leq \sum_{j \in \mathcal{N}} \left[ u_j \left( \mathbf{g}^* \right) - u_j^D 
ight].$$

- What is this "transaction cost"?
- To ensure an efficient outcome, the bargaining power should be given the party who faces the smallest transaction costs (i.e., the party who can easily contact others or who has most information) (RQ: Why?)

## Trading Pollution Permits ("Missing Market")

 If i has the right to emit Q<sub>i</sub><sup>0</sup>, while j has the right to emit Q<sub>j</sub><sup>0</sup>, the two might benefit from trading without increasing total emission:

$$g_i+g_j\leq Q_i^0+Q_j^0.$$

- That is, if *i* emits  $g_i$  and sell  $Q_i^0 g_i$ , *j* can emit  $g_j$  from buying  $g_j Q_j^0 = Q_i^0 g_i$  from *i*.
- This trade is beneficial as long as  $B'_i < B'_j$ .
- With efficient trade,  $B'_i = B'_i$ .
- More generally, a proposer *i* prefers to:

$$\begin{array}{lll} \max_{\mathbf{g},\mathbf{t}} u_i &=& B_i\left(g_i\right) - C_i\left(G\right) - t_i \text{ s.t.} \\ u_j &=& B_j\left(g_j\right) - C_j\left(G\right) - t_j \geq u_j^D \left(\mathsf{IR}_j\right) \text{ and} \\ \sum_{j \in N} g_j &\leq& \sum_{j \in N} Q_j^0 \text{ and } \sum_{j \in N} t_j \geq 0. \end{array}$$

• Consequently,  $B_i' = B_j'$  for all pairs (i,j)

• ...regardless of the endowments.

## Perfect Pollution Markets ("Missing Market")

- If  $n \to \infty$ , every *i* is likely to take the permit price *p* as given.
- If *i* owns  $Q_i^0$  permits already, *i* solves

$$\max_{g_{i}}B_{i}\left(g_{i}\right)-C_{i}\left(G\right)-p\left(g_{i}-Q_{i}^{0}\right)\Rightarrow B_{i}'\left(g_{i}\right)=p,$$

since  $G = \sum_{j \in N} Q_j^0$  is independent of  $g_i$ .

• The outcome is FB if:

$$p=\sum_{j\in N}C_{j}^{\prime}\left( G^{st}
ight) .$$

 I.e., the outcome is FB if the quantity (and thus the price) is "right", i.e., if:

$$B_i(g_i) = p = \sum_{j \in N} C'_j(G^*).$$

# Perfect Pollution Markets ("Missing Market")

#### Proposition

- When each emitter is a price-taker, the permit market equilibrium is efficient, regardless of the initial allocation of rights.
- RQ: Why is the initial allocation  $(Q_i^0)$  is irrelevant?
- RQ: Is that useful for the regulator? How will the regulator decide on the initial endowments? Must Q<sub>i</sub><sup>0</sup> be exogenous?
- What if  $Q_i^0$  depends on past production or past emissions?
- So, permit trade => FB whether n = 2 or  $n = \infty$ .
  - Should we expect FB also if  $n \in (2, \infty)$ ? Why/why not?
- With heterogeneous pollutants (i.e.,  $G = \sum_{j \in N} h_j g_j$ , the FB requires:

$$B_{i}^{\prime}\left(g_{i}
ight)=pq_{i}=\sum_{j\in\mathcal{N}}h_{i}C_{j}^{\prime}\left(G^{*}
ight)$$
 , so  $rac{q_{i}}{q_{j}}=rac{h_{i}}{h_{j}}$   $orall\left(i,j
ight)\in\mathcal{N}^{2}.$ 

### Perfect Pollution Markets - Uncertainty

- Private information: Conditions above (when n = ∞) hold if B<sub>i</sub> = B<sub>i</sub> (g<sub>i</sub>, ε<sub>i</sub>) and ε<sub>i</sub> is i's private information.
- Total benefit in equilibrium is:

$$B\left( {\left( {G,\epsilon } 
ight)} = \mathop {\max }\limits_{\mathbf{g}} \sum\limits_{j \in {N}} {B_j \left( {g_j,\epsilon _j } 
ight)} \,\,\, {
m s.t.} \,\,\, \sum\limits_{j \in {N}} {g_j } = G.$$

The optimal cap is

$$\max_{G} \mathsf{E}B(G, \epsilon) - C(G) \Rightarrow \mathsf{E}B'(G, \epsilon) = C'(G).$$

• Example Q (with a single aggregate shock  $\epsilon \in \mathbb{R}$ ):

$$\mathsf{E}b(Y-G+\epsilon)=cG\Rightarrow G^*=rac{b}{c+b}Y.$$

- The shock does not affect G, but only B'.
- Relative to no uncertainty, the welfare loss is:

$$L_G^{\epsilon} = \frac{b\sigma_{\epsilon}^2}{2}.$$

# Prices vs. Quantities (Weitzman '74)

#### Proposition

• The efficiency loss under quotas is smaller than under prices/taxes,  $L_G^{\epsilon} < L_t^{\epsilon}$ , IFF b < c.

- This holds generally when *B* and *C* are approximated by quadratic functions, no matter the distribution of errors, and even if there are (additive) shocks in the *C* function (RQ: Why?)
- Rather than comparing welfare to the situation without uncertainty, we can compare to the first-best outcome with the shock. (RQ: Why?)
- RQ: Without shocks in *B*(.), the shock in *C*(.) is irrelevant for the comparison, and then the slopes are also irrelevant. (Why?)
- RQ: How can the losses be reduced further?
- By hybrid schemes?
- Floor/ceiling for price?

- Pigou taxes raises revenues, which has an additional benefit.
- The willingness to pay for a quota is B', so the revenues when auctioning the initial quota endowments are:

$$rac{b}{c+b}Yb\left(Y-rac{b}{c+b}Y+\epsilon
ight)=rac{b^2Y}{c+b}\left(rac{c}{c+b}Y+\epsilon
ight)$$

- This has the same mean as the expected Pigou tax revenues.
- The variance of the auction revenues is smaller IFF b < c.
- This adds to the benefits of quotas, rather than taxes, IFF b < c.